# prior beliefs and projection

an RSA-based approach

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workshop on "background beliefs in the construction of meaning" University of Tübingen, January 9-10, 2025



#### The Guardian, April 26 2004

"Geographically, Europe can be divided in two parts: Europe of the hare and Europe of the squirrel. Estonia is the latter: a squirrel could, without too much trouble, go from one end of the country to the other, jumping from tree to tree. Of course, the squirrel doesn't know that Estonia includes hundreds of islands, small and big. Estonia is a land of islands and forests. [...]"

~ Estonia includes hundreds of islands



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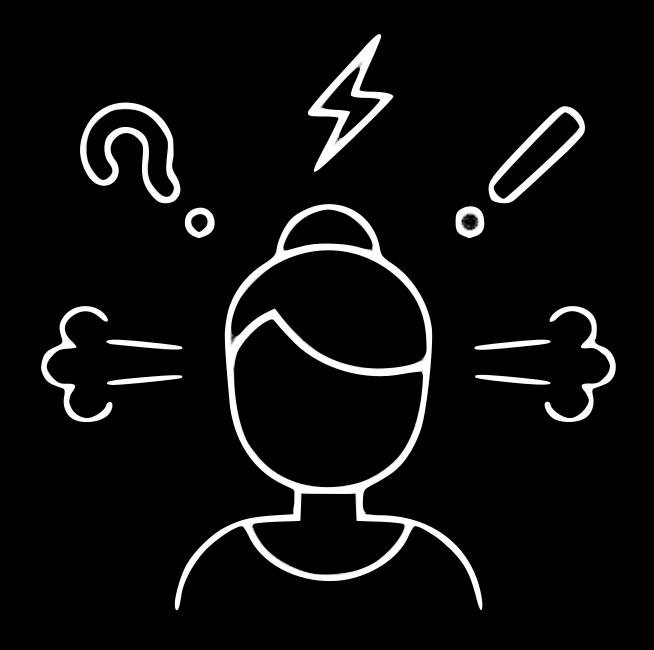
rescue strategy: accommodation

(e.g., Heim 1983, van der Sandt 1992)

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### rescue strategy: accommodation

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accommodation is a rescue strategy but with "informative" presuppositions it must apply in the majority of examples

(e.g., Delin 1995, Spenader 2003)

# "informative" presuppositions

CC of clause-embedding predicates (know, discover, realize, regret...)

Pre-state of change-of-state predicates (stop, continue,...)

Content of temporal clauses (before, after,...)

Existential content of clefts (e.g., It was Alvin who arrived)

Possession content of possessive NPs (e.g., Brenda's parrot)

Prejacent of only (e.g., Only Cassie danced)

Prejacent of manner adverb sentences (e.g., Simone ran quickly)



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Nancy asks: "Does Cole know that Julian dances salsa?"

→ Julian dances salsa

- 1. Nancy knows (and we know) that Julian is Cuban.
- 2. Nancy knows (and we know) that Julian is German.

(Degen & Tonhauser 2021, Open Mind; ms under review)

allow for the principled integration of information from multiple factors (lexical entailments, compositional semantics, prior beliefs, QUDs,...)

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instead of developing analyses tailored to informative presuppositions, we **can** and **should** develop more general analyses that make predictions about inferences drawn from utterances

informative presuppositions are just one kind of inference

factors that modulate informative presuppositions also modulate other types of inferences

### factors that modulate informative presuppositions

lexical meaning compositional semantics question under discussion prior beliefs alternatives

(e.g., Abrusán 2011, 2016; Abusch 2002, 2010; Chemla 2009; Cummins & Rohde 2015; Degen & Tonhauser 2021, 2022, under review; Djärv & Bacovcin 2020; Romoli 2015; Simons et al 2010, 2017)

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Rational Speech Act (RSA) modeling framework

Cole doesn't think/know that Charley speaks Spanish.

→ Charley speaks Spanish

#### Cole doesn't think/know that Charley speaks Spanish.

Charley speaks Spanish

# empirical targets

know projects more than think

(e.g., Kiparsky & Kiparsky 1970; Degen & Tonhauser 2022)

prior beliefs modulate projection

(e.g., Mahler 2020, 2022; Degen & Tonhauser 2021)

QUDs modulate projection

(e.g., Abrusán 2011, 2016; Simons et al 2017; Tonhauser et al. 2018, Degen & Tonhauser under review)

### basic model

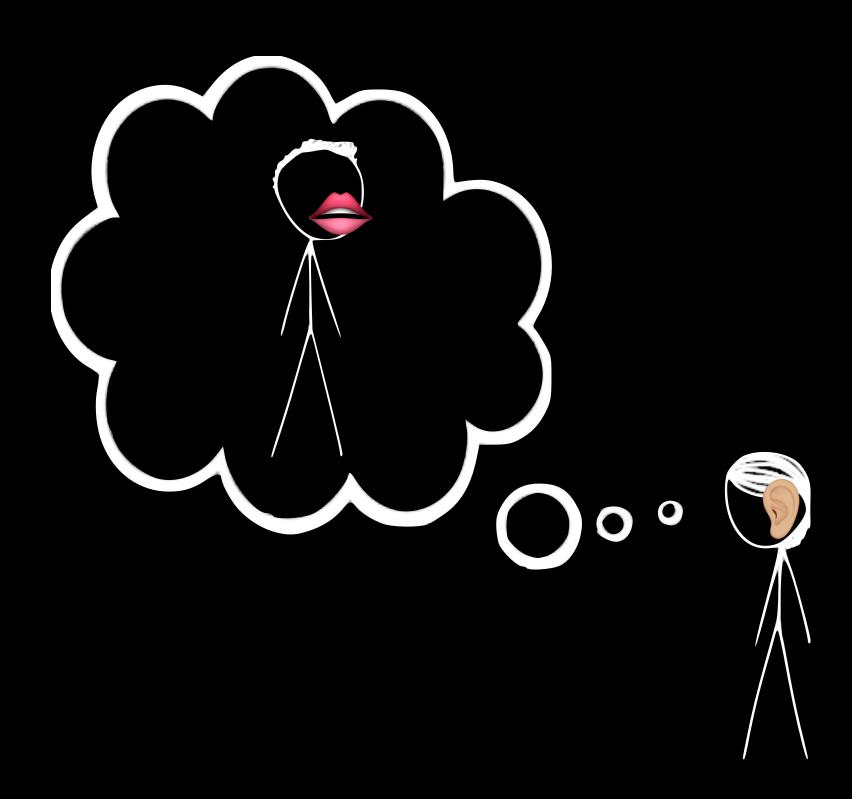
$$P_{L_0}(Q(w) \mid u, CG, Q) \propto \sum_{w' \in CG \cap \llbracket u \rrbracket} \delta_{Q(w) = Q(w')} \cdot P(w')$$
 literal listener

$$P_{S_1}(u \mid w, CG, Q) \propto exp(\alpha(log(P_{L_0}(Q(w) \mid u, CG, Q) - C(u))))$$
 pragmatic speaker

$$P_{L_1}(Q(w), CG \mid u, Q) \propto P_{S_1}(u \mid w, CG, Q) \cdot P(w) \cdot P(CG)$$
 pragmatic listener

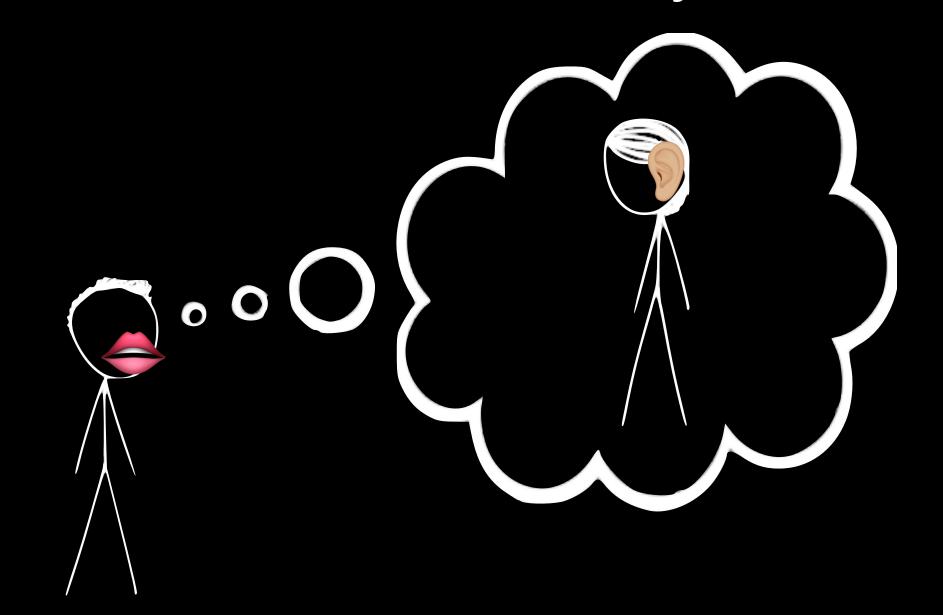
adapted from Qing et al. 2016 (CogSci) for stop

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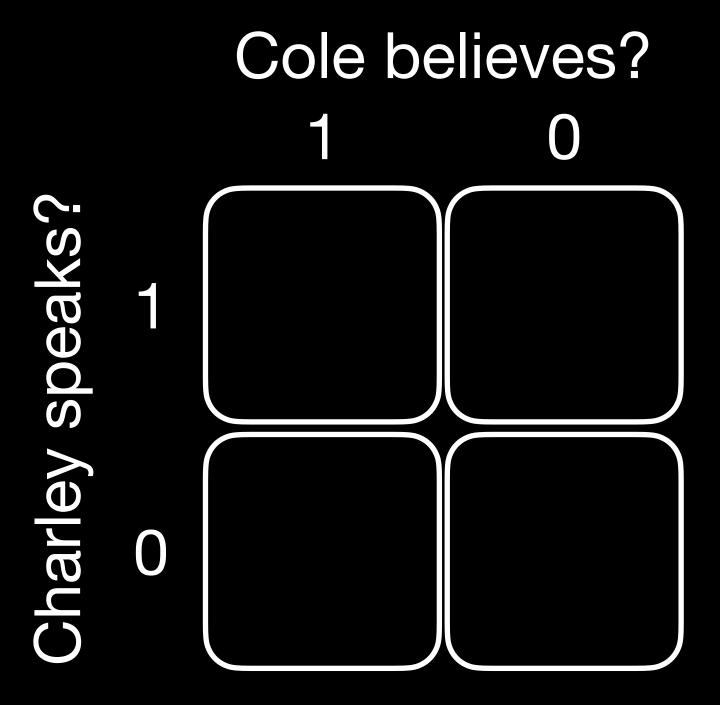
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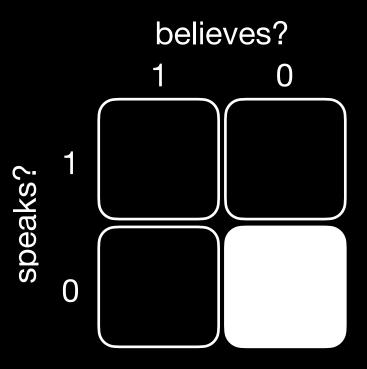
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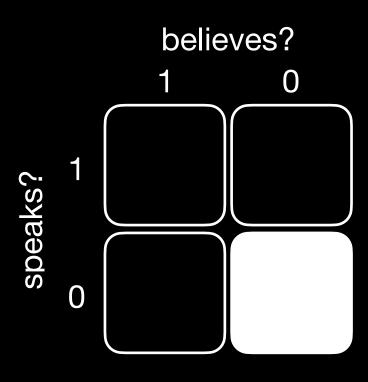
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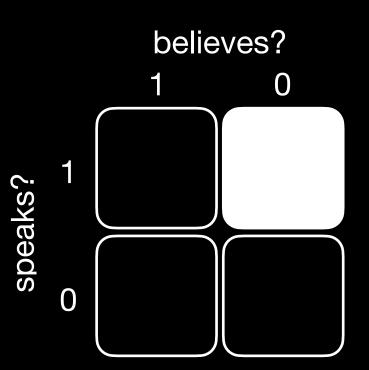
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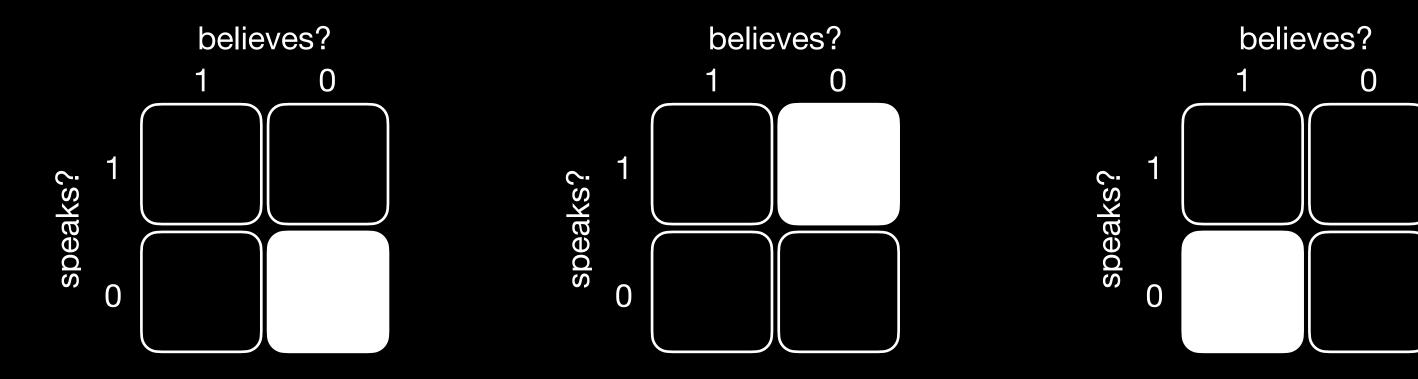
a *know* utterance is **more useful** to a speaker who is already privately **committed to the content of the complement** being true

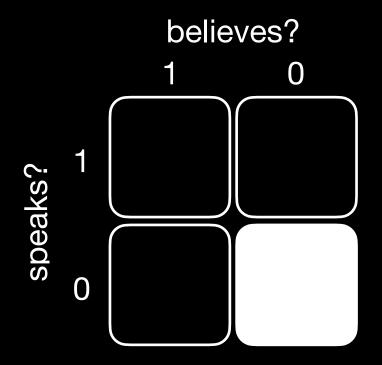


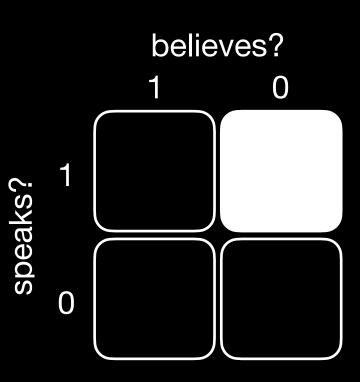


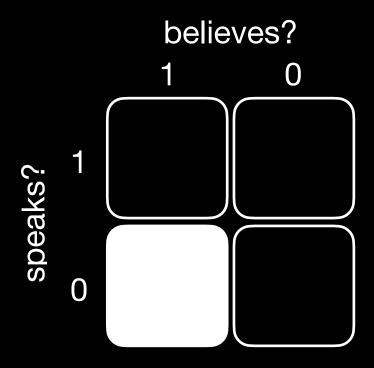


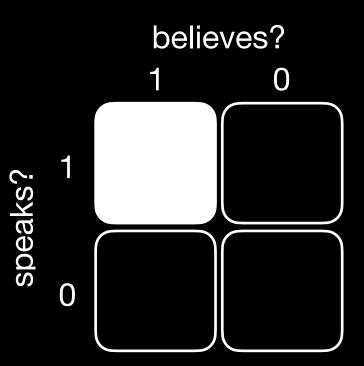




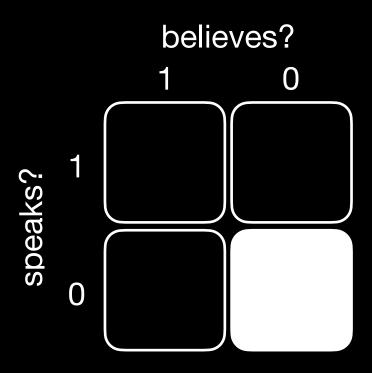


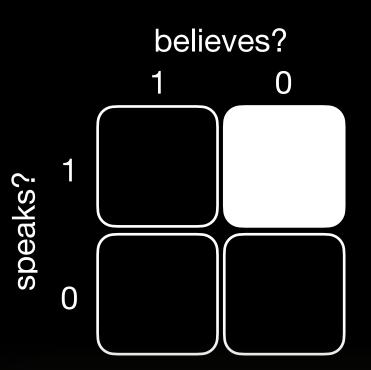


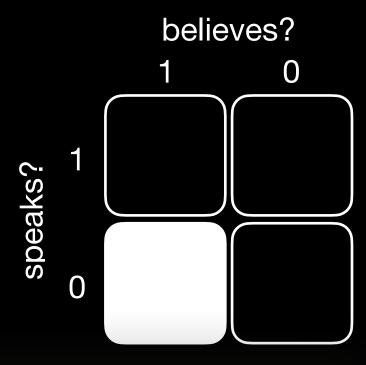


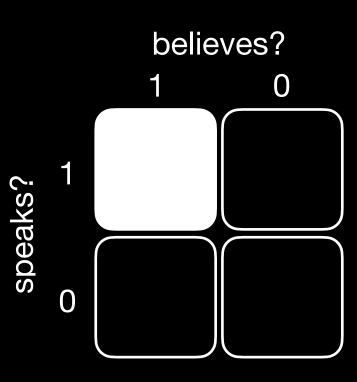


# prior belief manipulation



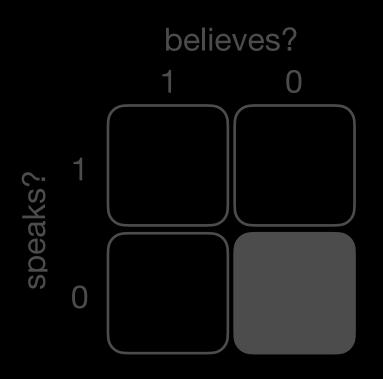


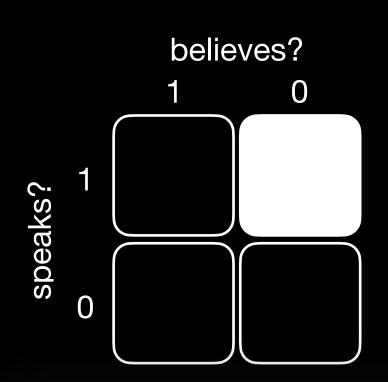


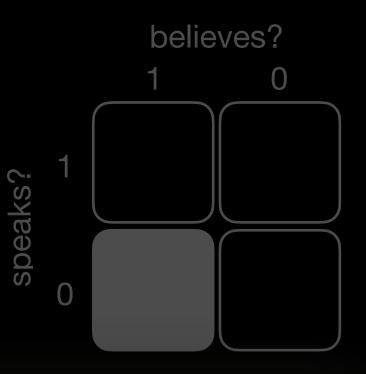


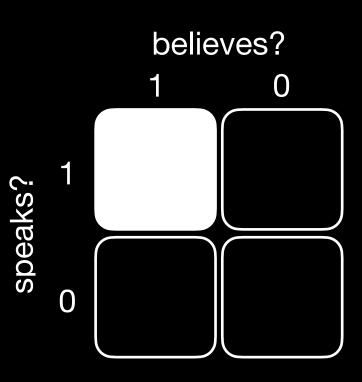


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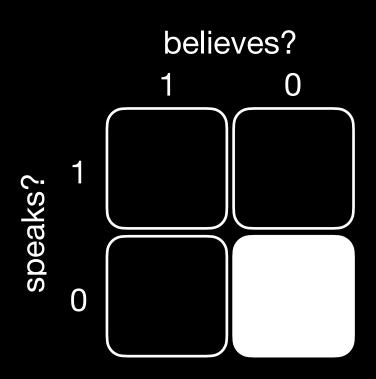


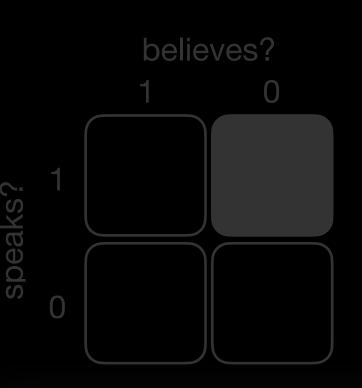


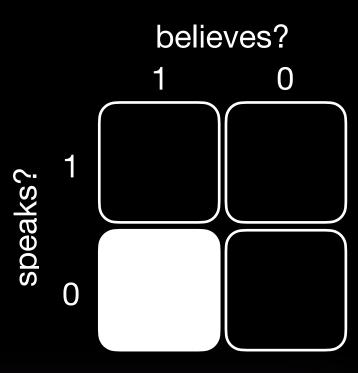




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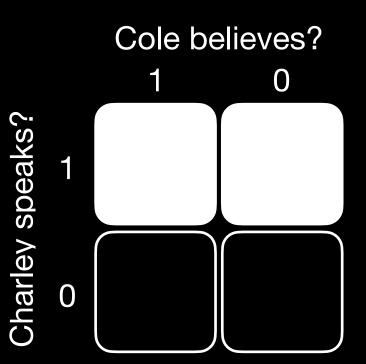




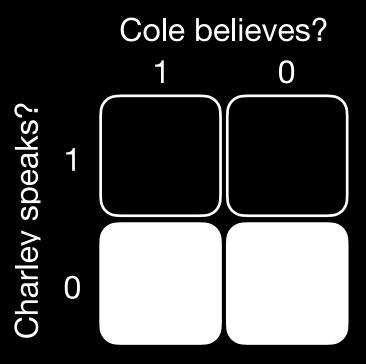
believes?



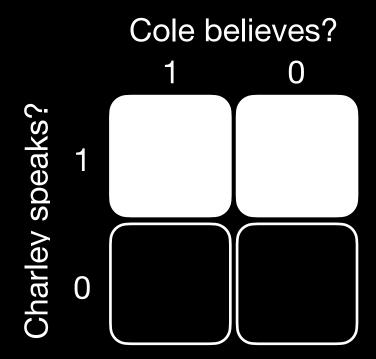
Charley speaks Spanish.



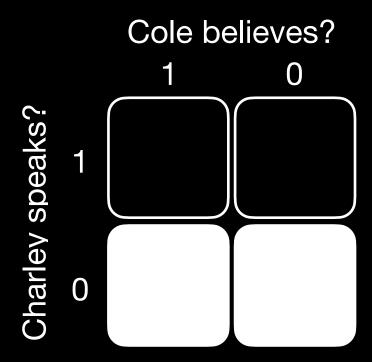
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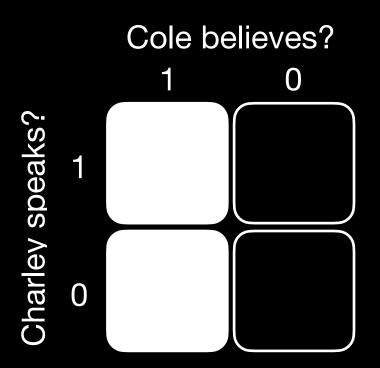
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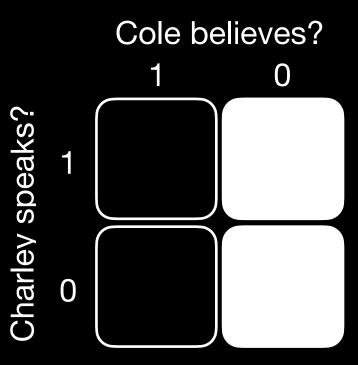


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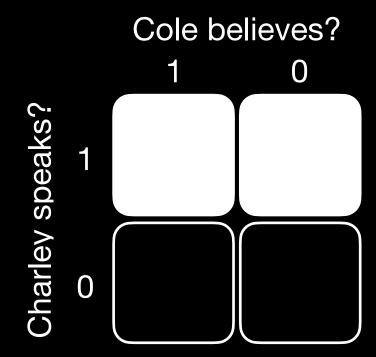


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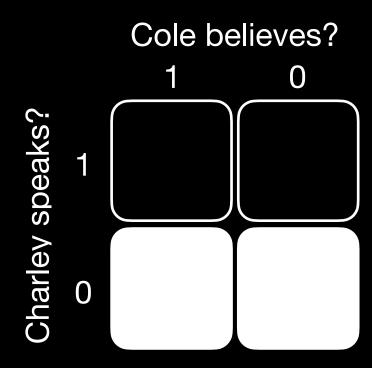




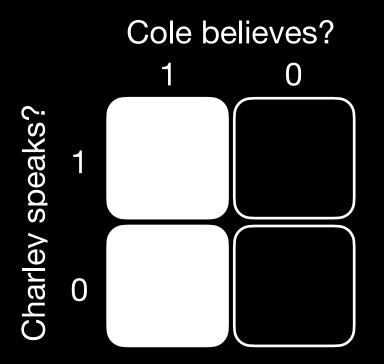
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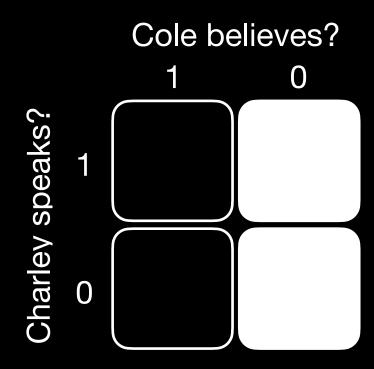
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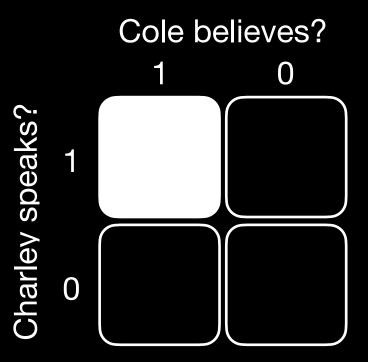
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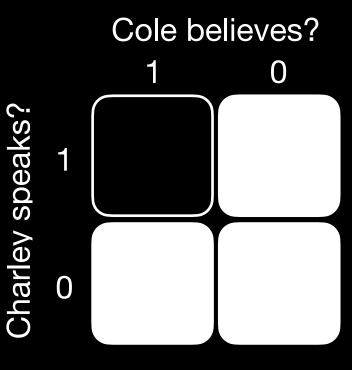


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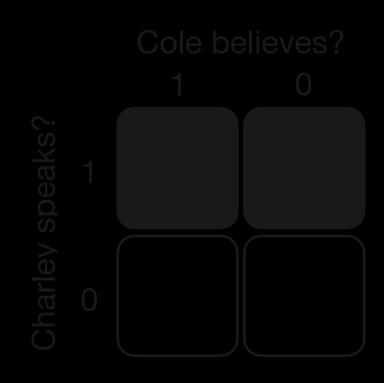


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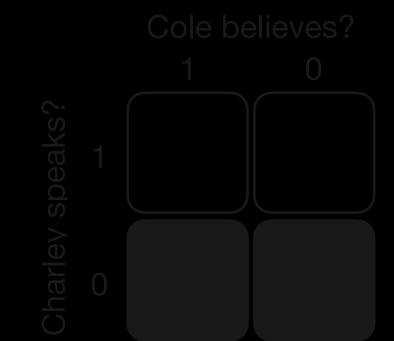


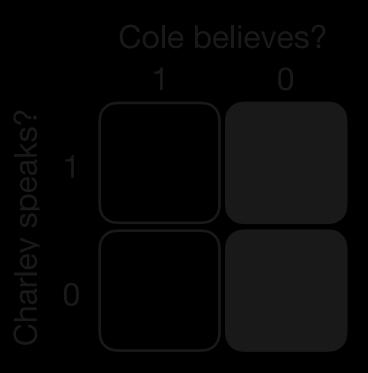
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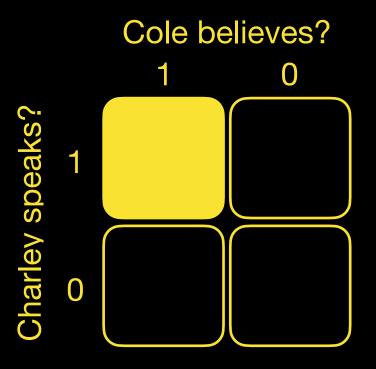
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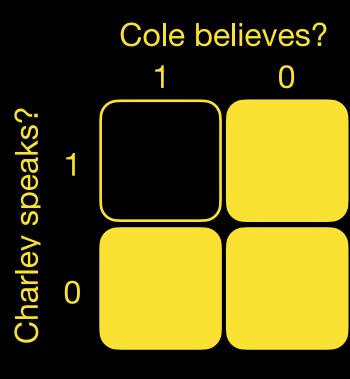




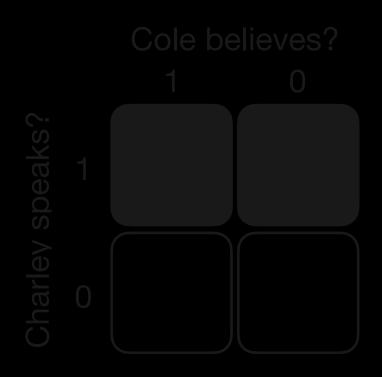


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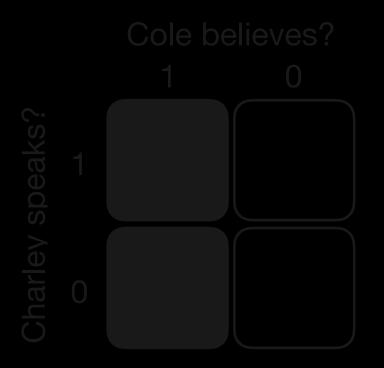




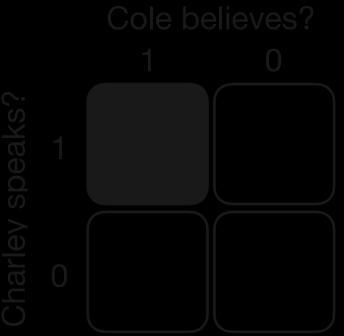
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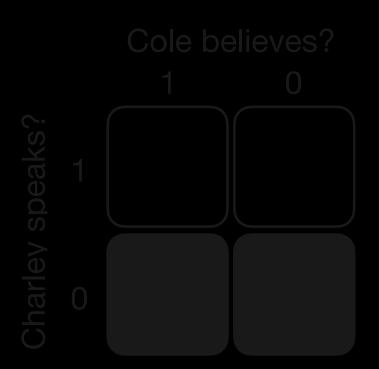
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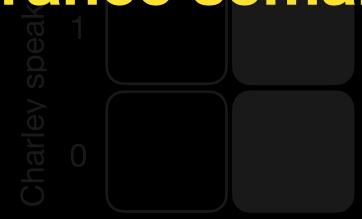


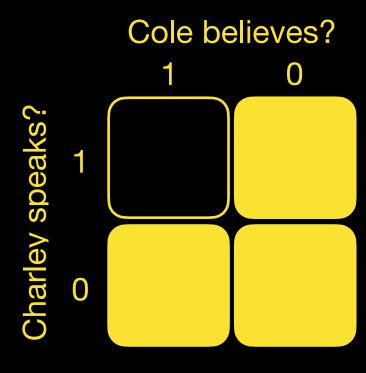
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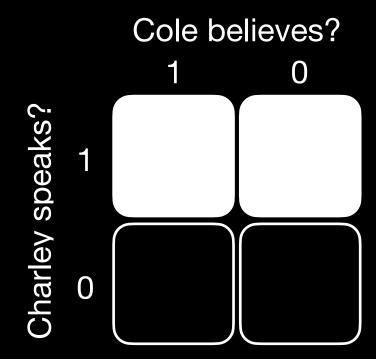
relatively uninformative utterance semantics



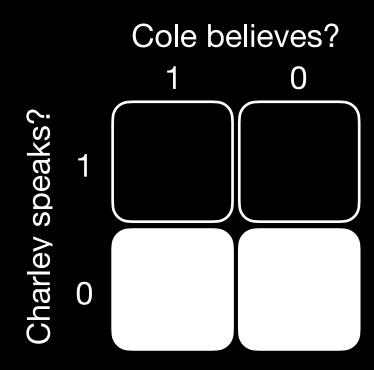


#### basic model utterances and semantics

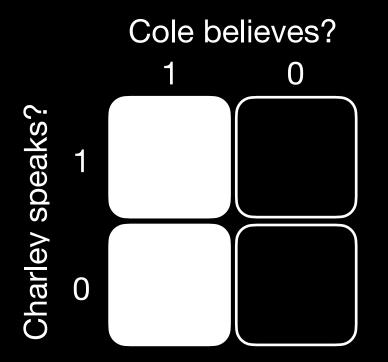
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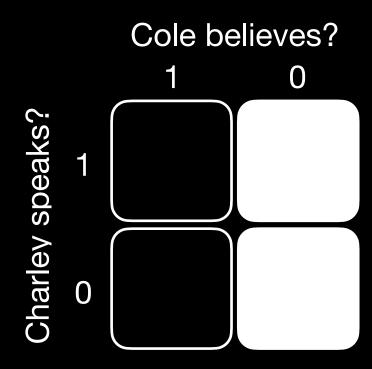
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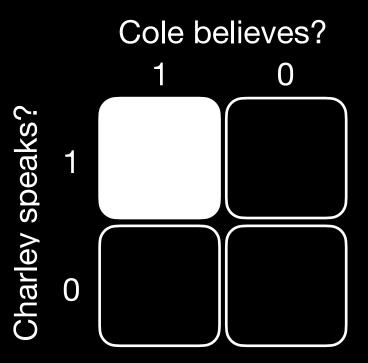
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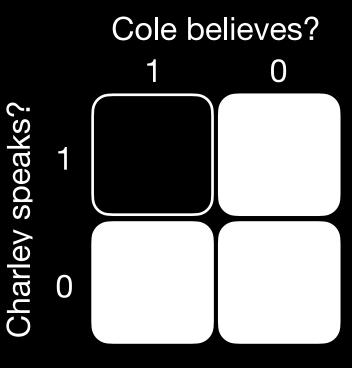
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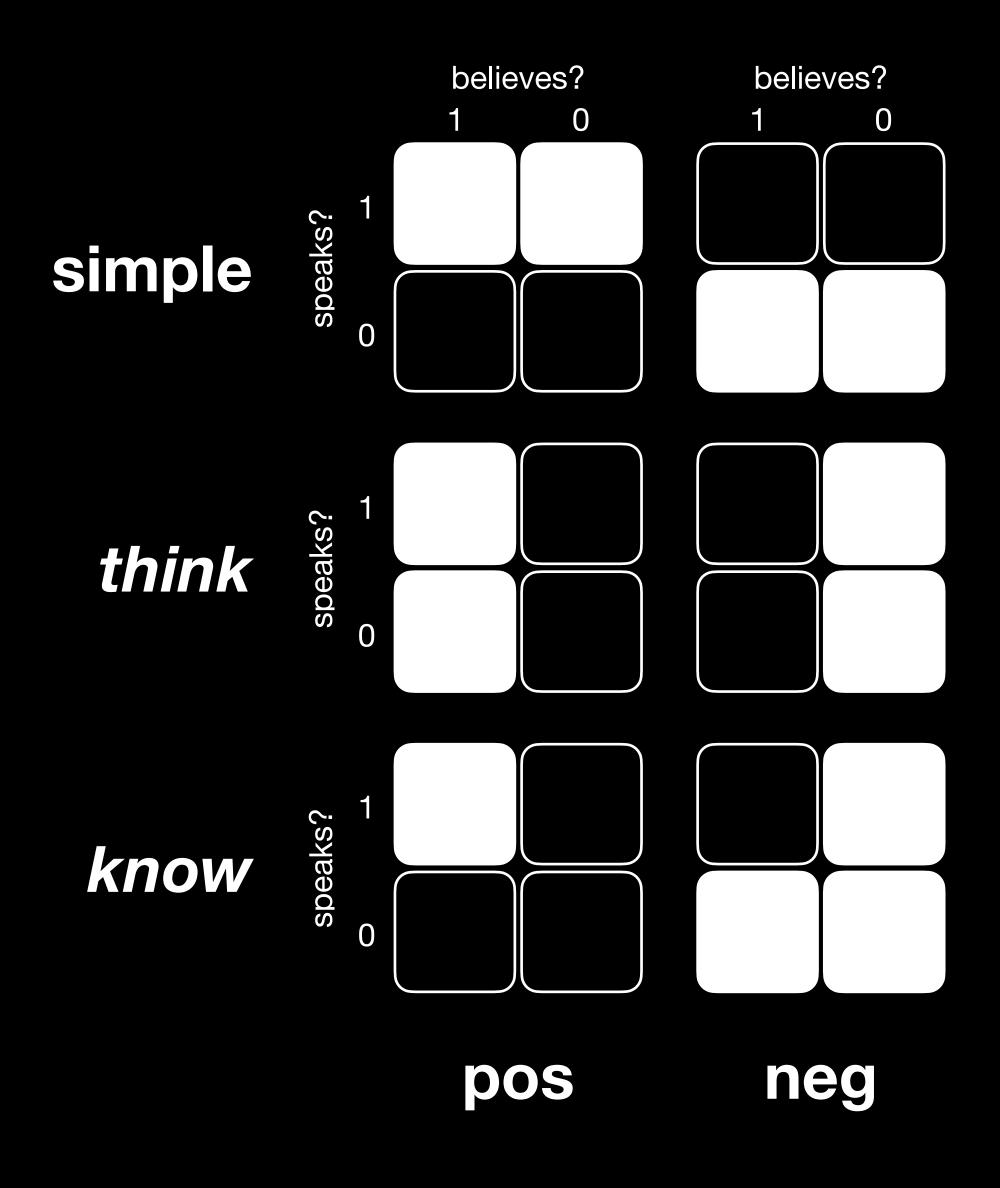
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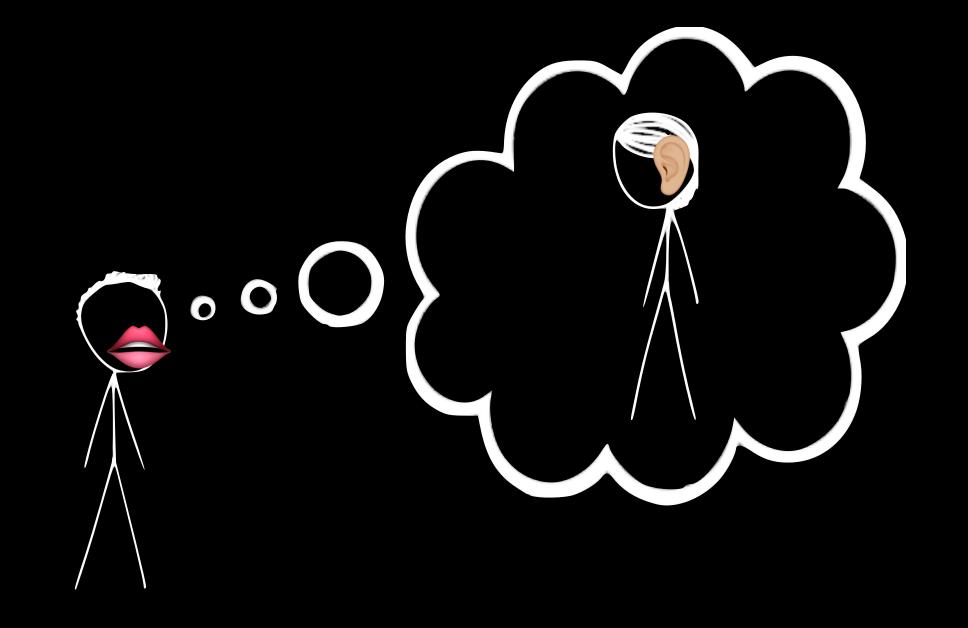
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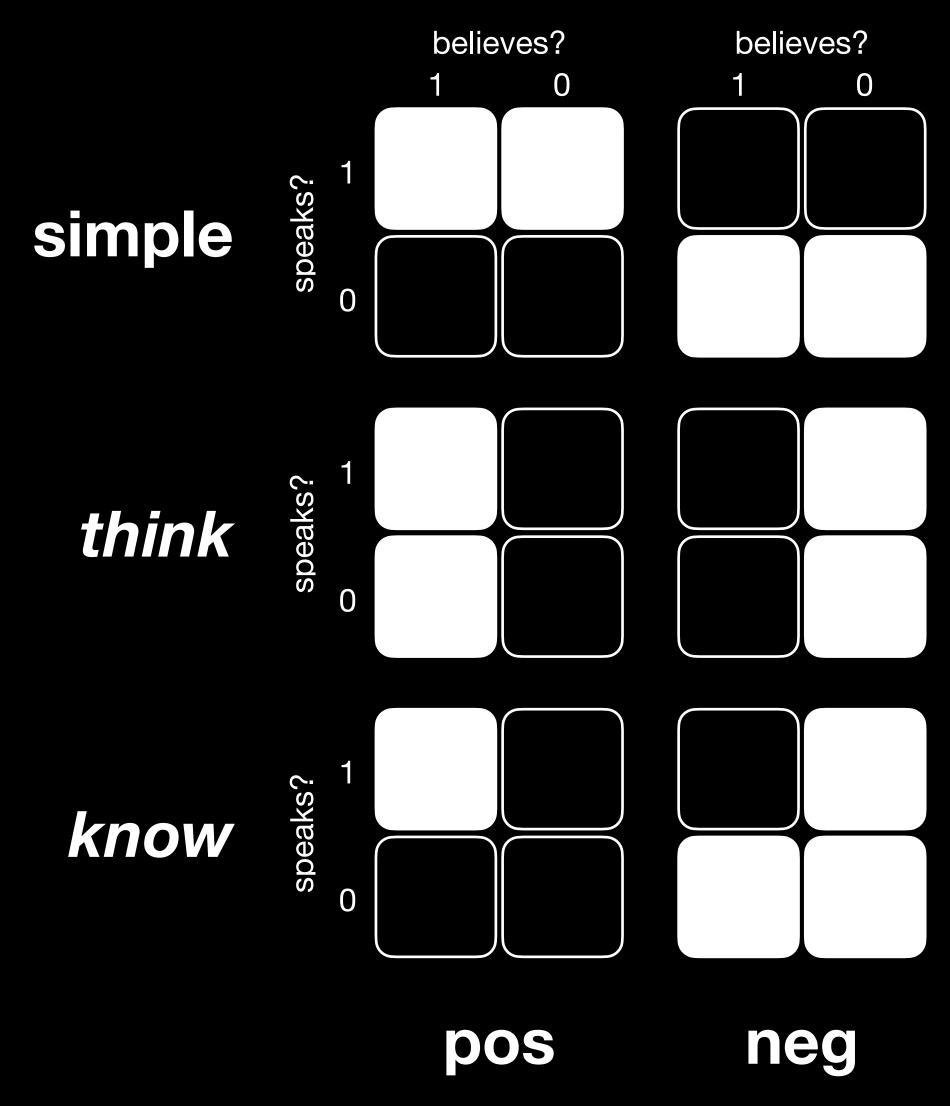


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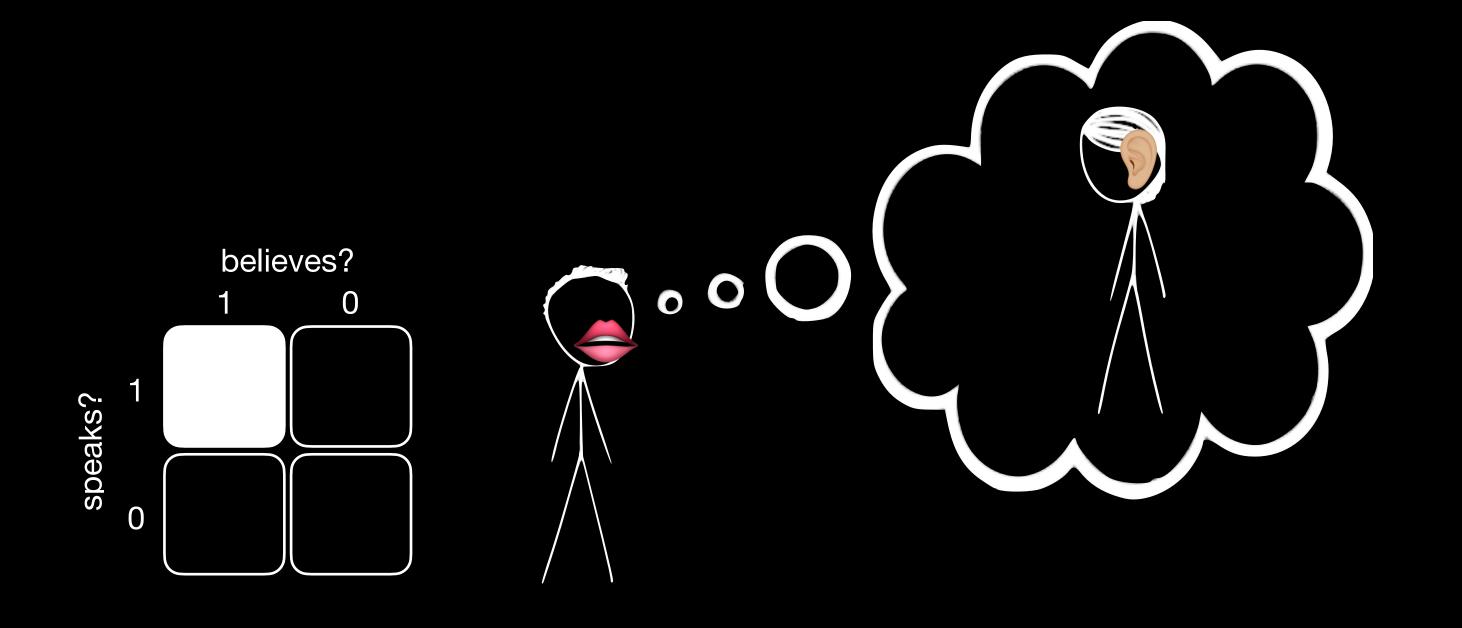


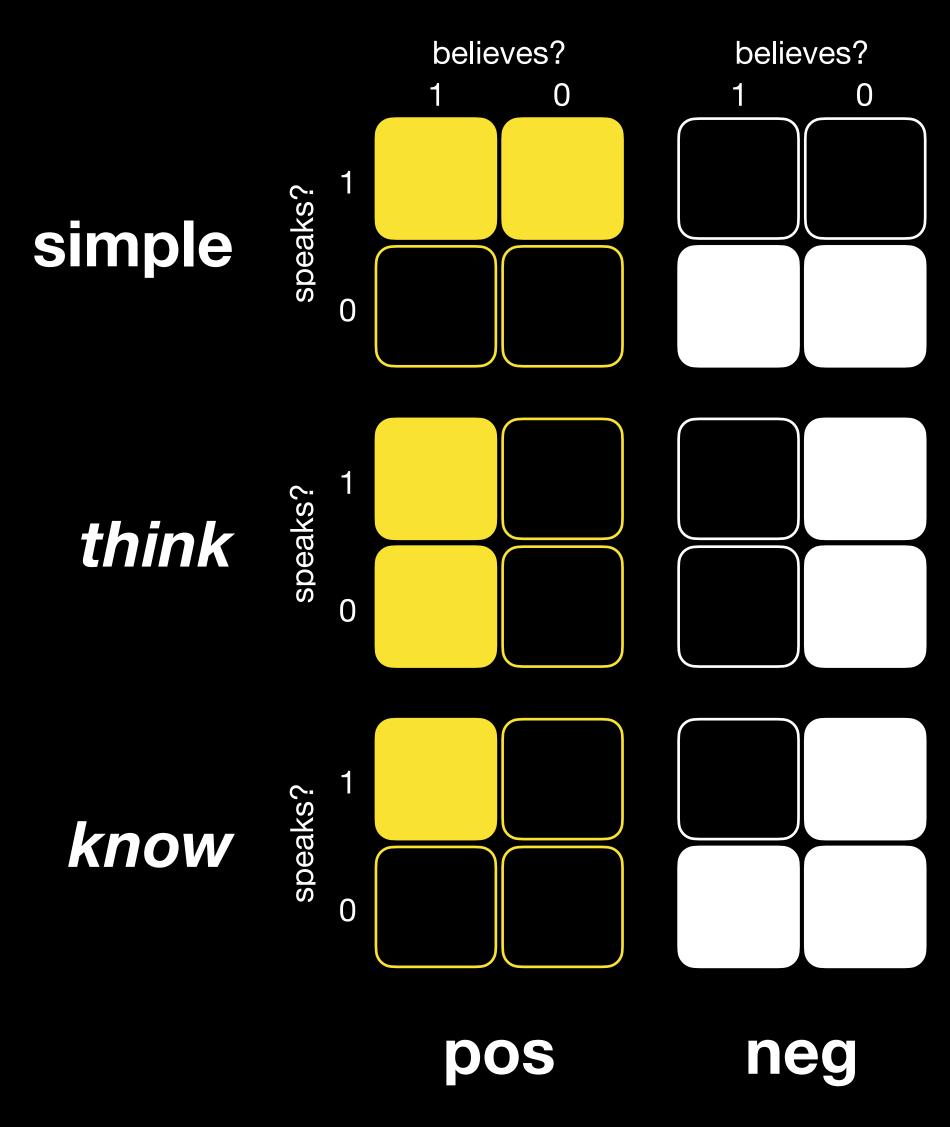
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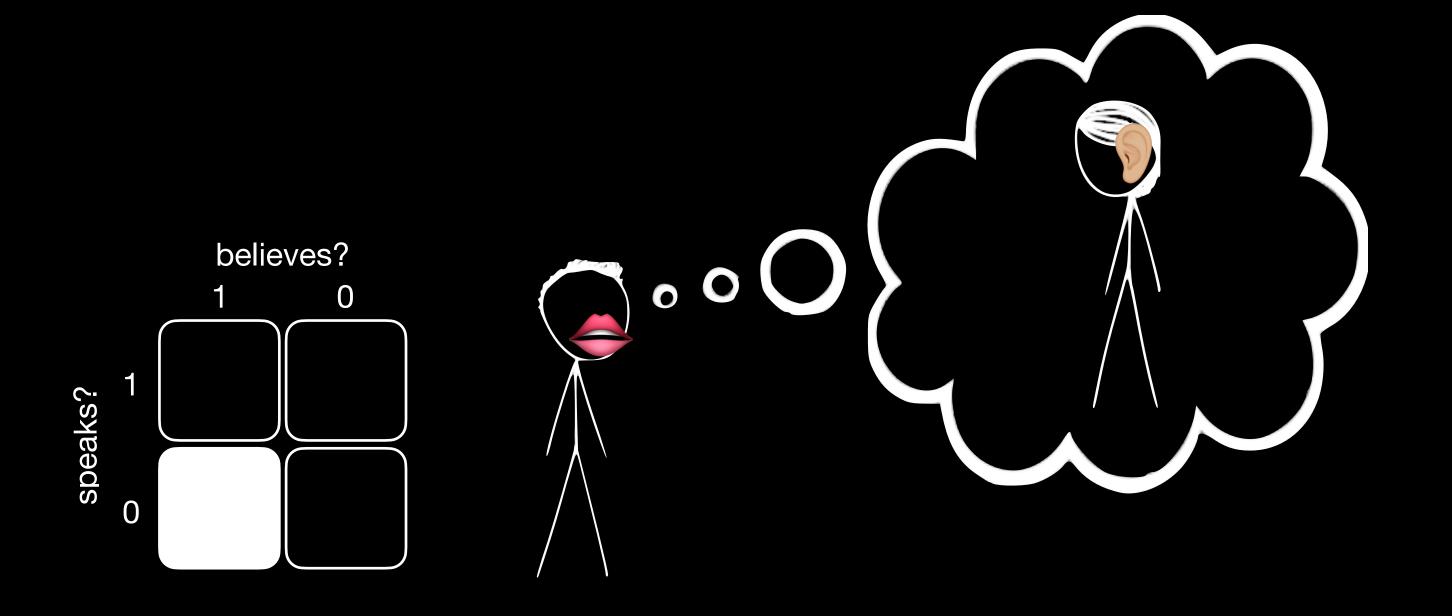


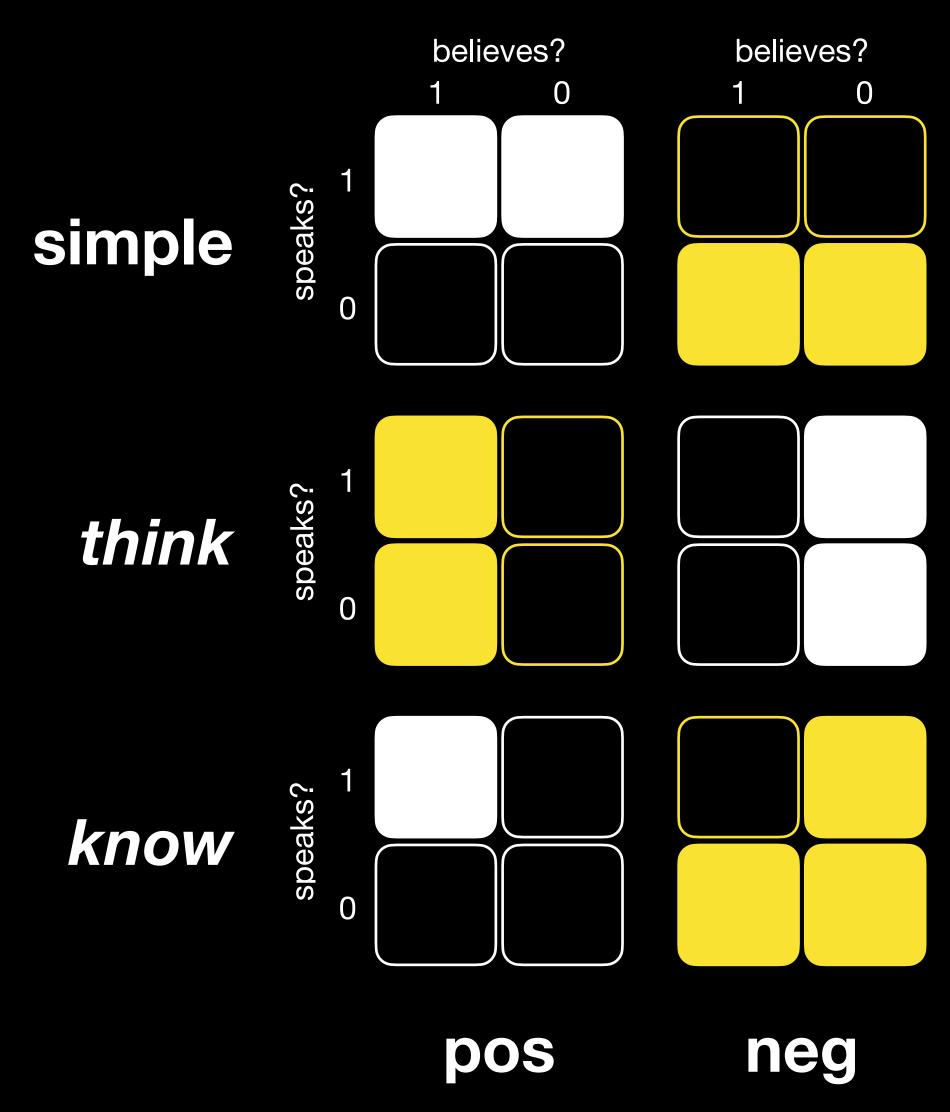
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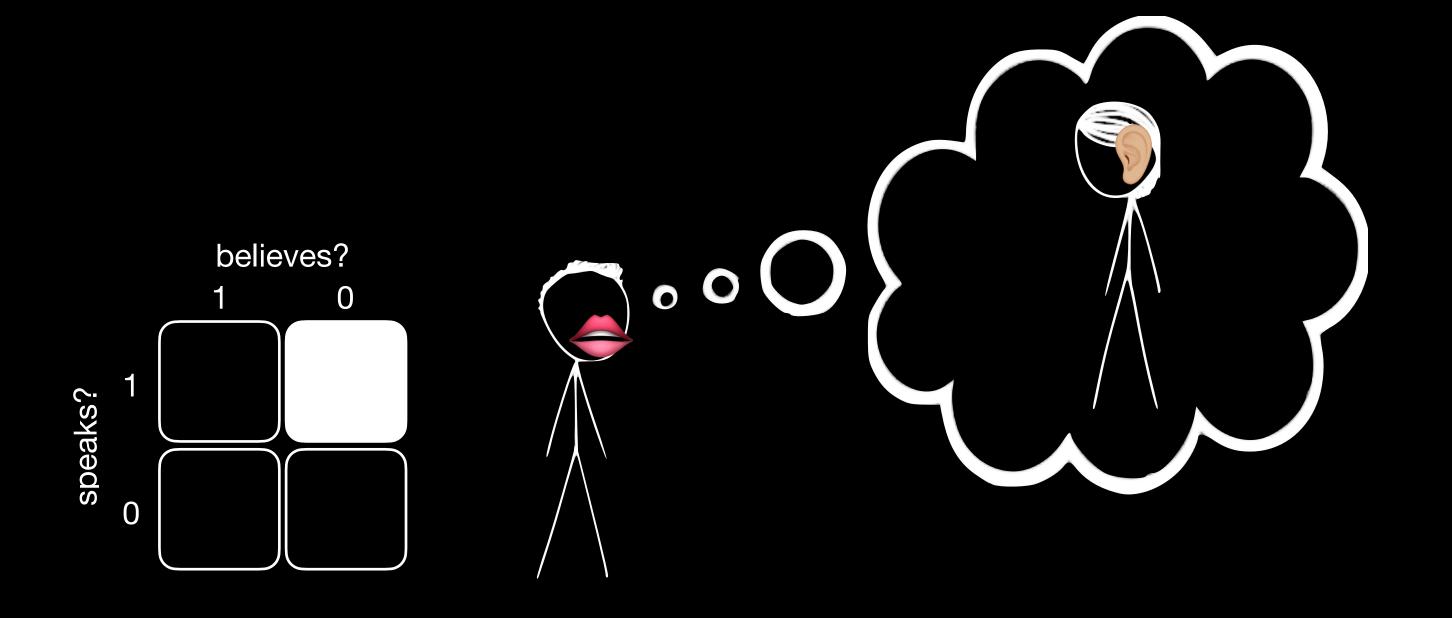


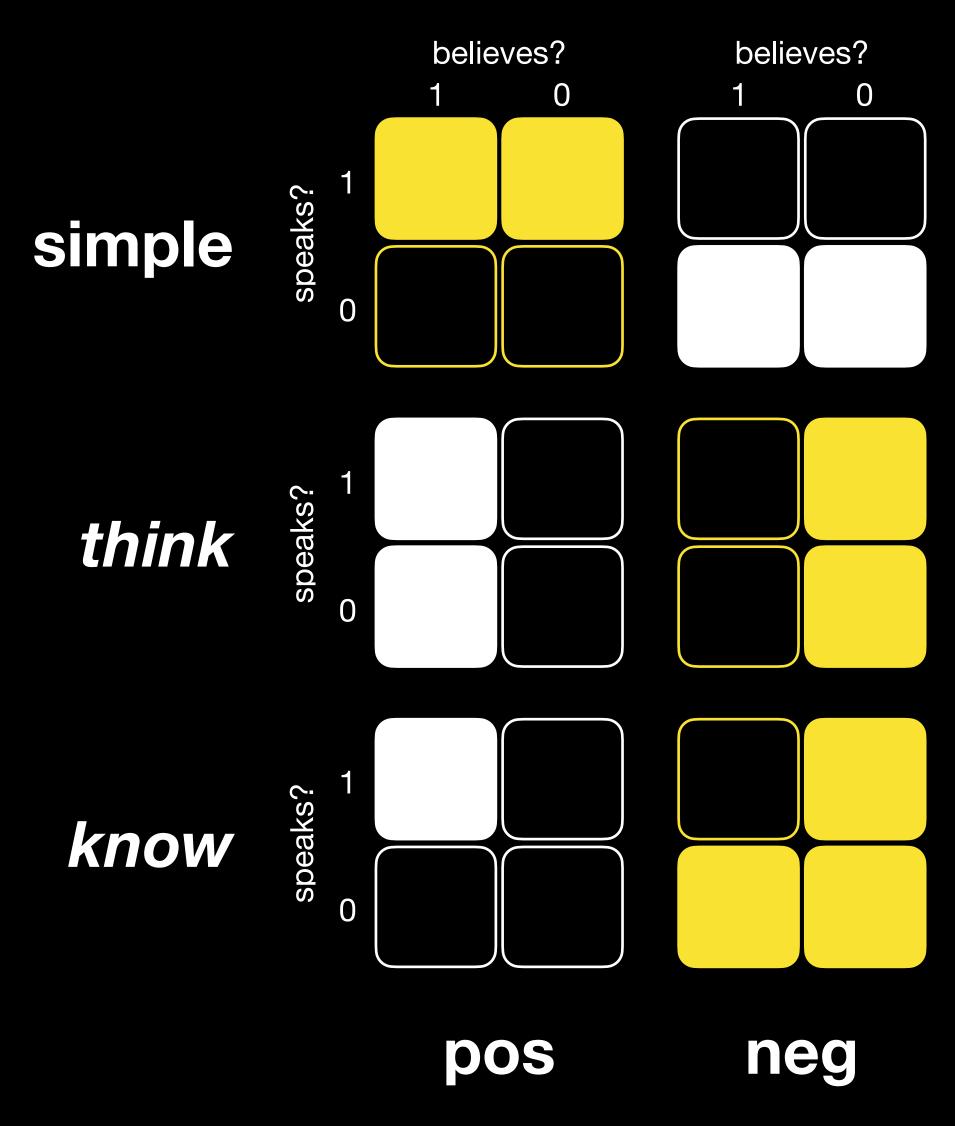
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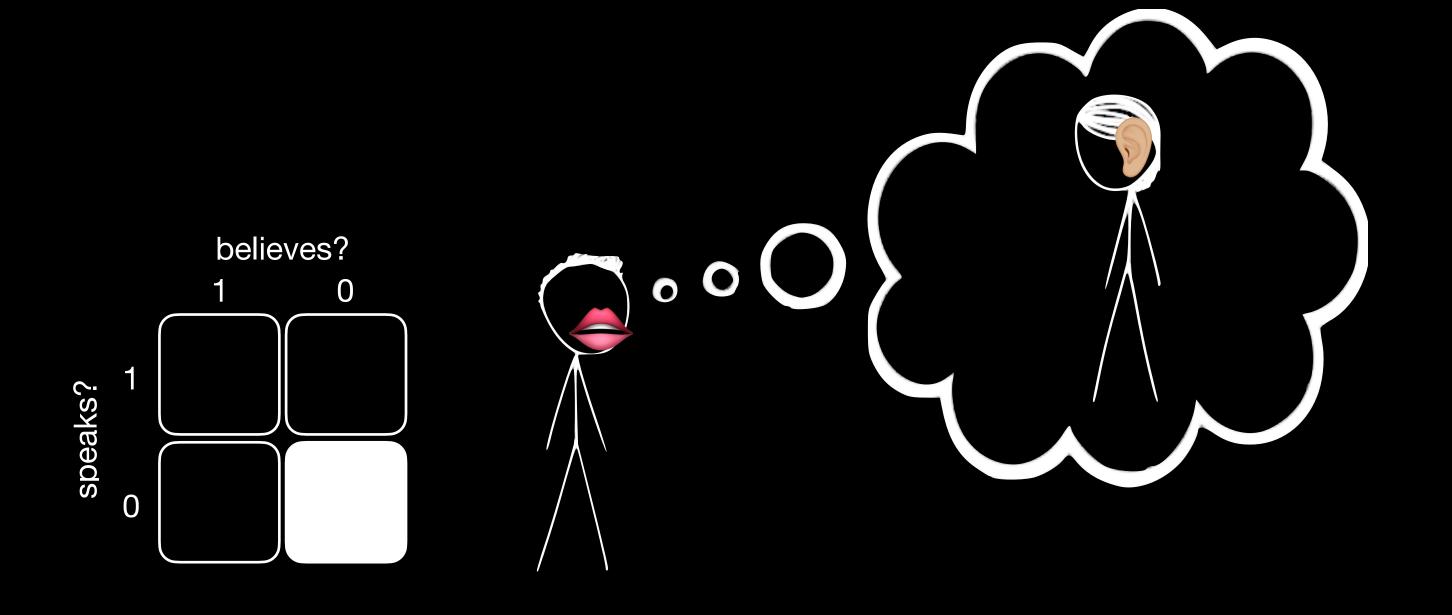


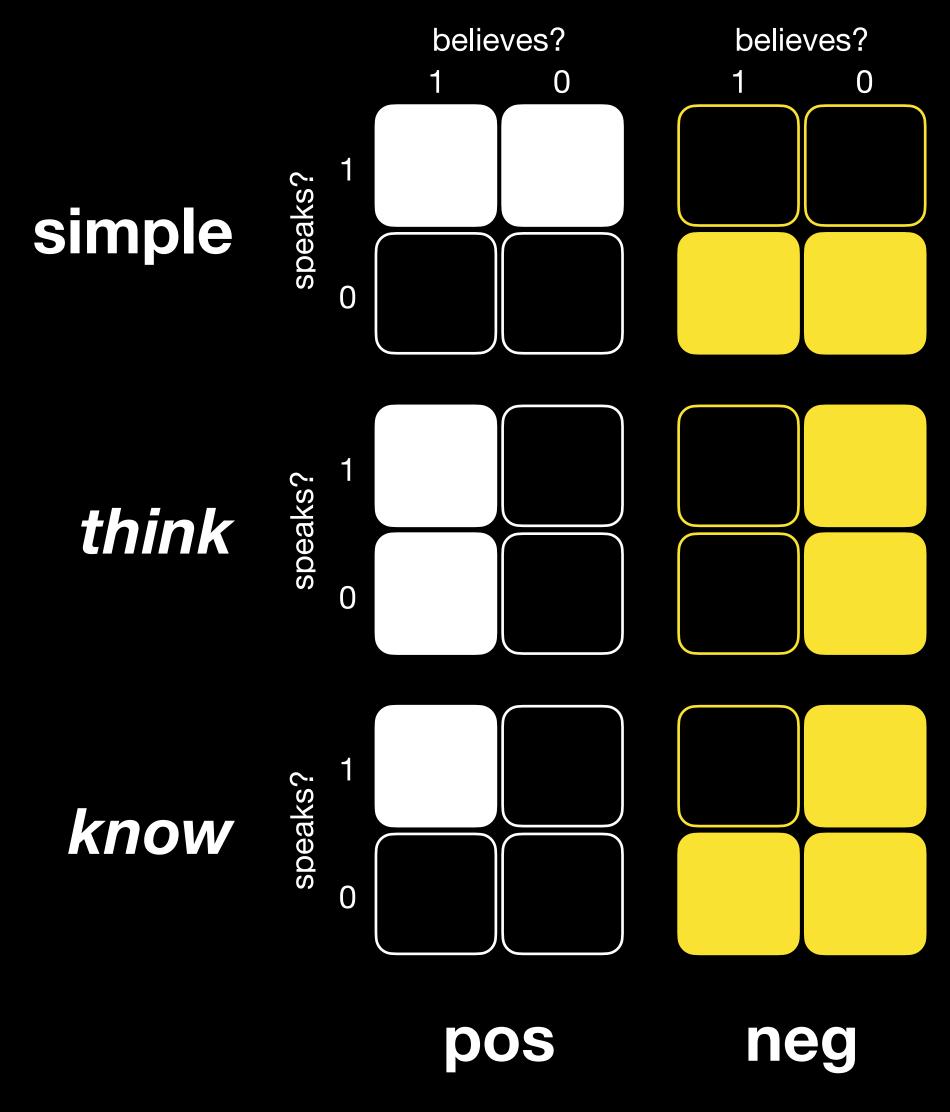
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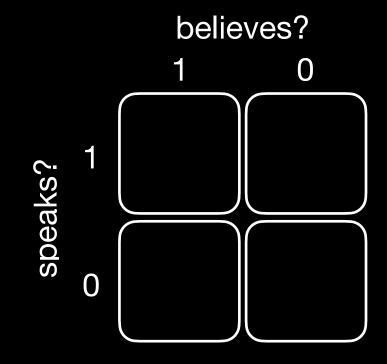
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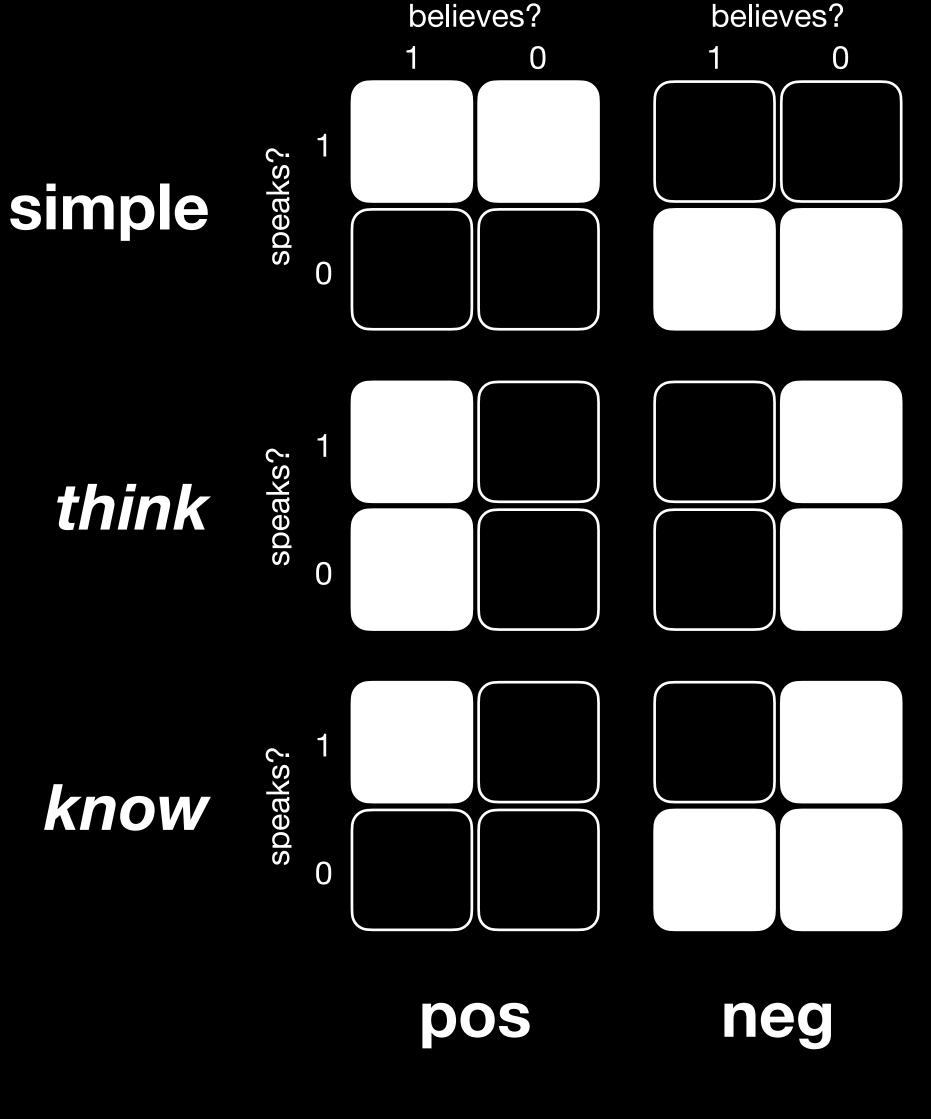




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so far, we've considered the QUD what is the state of the world?





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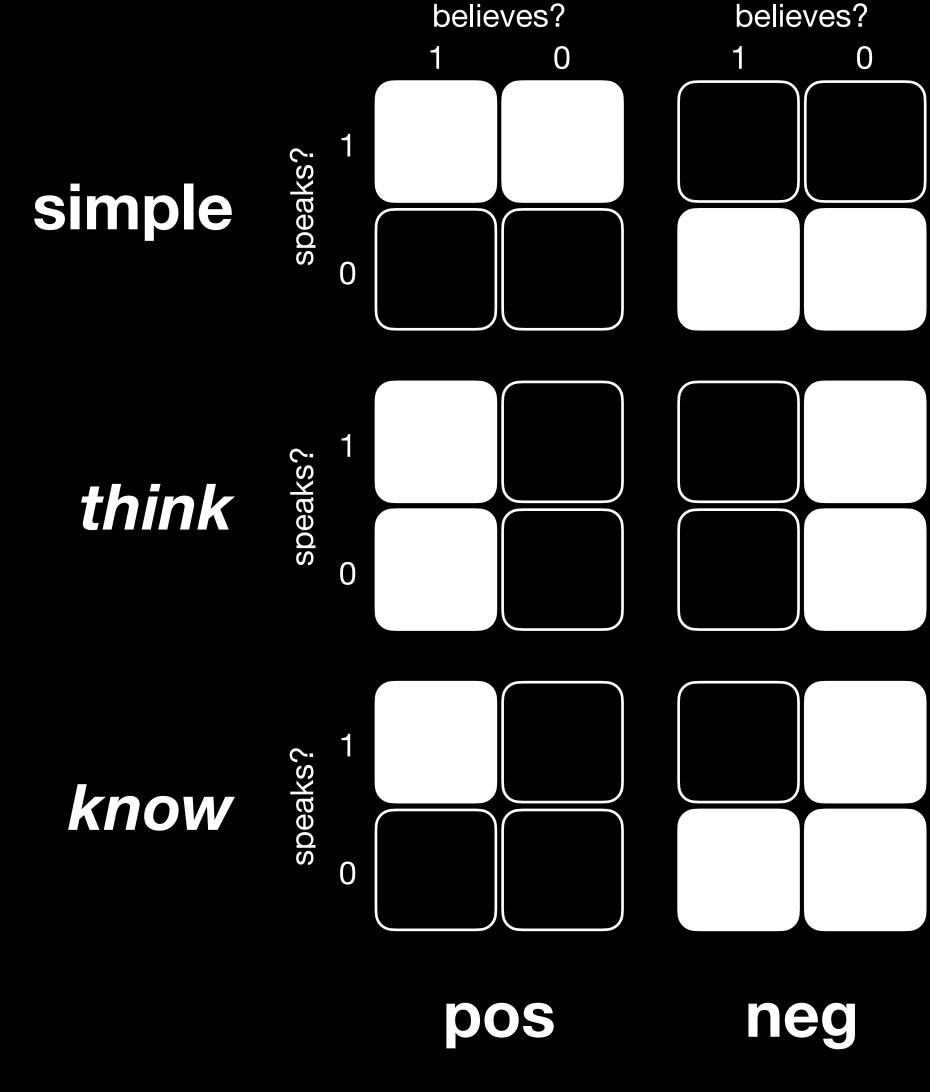
believes?

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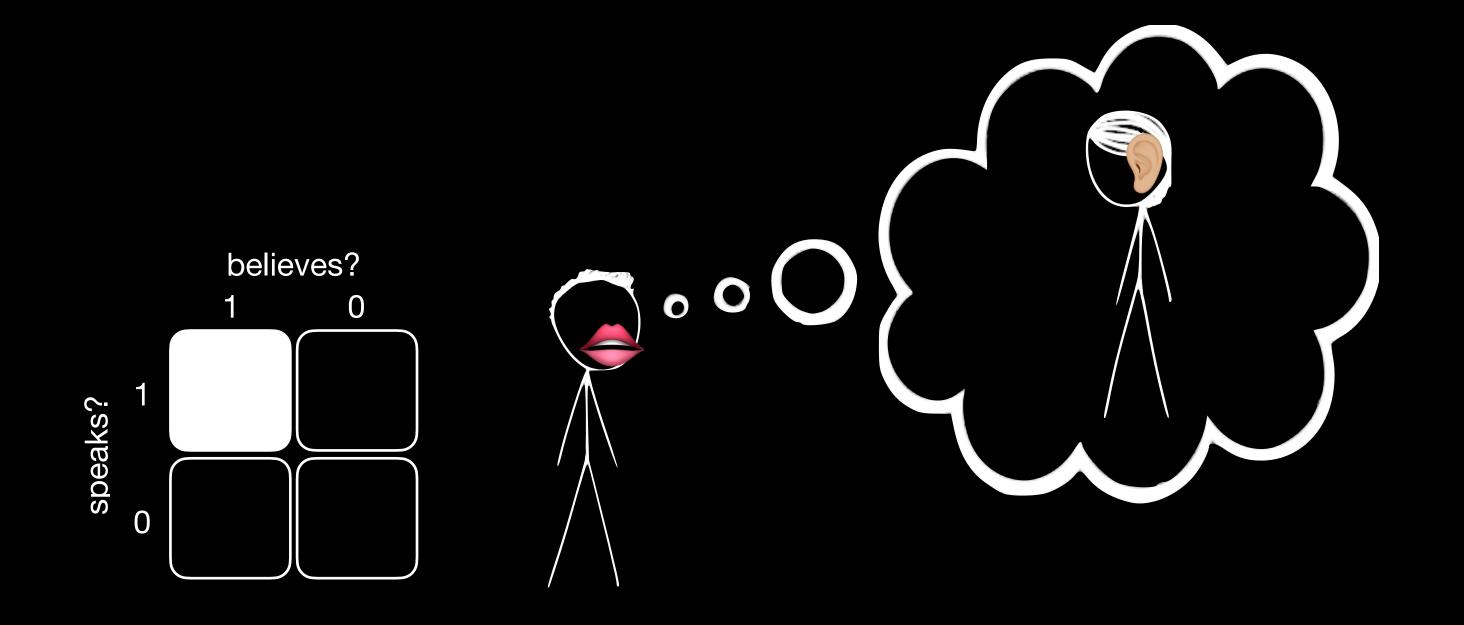
other QUDs:

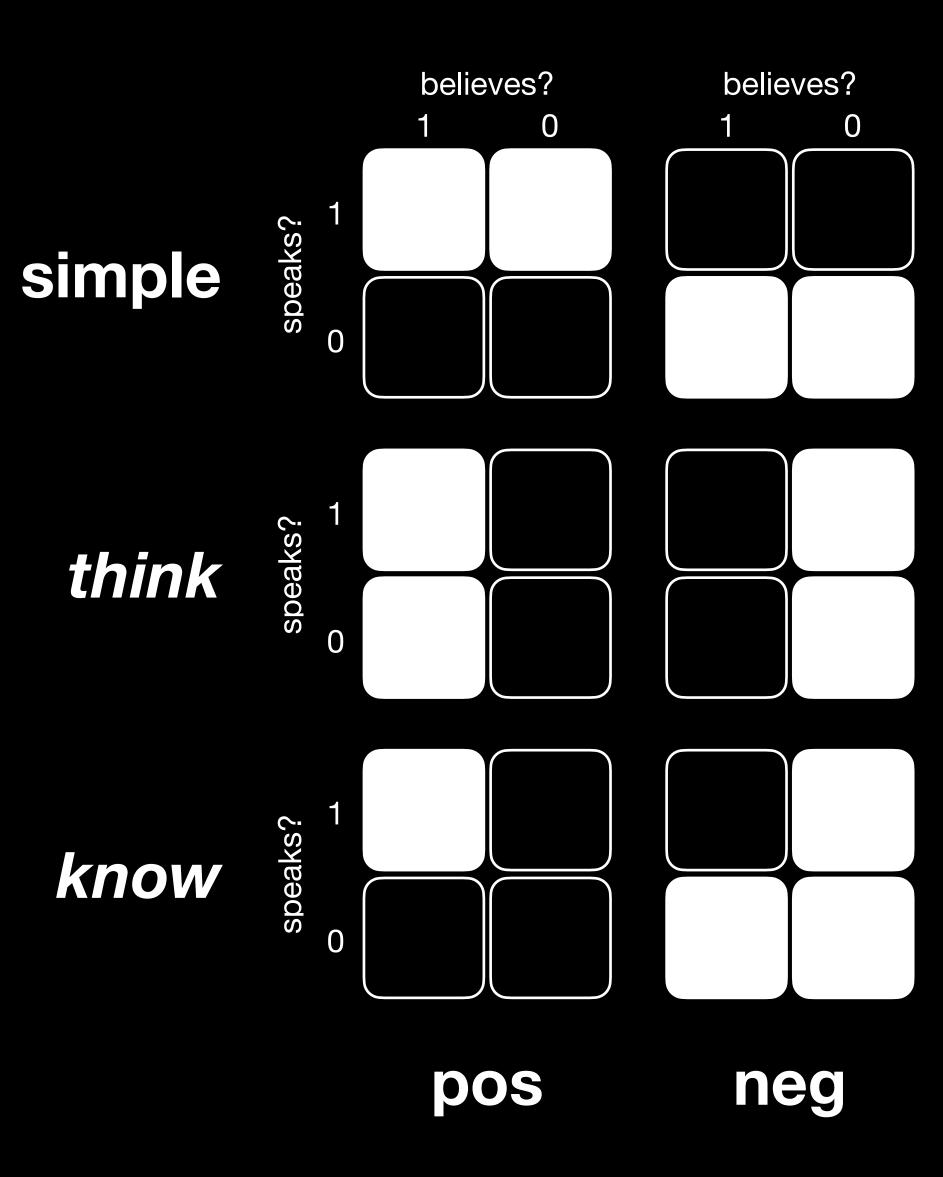
does Cole believe?

does Charley speak Spanish?

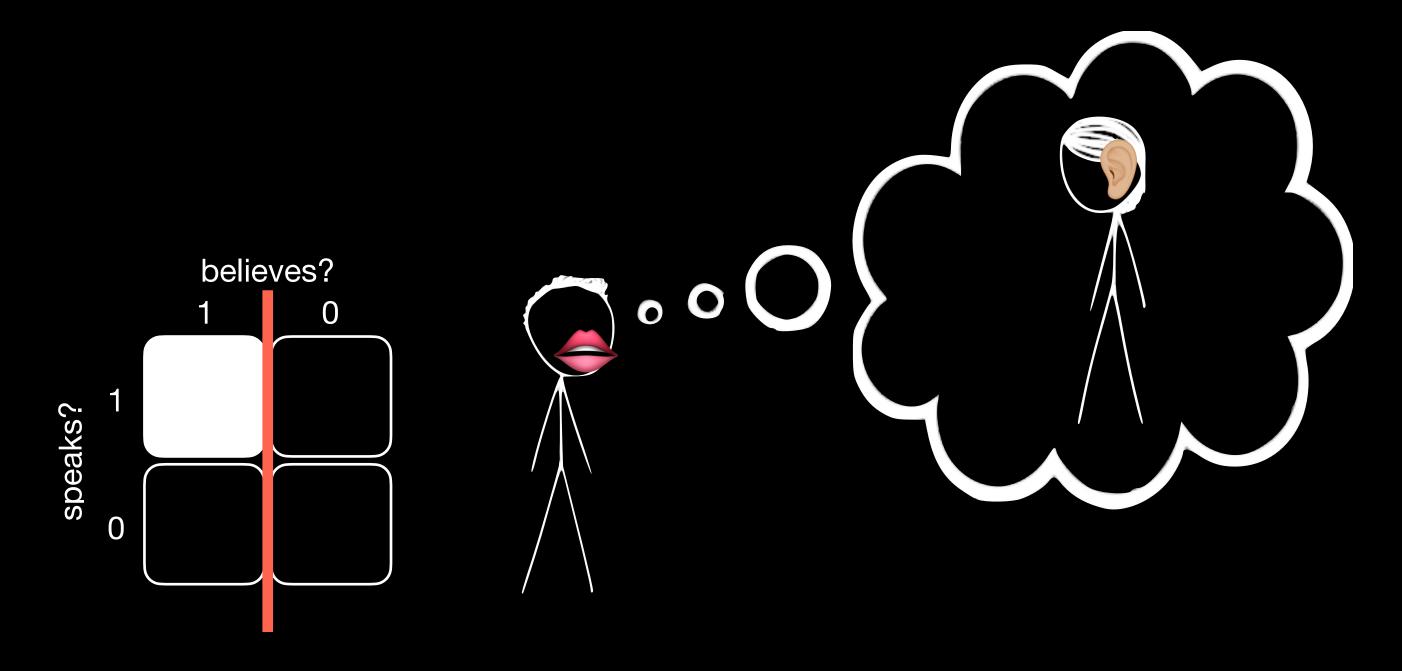


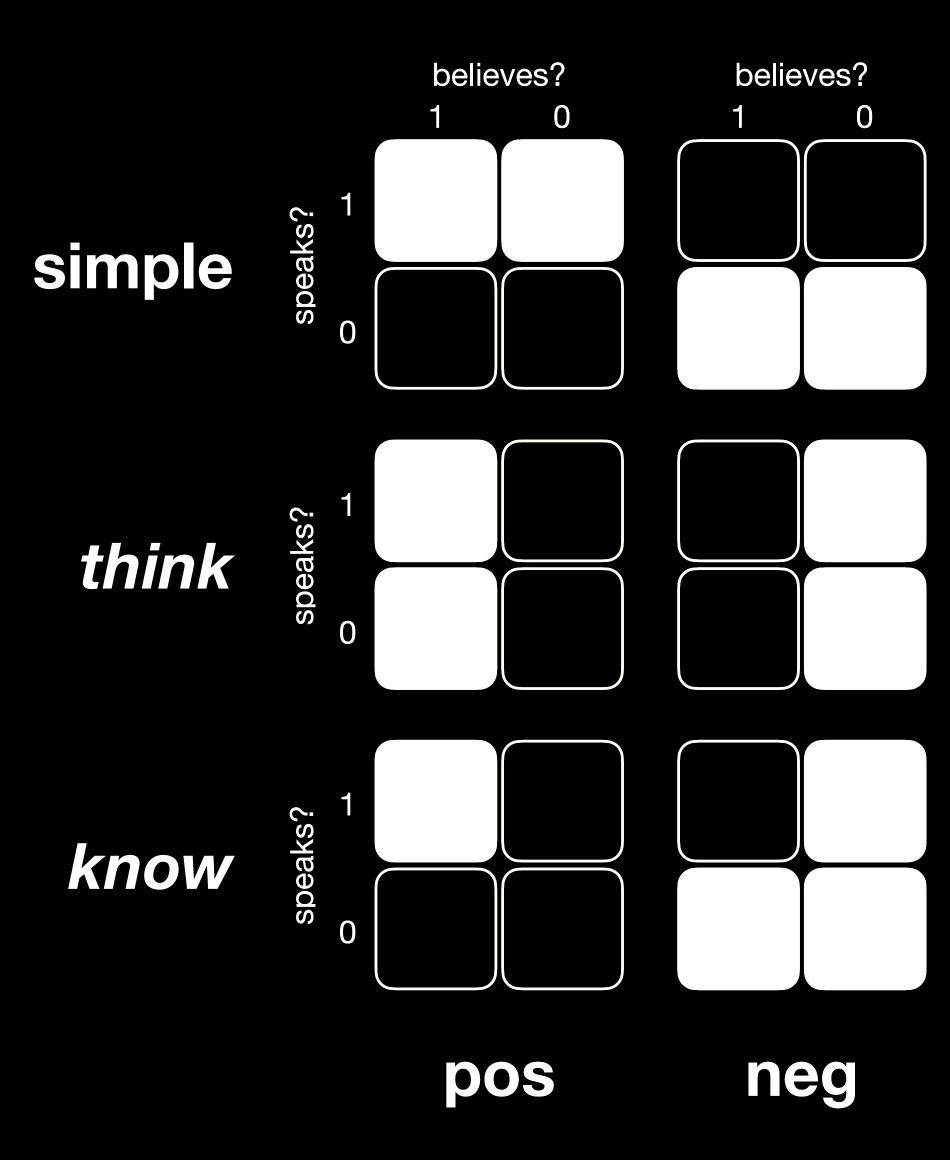
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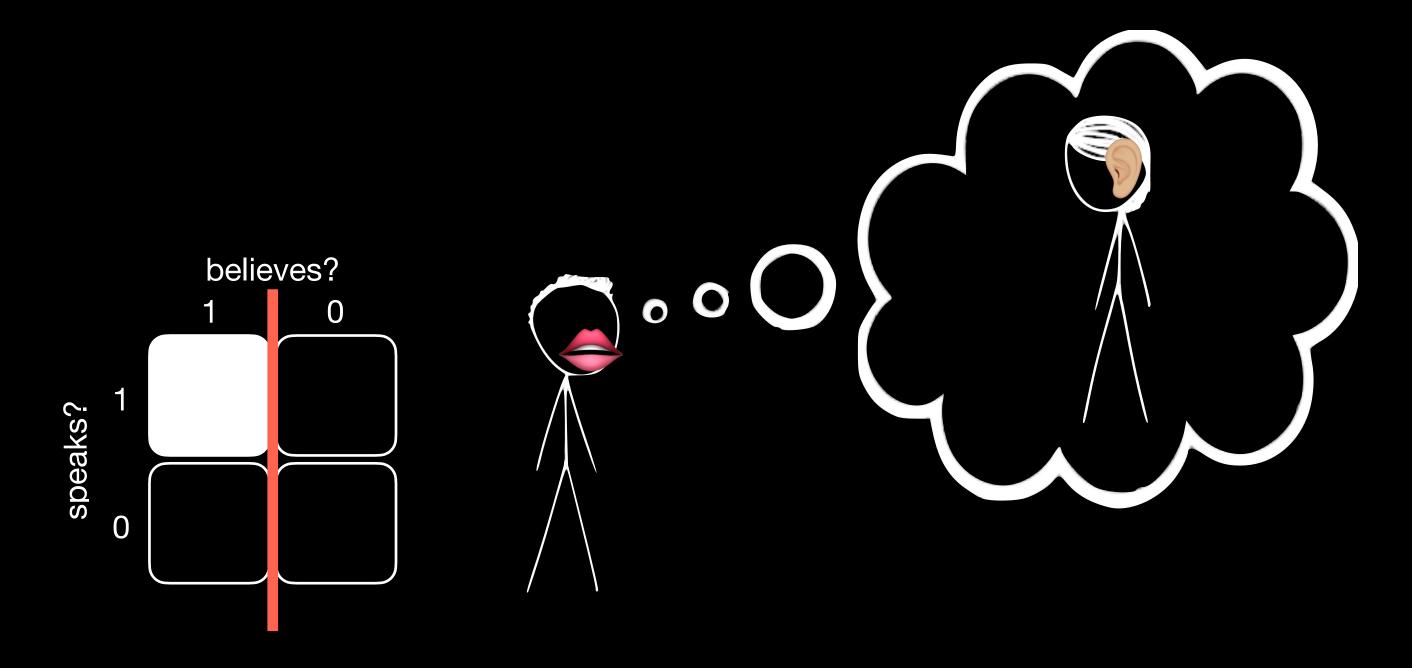


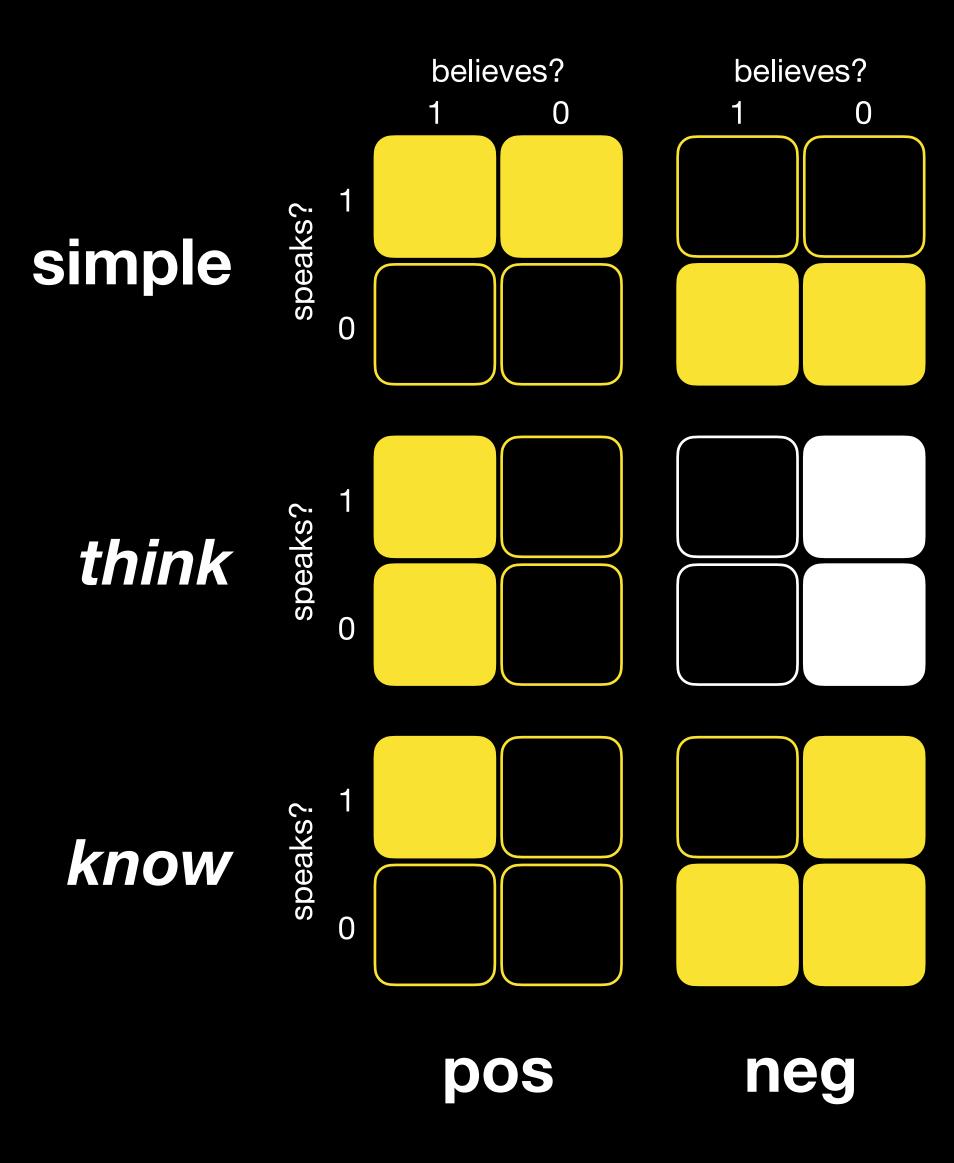
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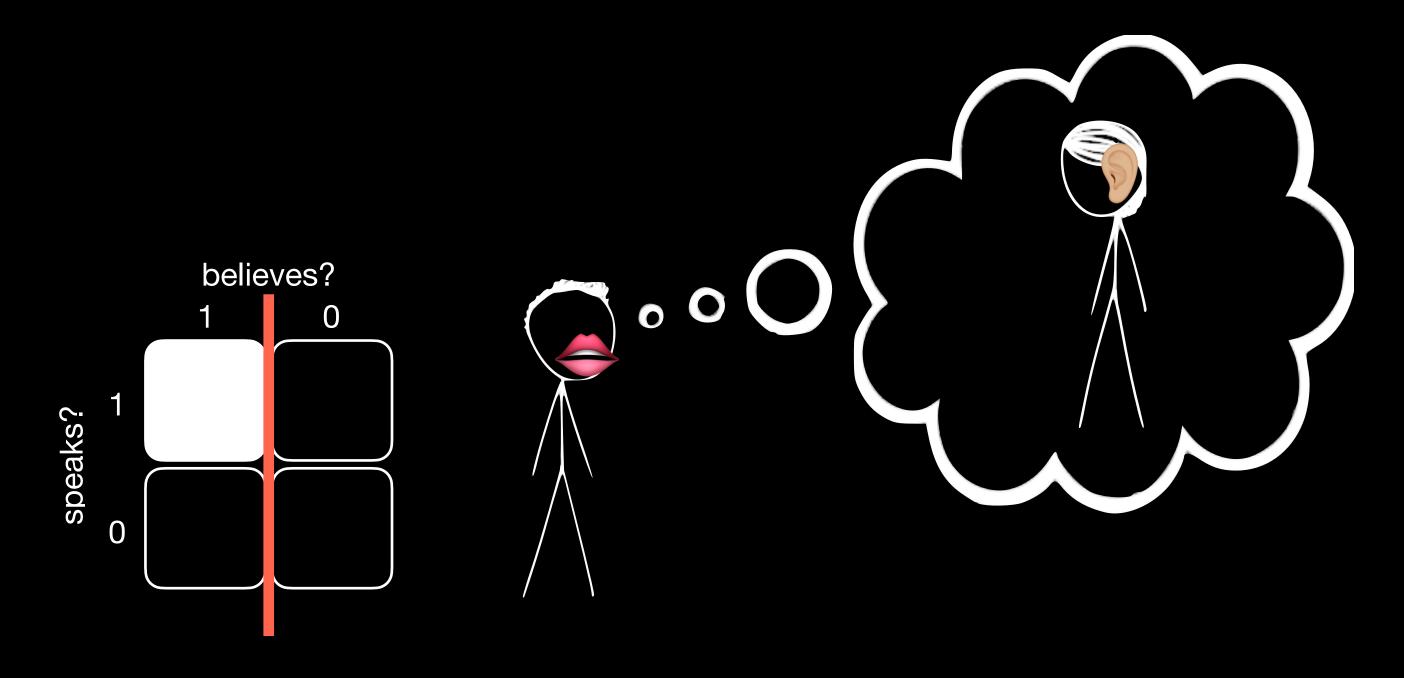


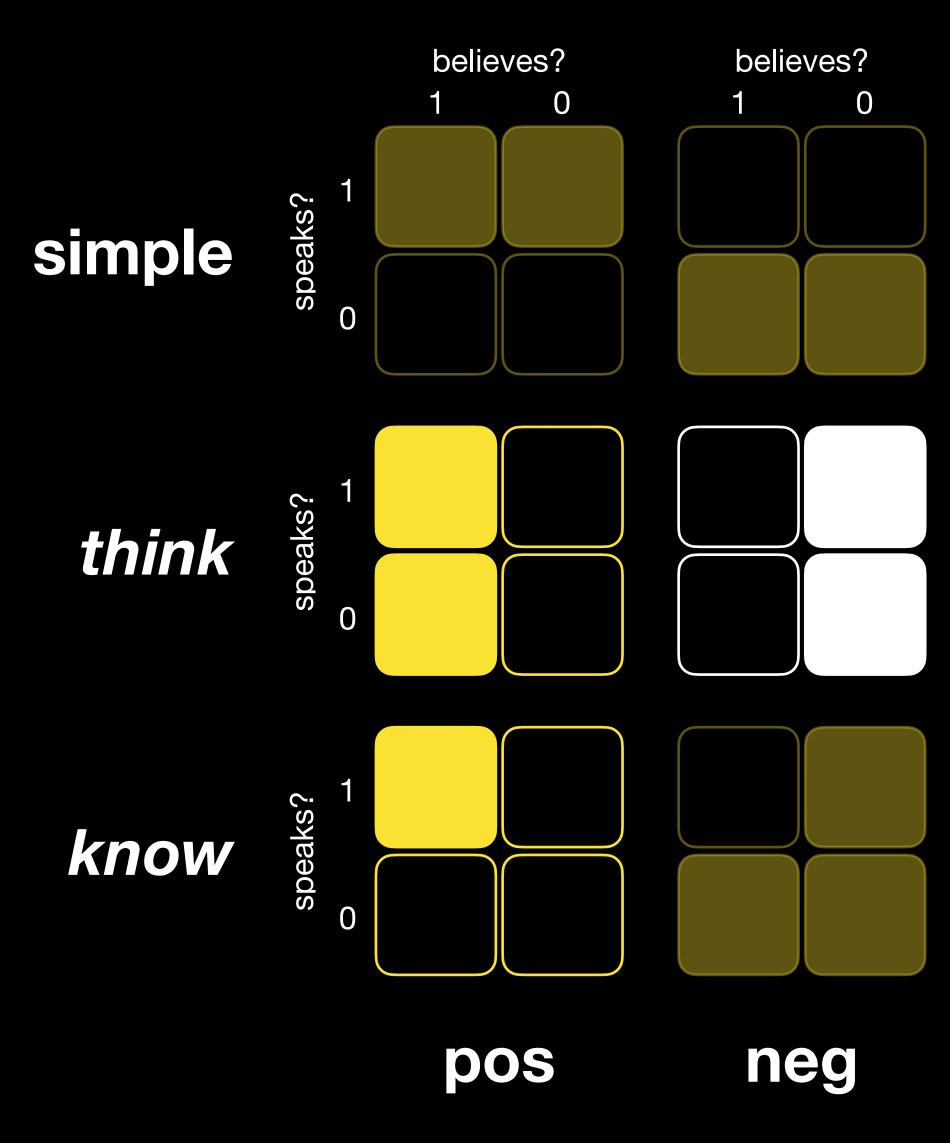
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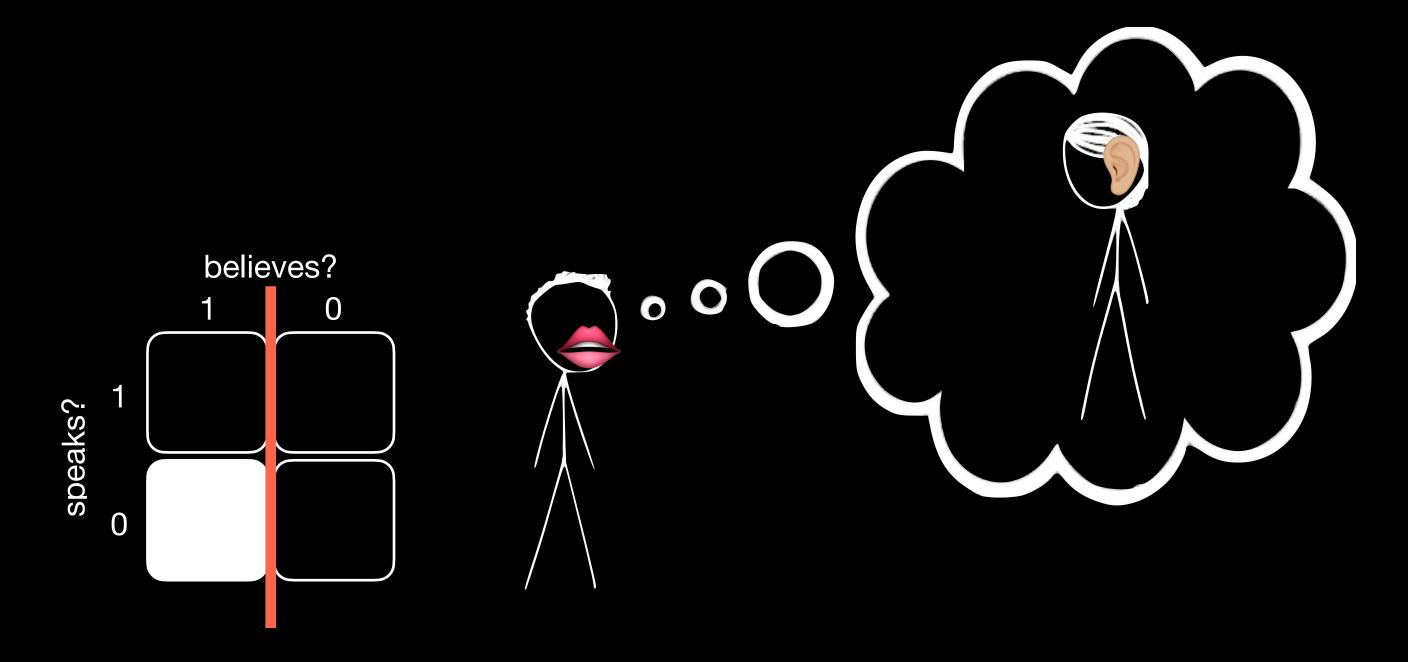


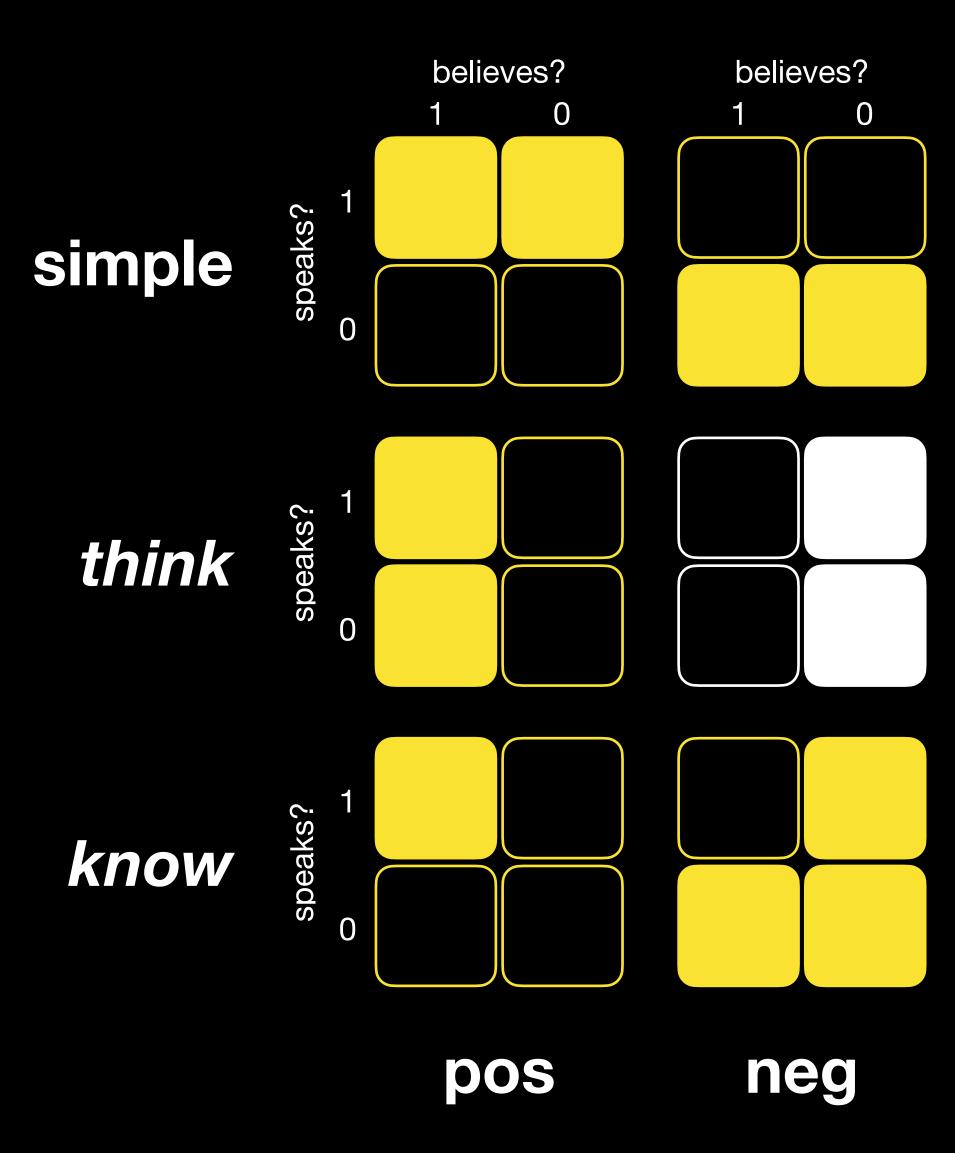
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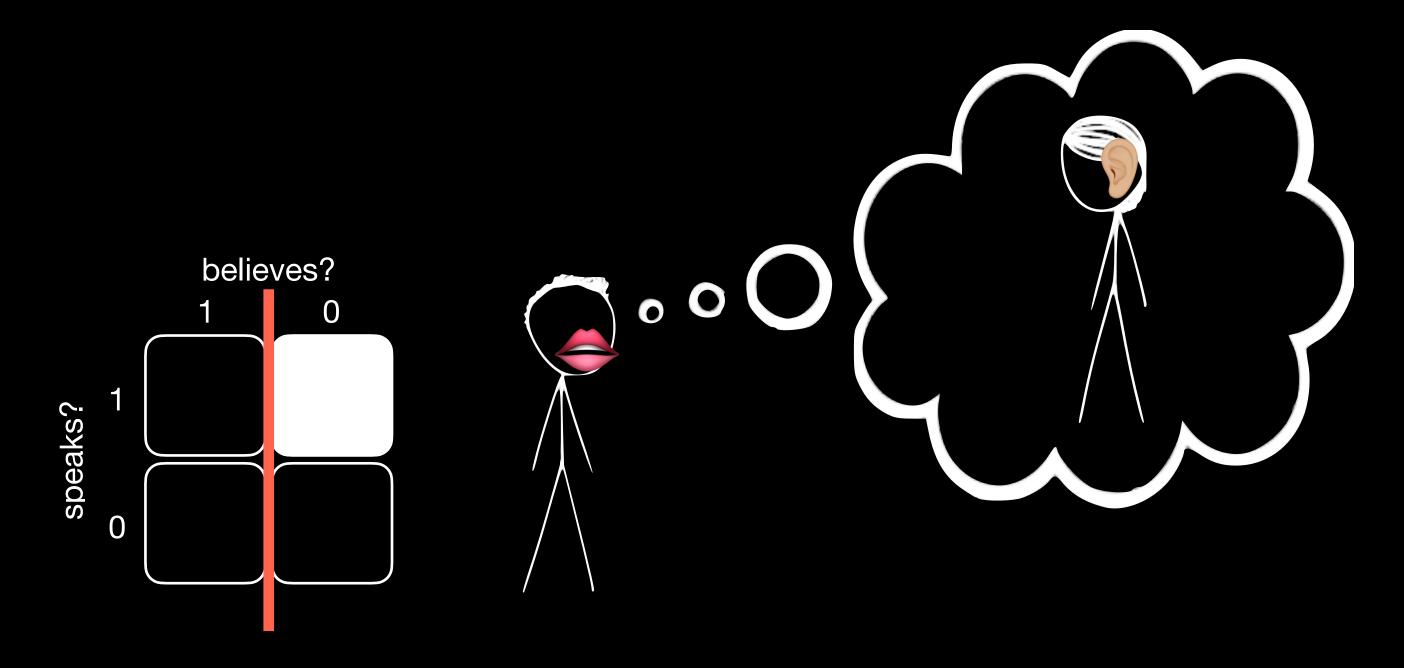


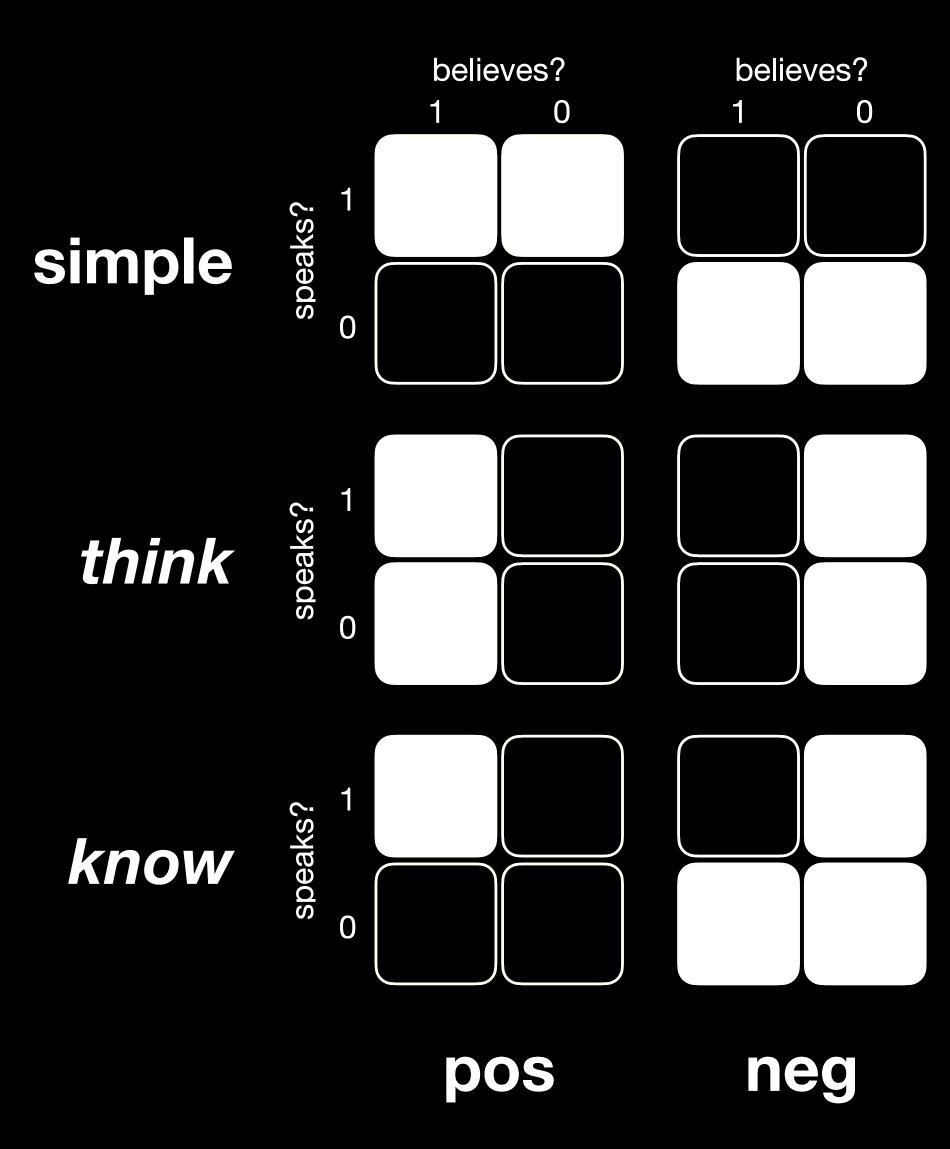
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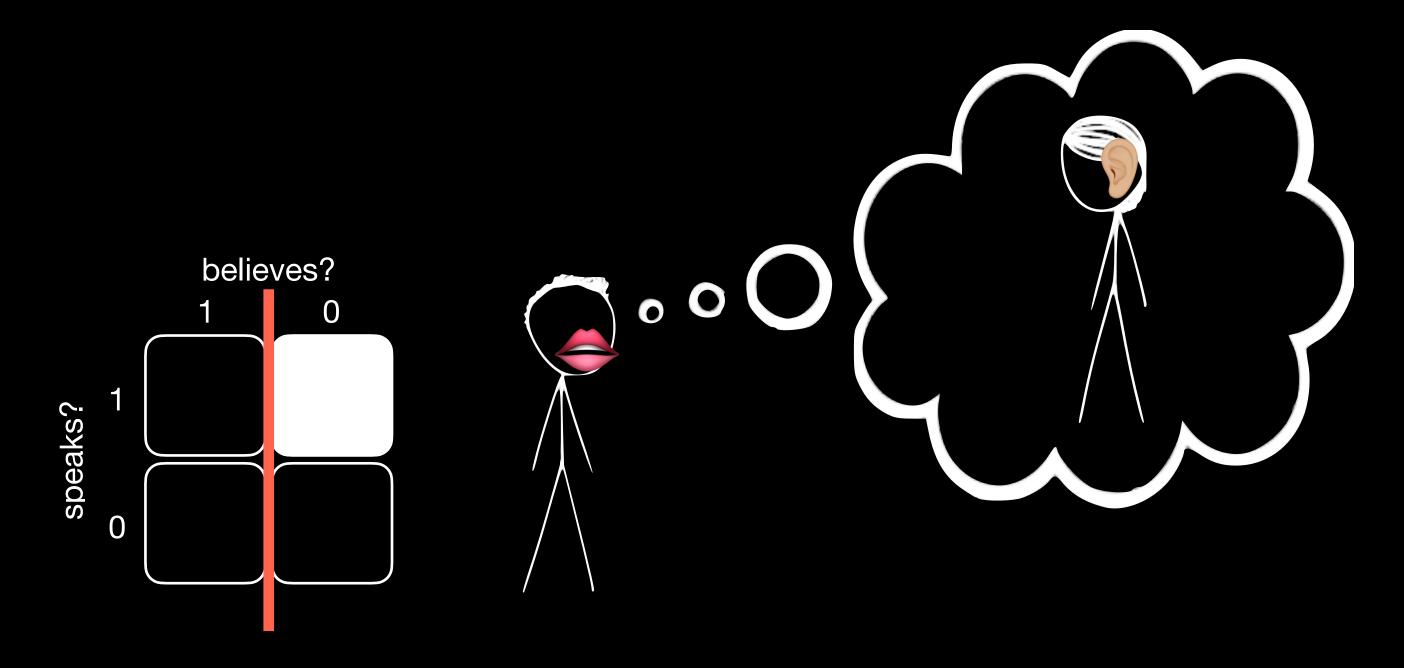


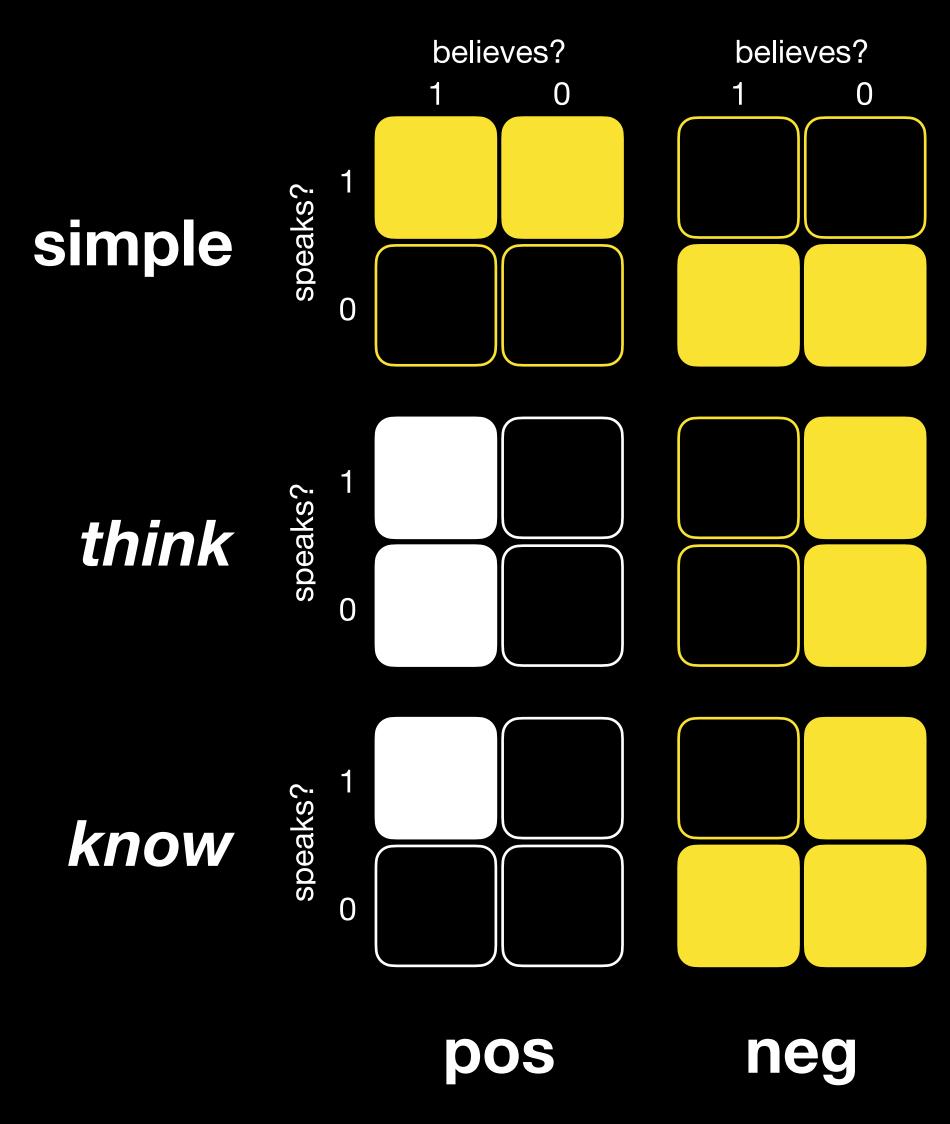
speakers **choose** to produce **utterances in proportion to their utility** for leading the **listener** to correctly
resolve the QUD



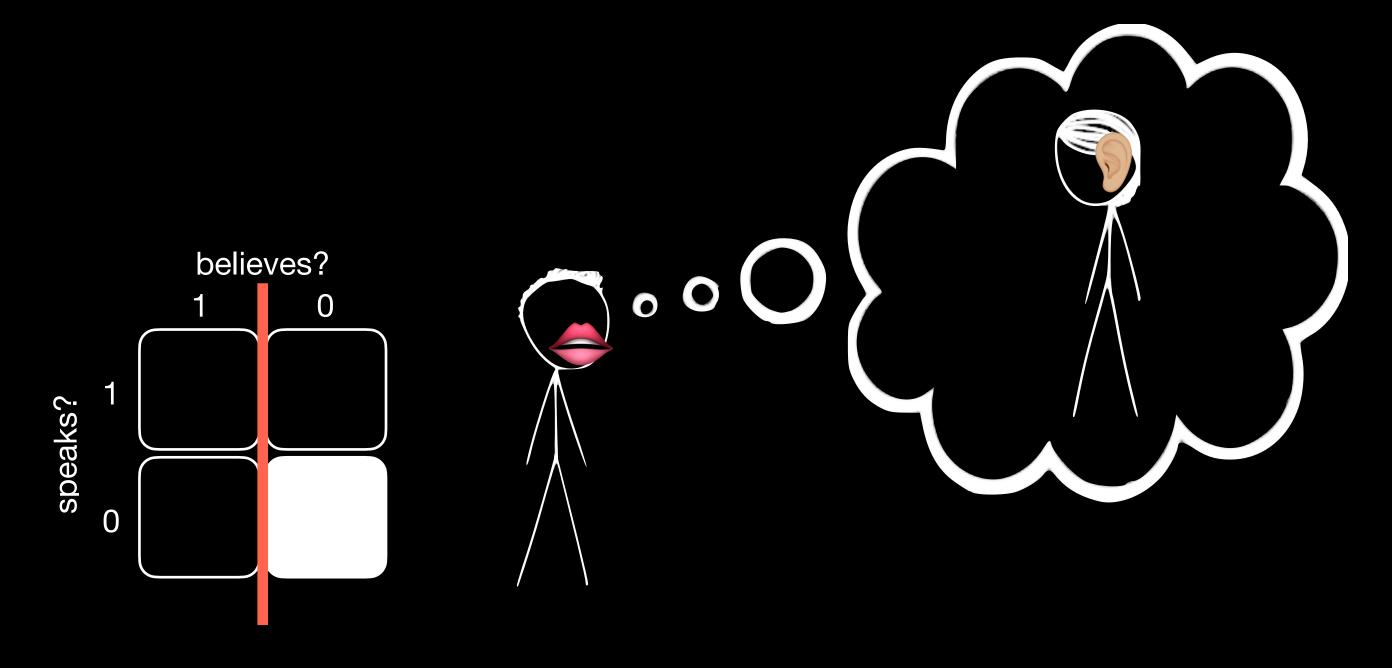


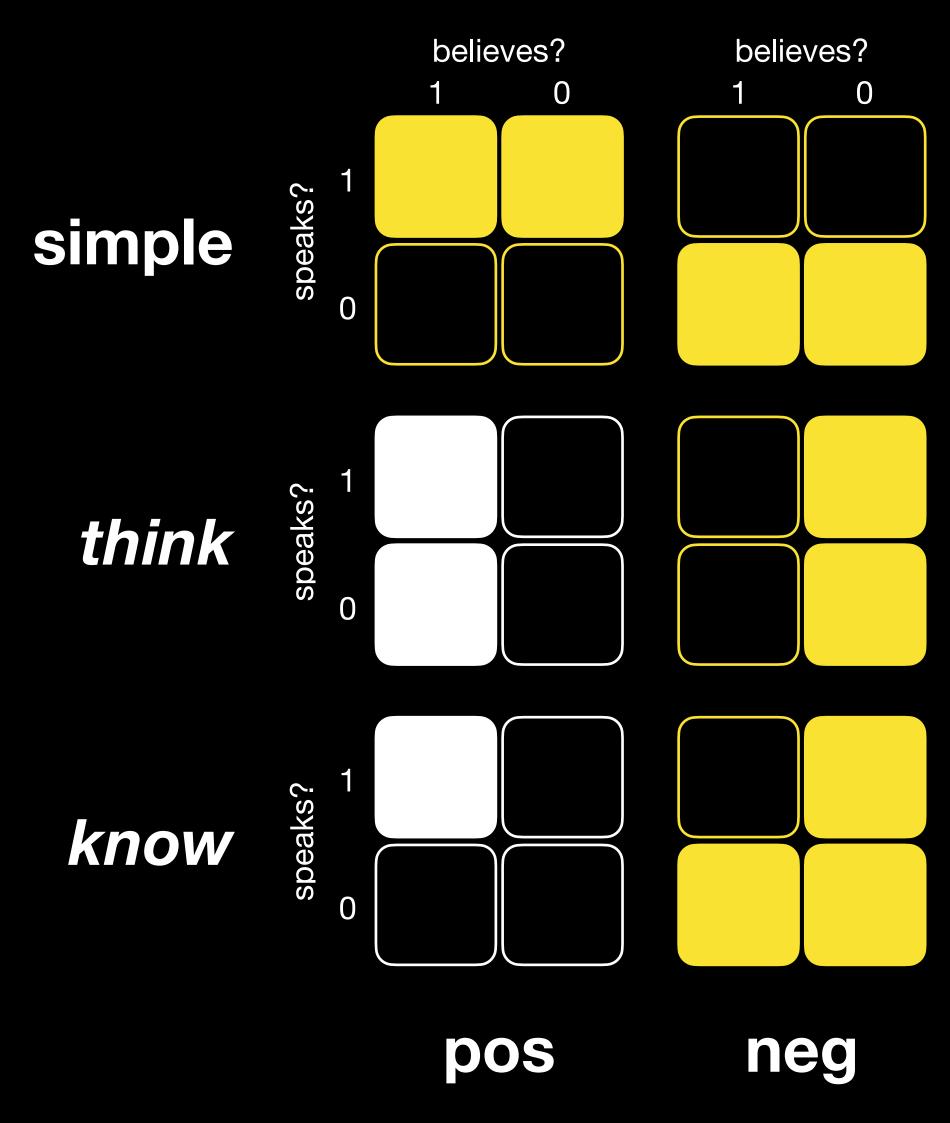
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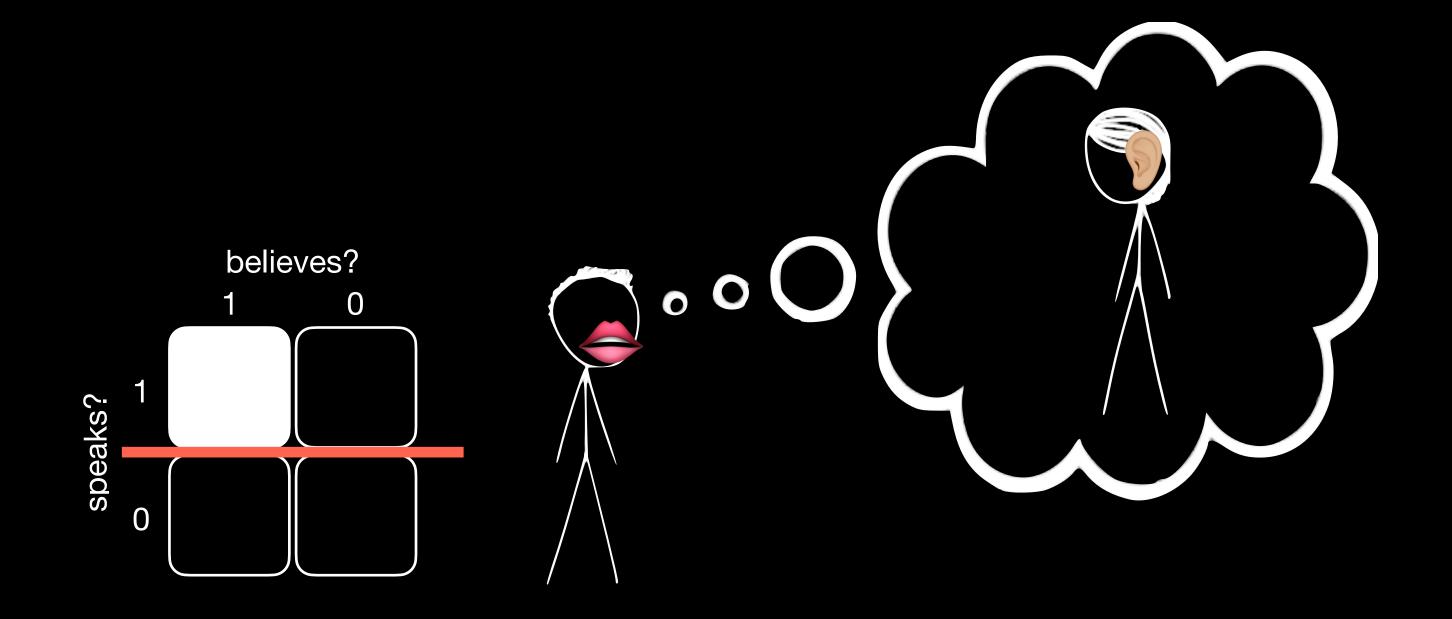


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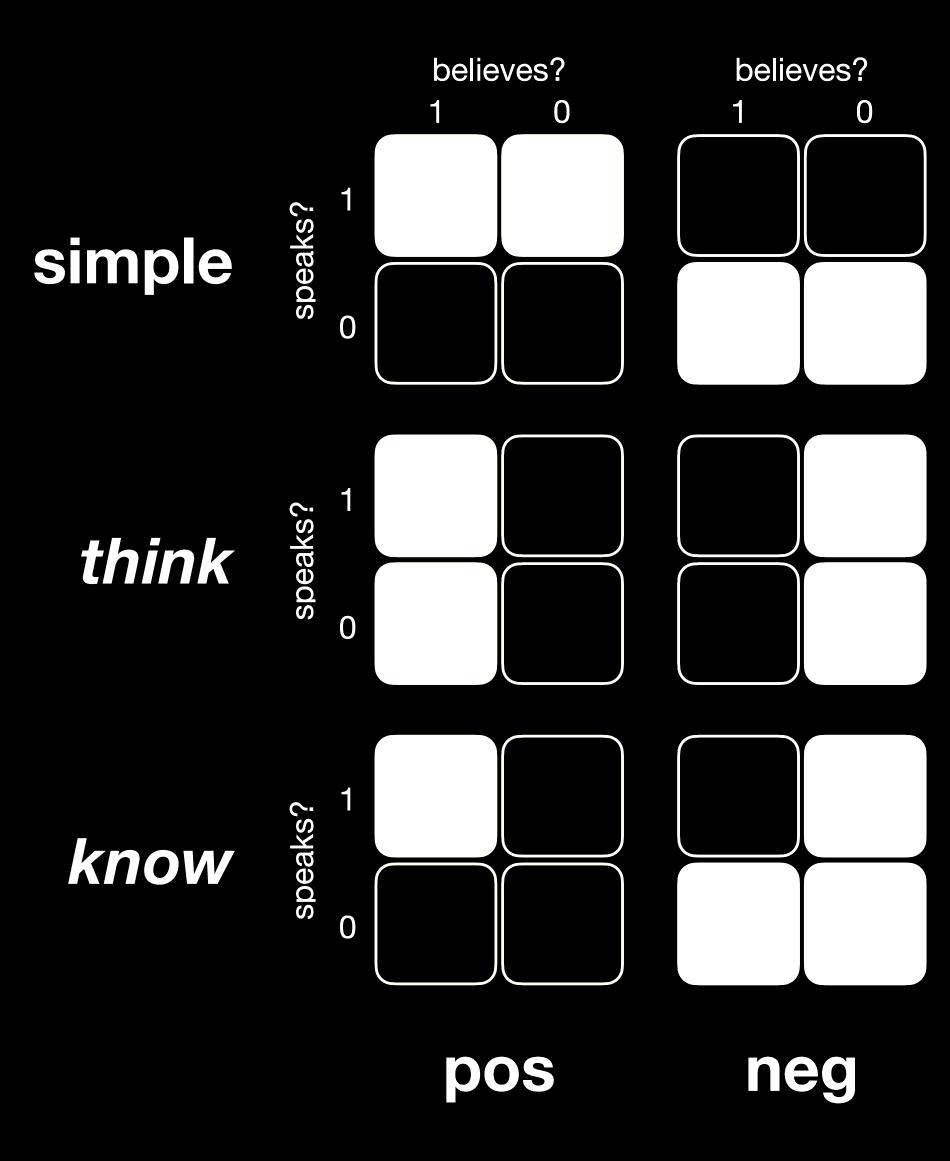




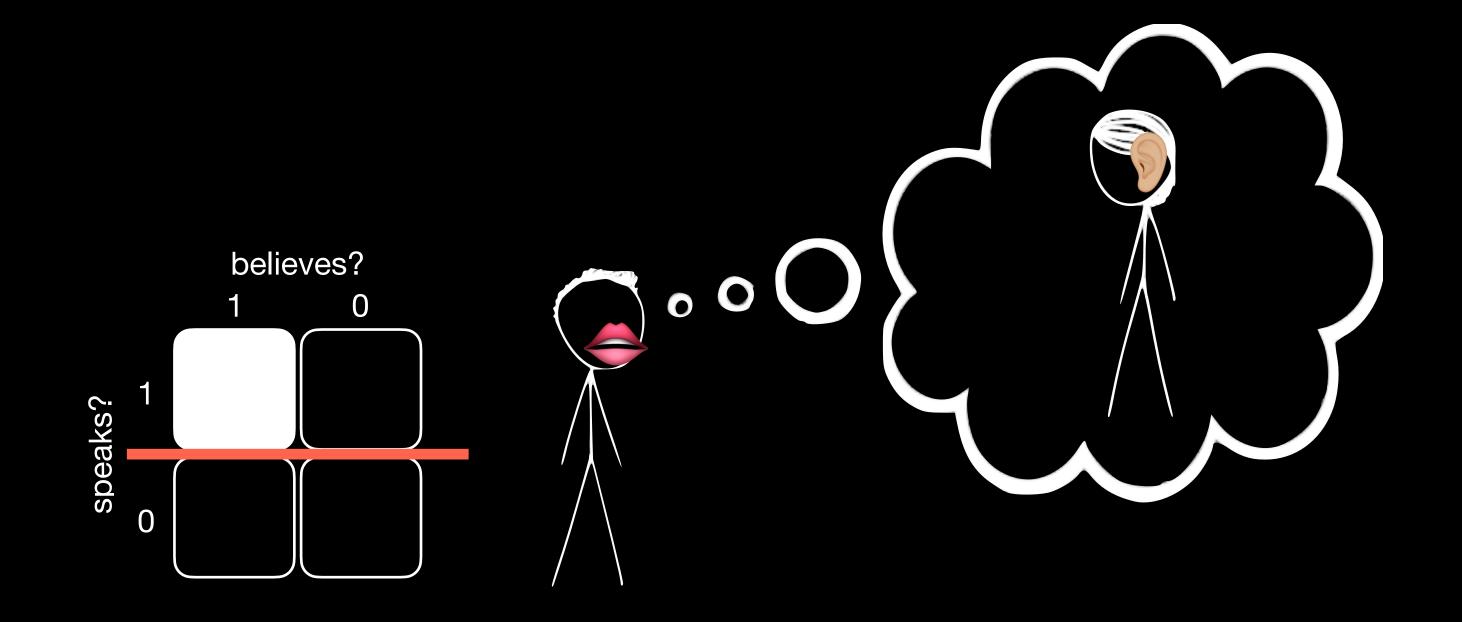
speakers **choose** to produce **utterances in proportion to their utility** for leading the **listener** to correctly resolve the QUD



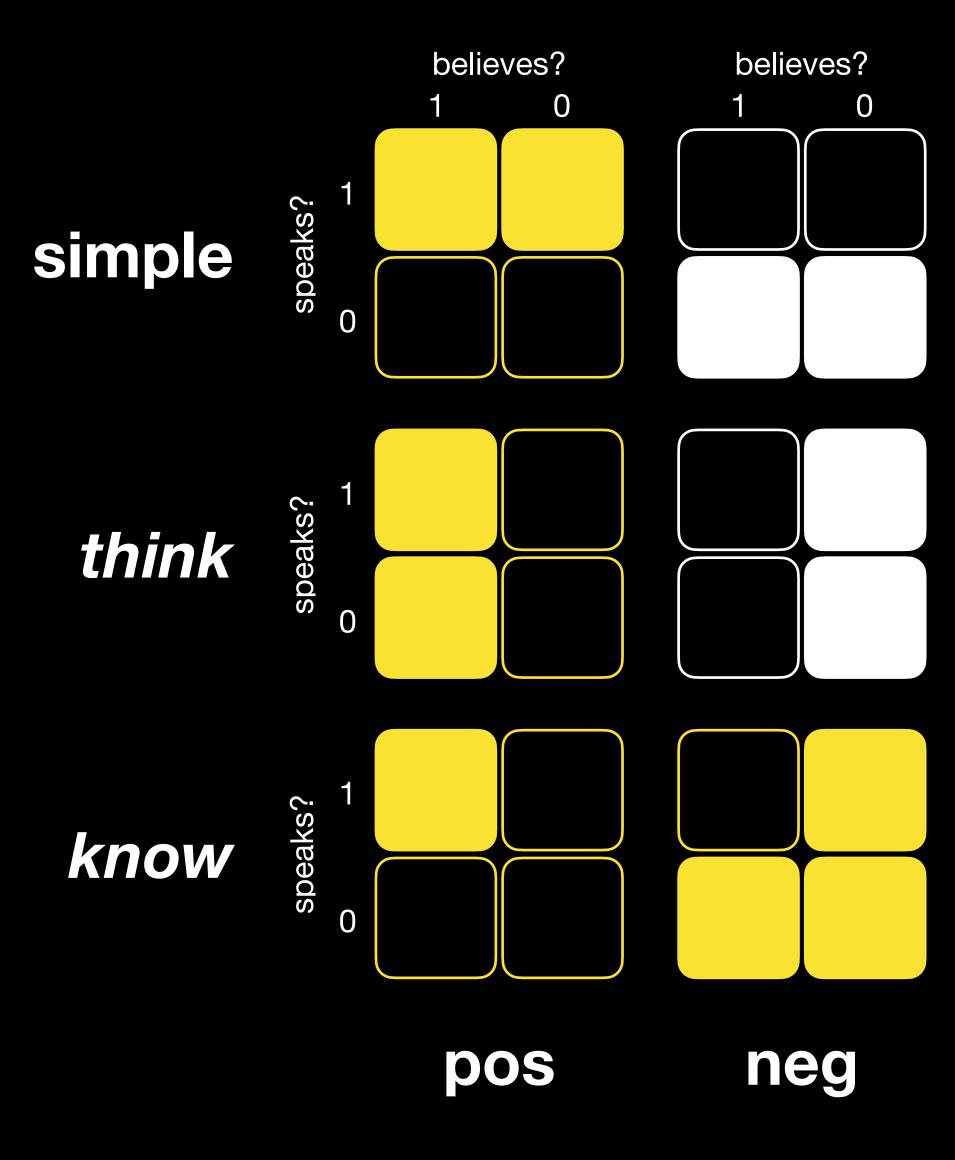
does Charley speak Spanish?



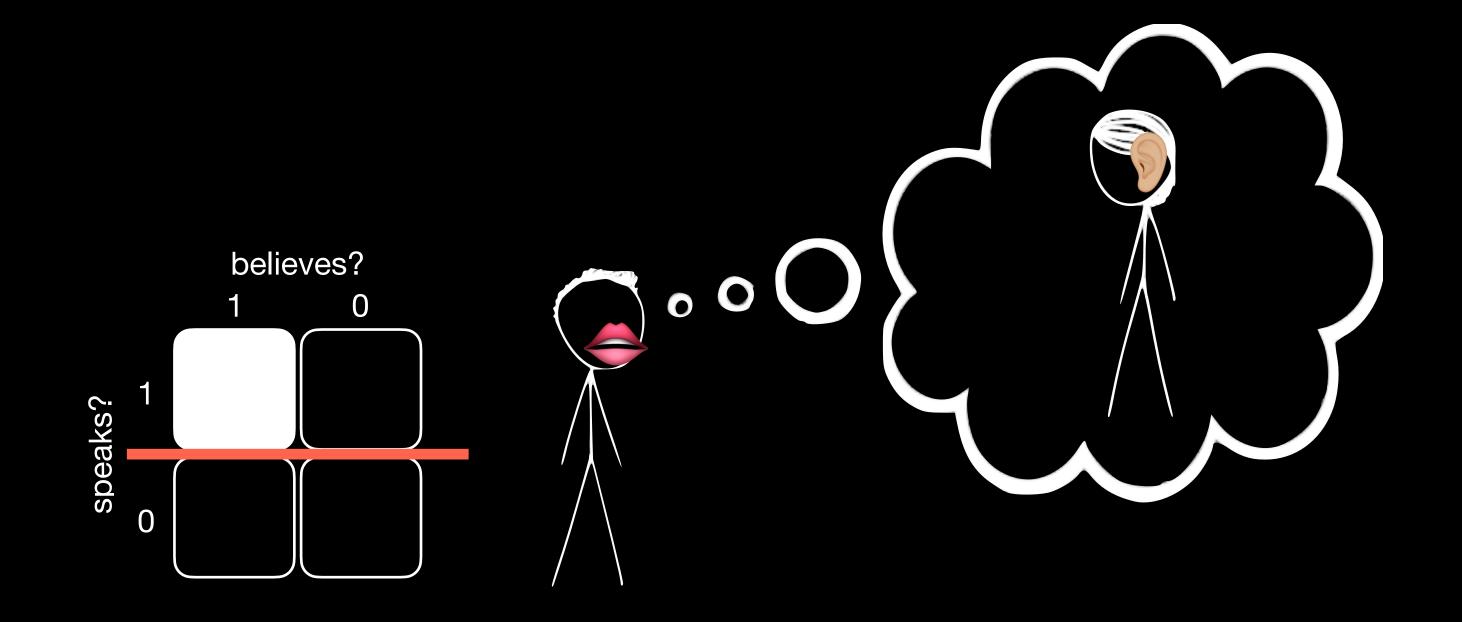
speakers **choose** to produce **utterances in proportion to their utility** for leading the **listener** to correctly resolve the QUD



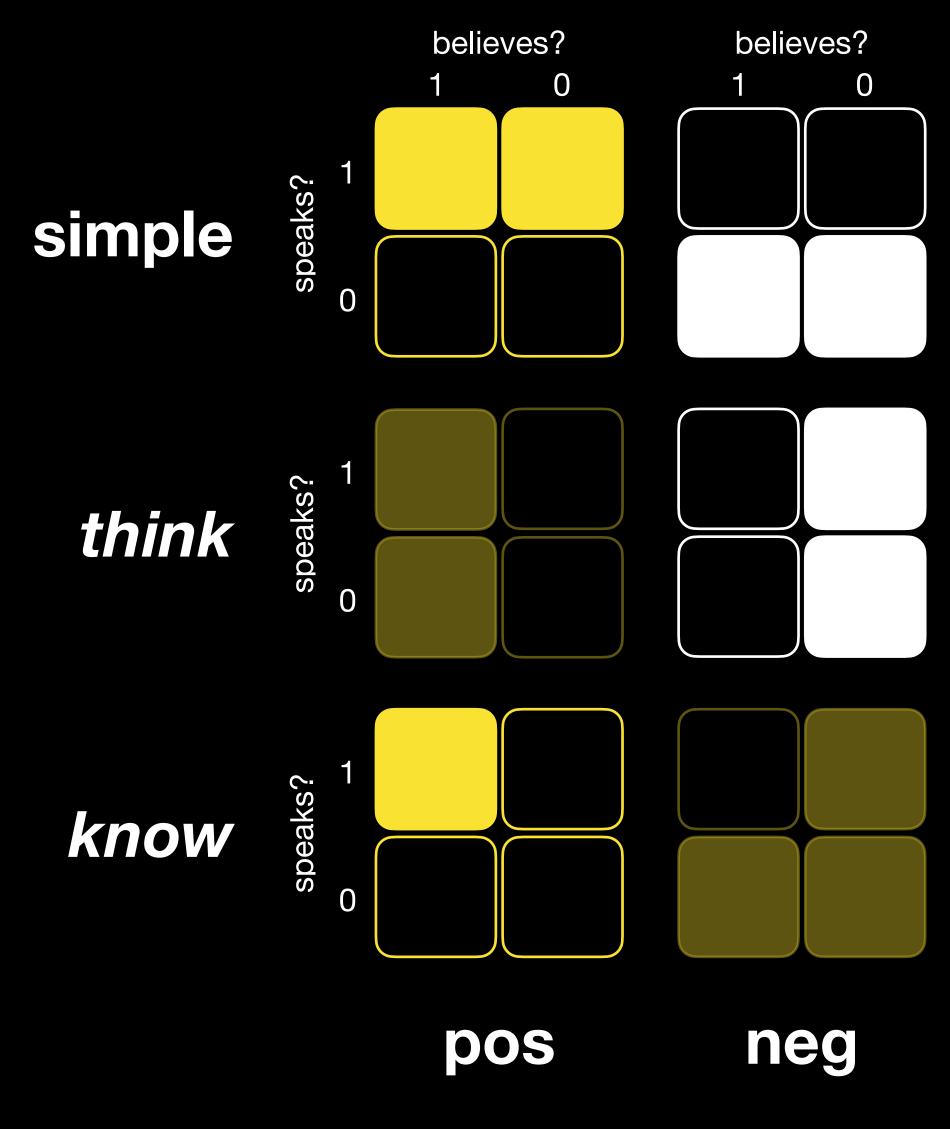
does Charley speak
Spanish?



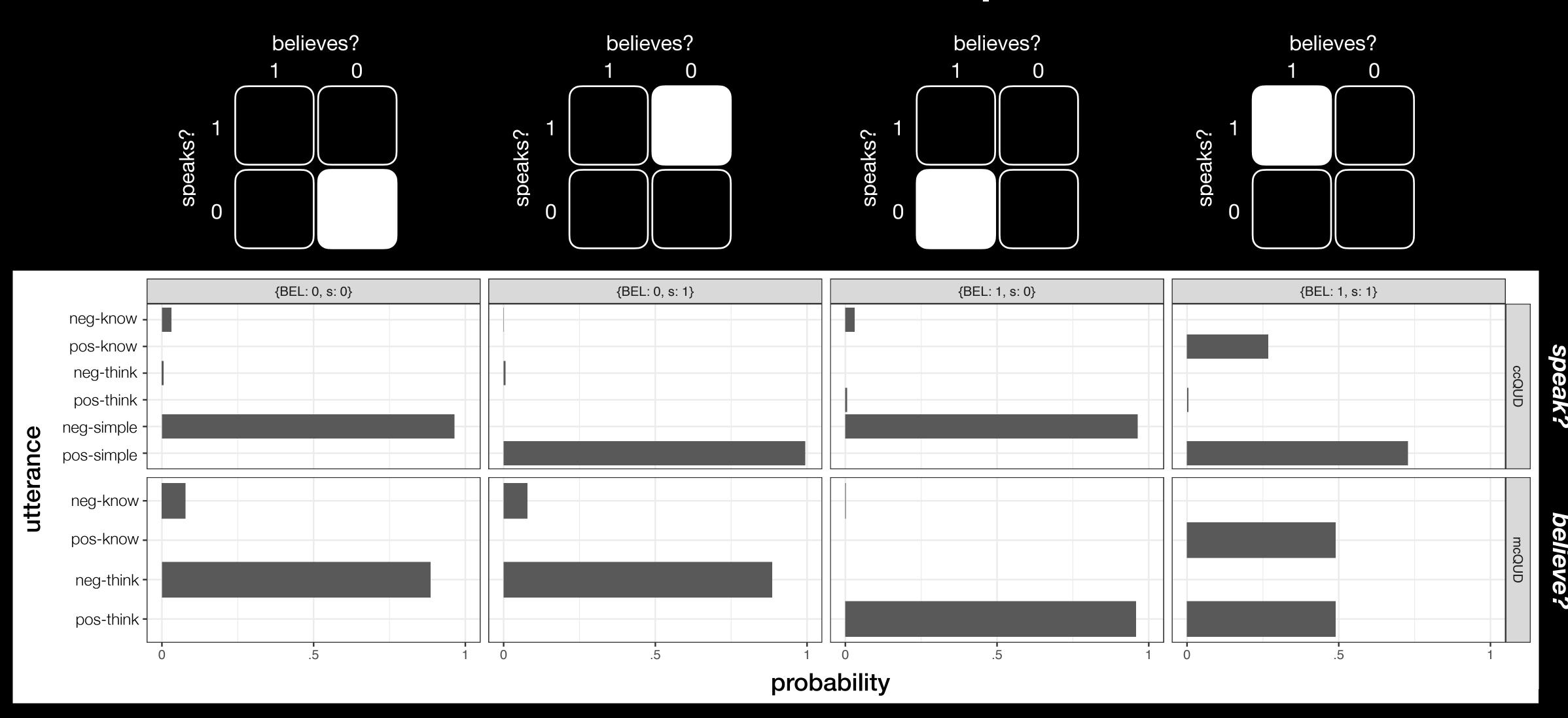
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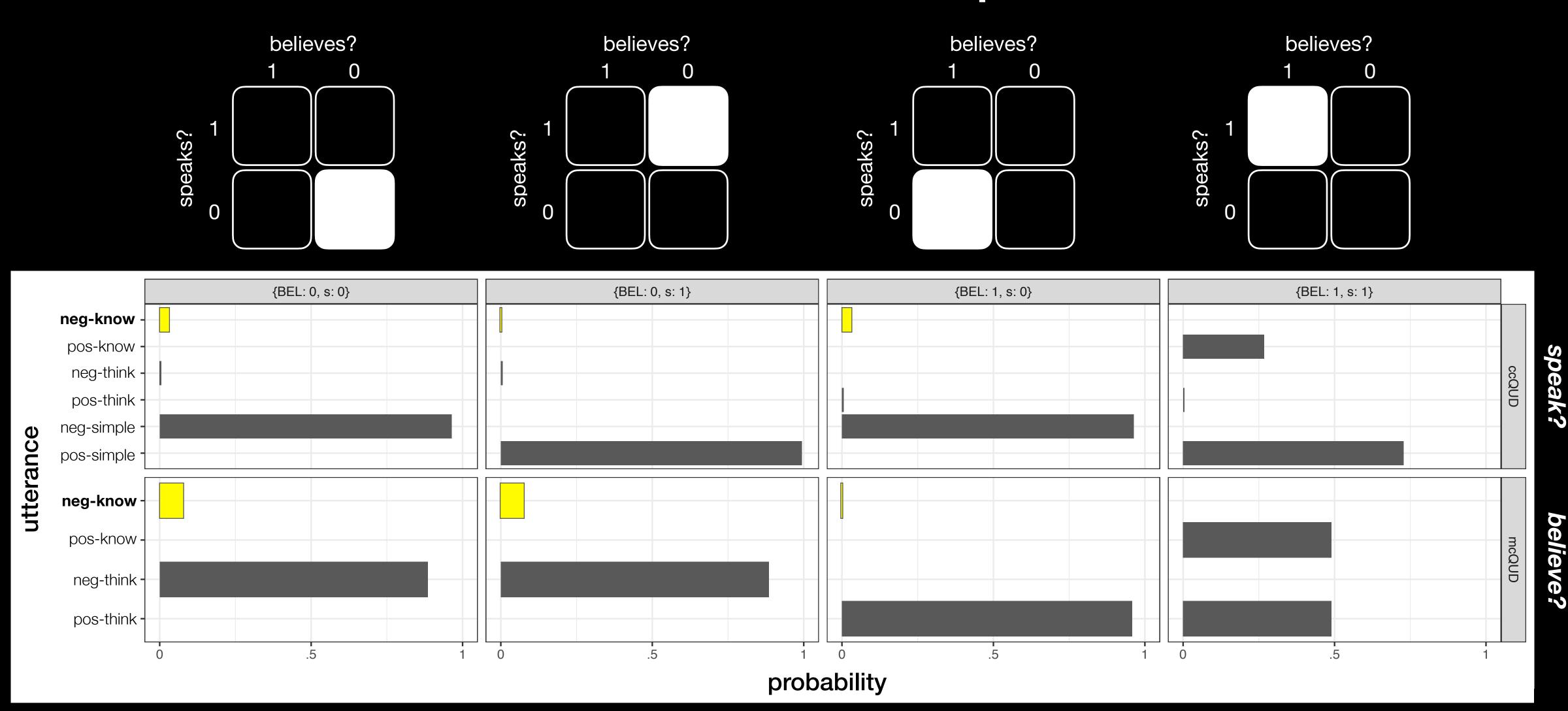
does Charley speak
Spanish?



# which utterance does the speaker choose?



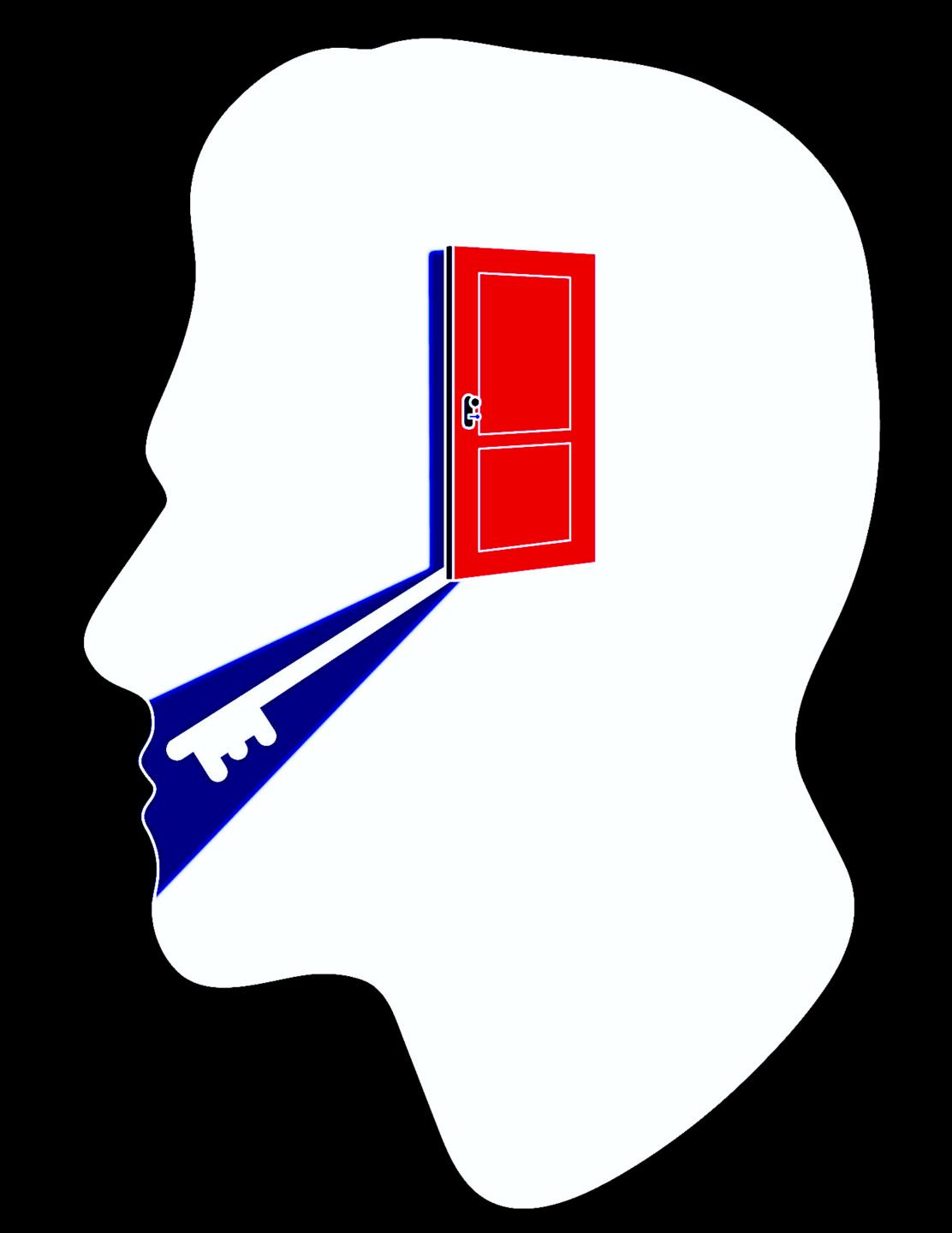
# which utterance does the speaker choose?



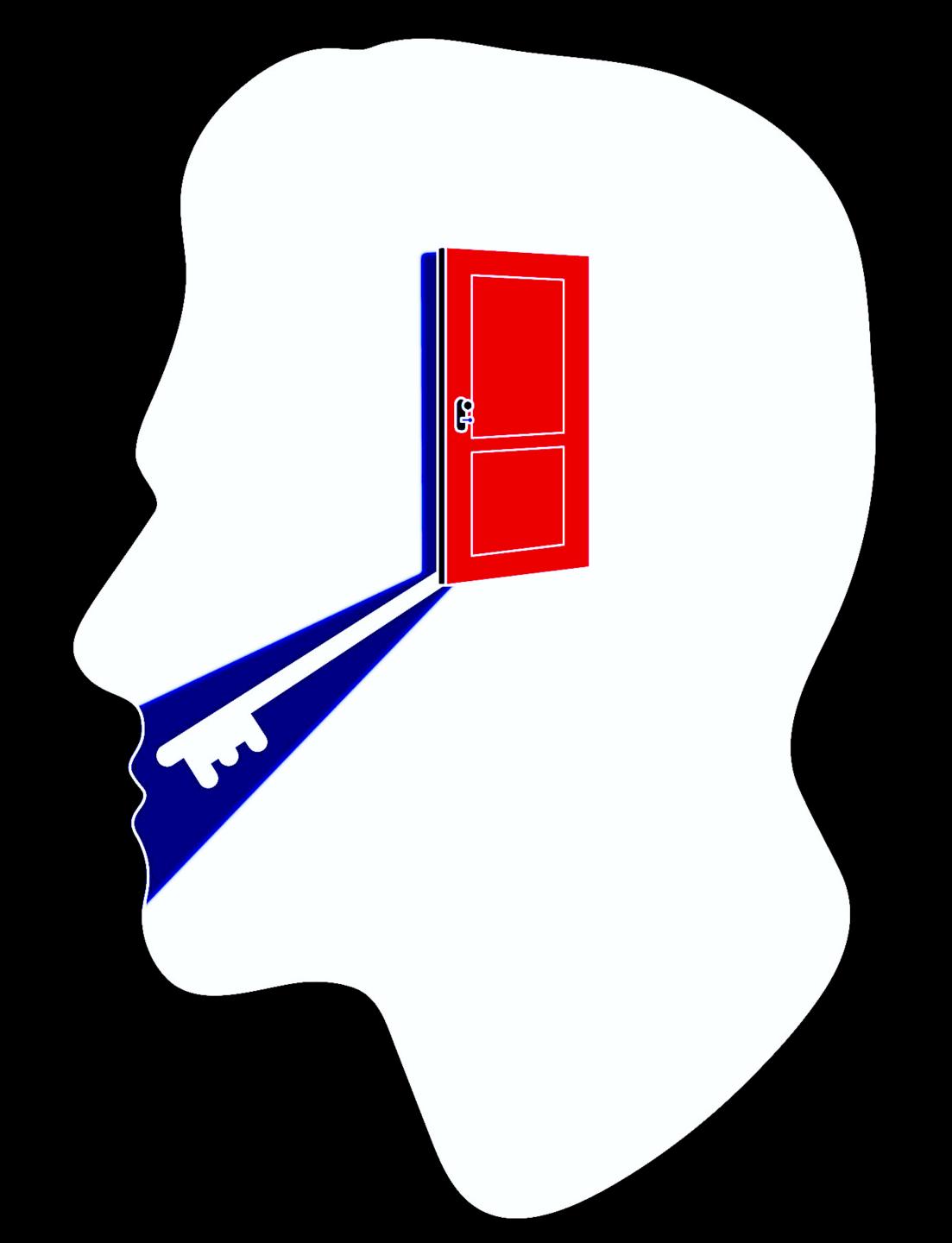
neg-know has low utility because it has a weak semantics

One more thing...

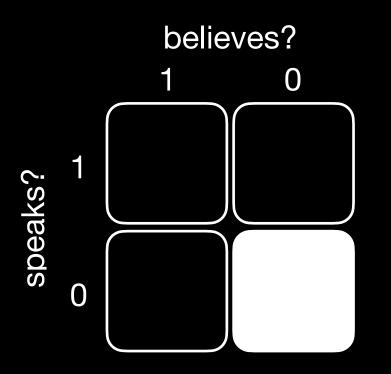
private assumptions

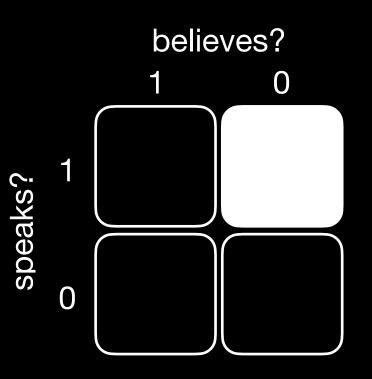


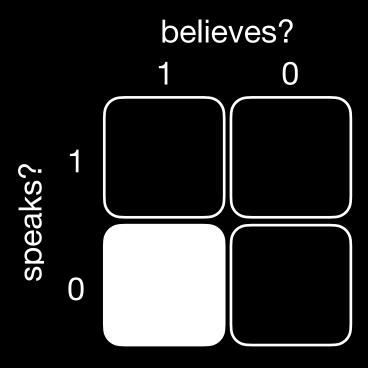
the speaker wants to convey an answer to the QUD that is consistent with their private assumptions

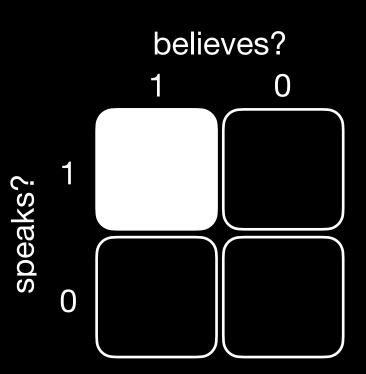


#### private assumptions: what the speaker assumes to be true

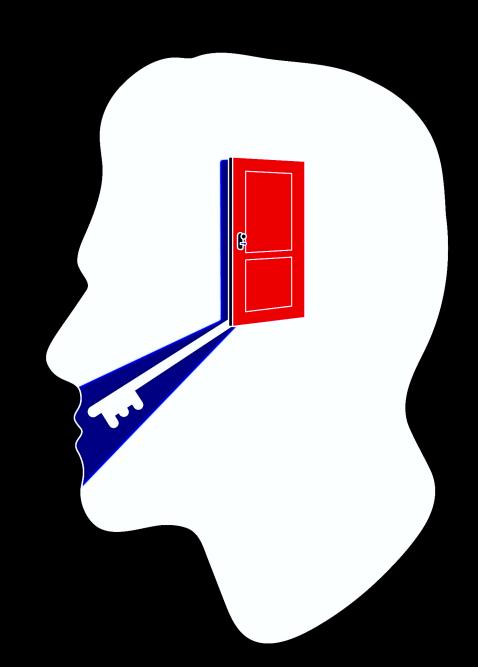




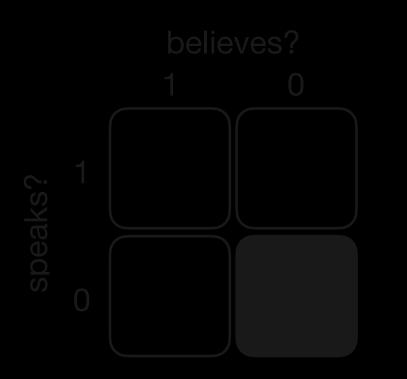


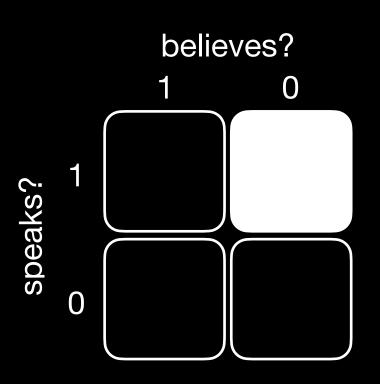


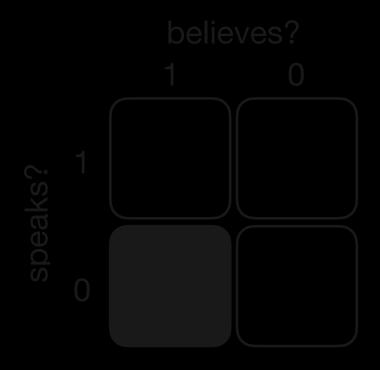
no assumptions; all worlds are possible

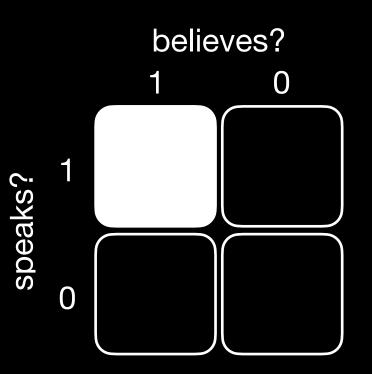


#### private assumptions: what the speaker assumes to be true

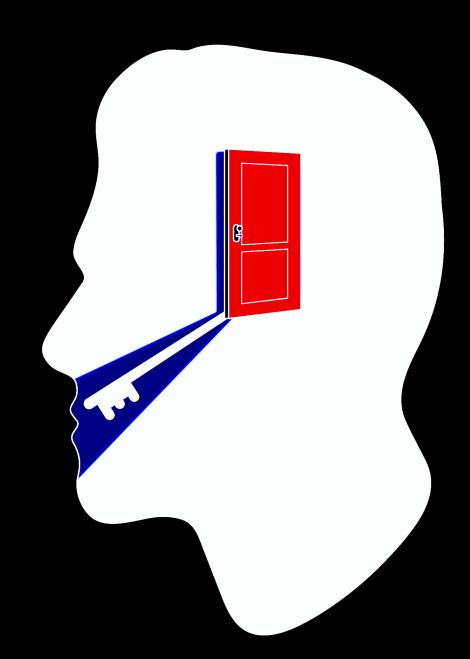




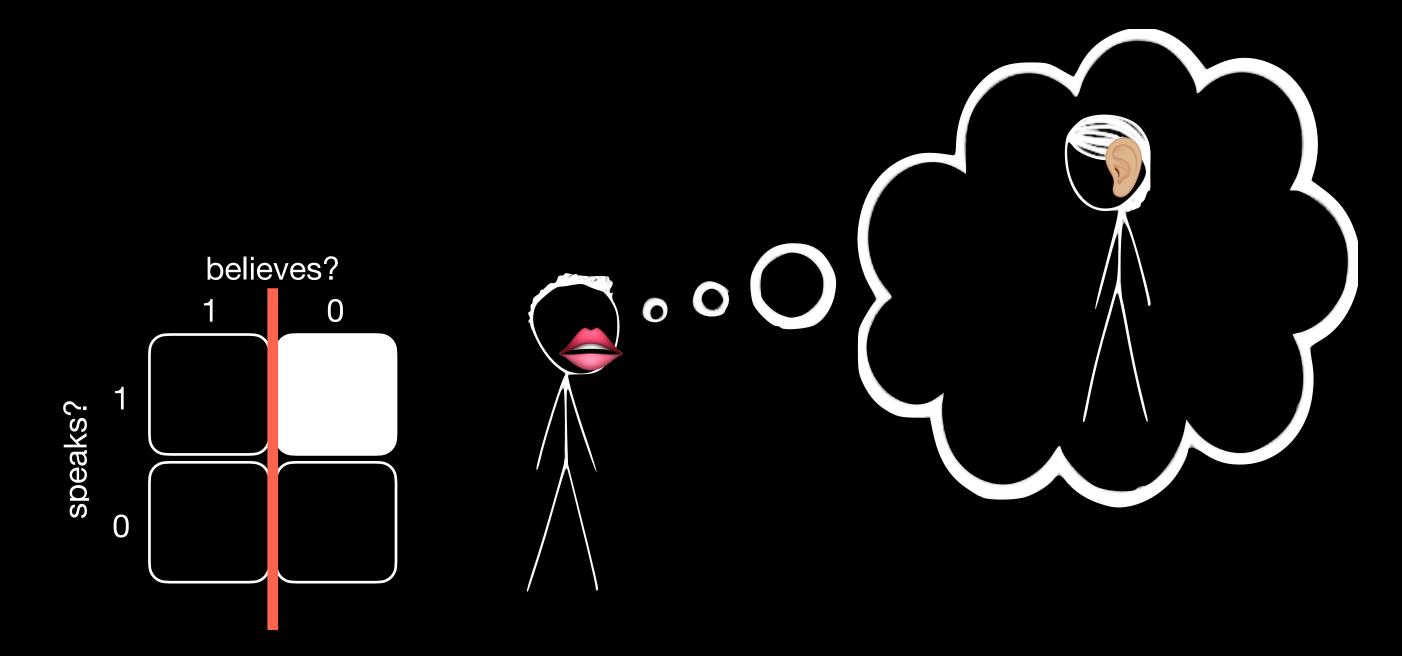


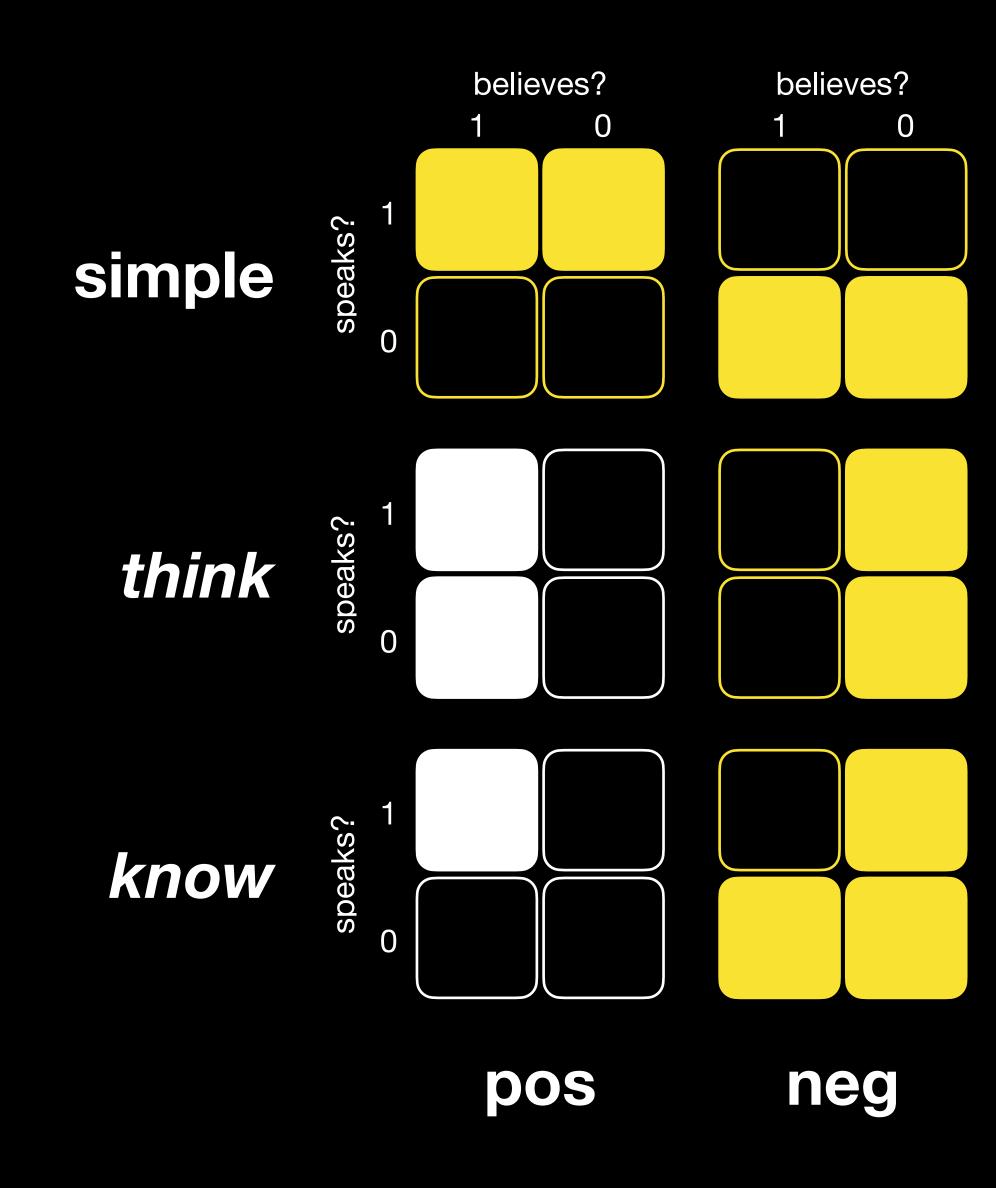


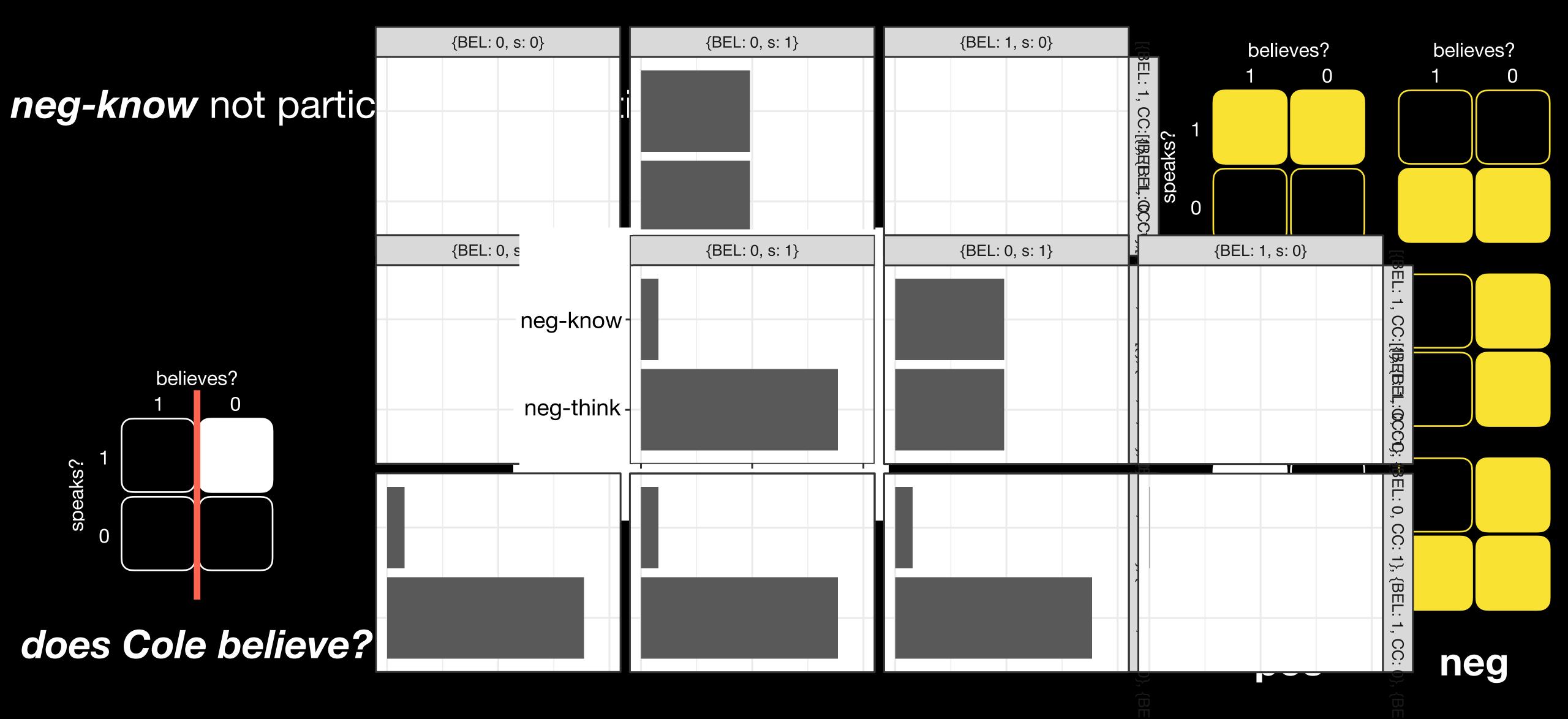
assumption that Charley speaks Spanish

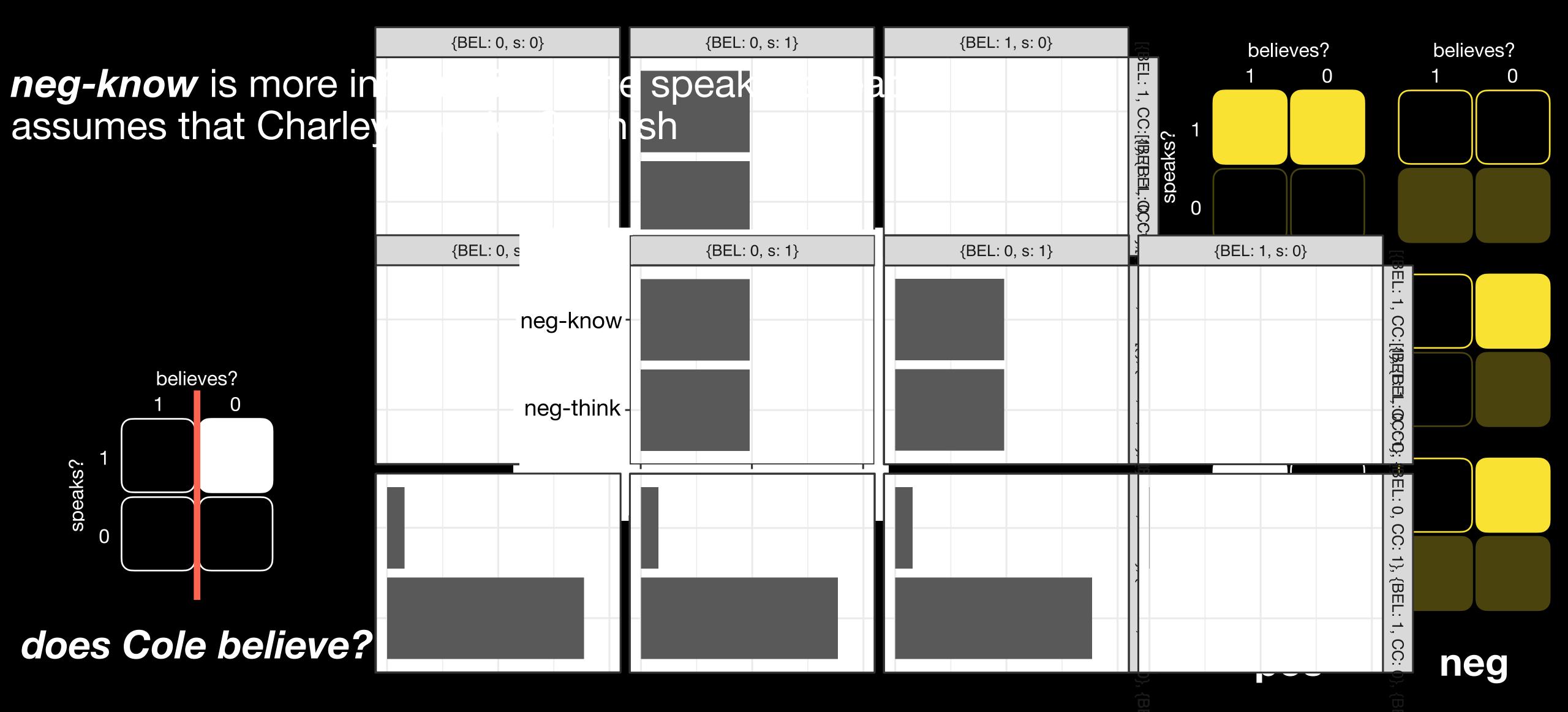


neg-know not particularly informative



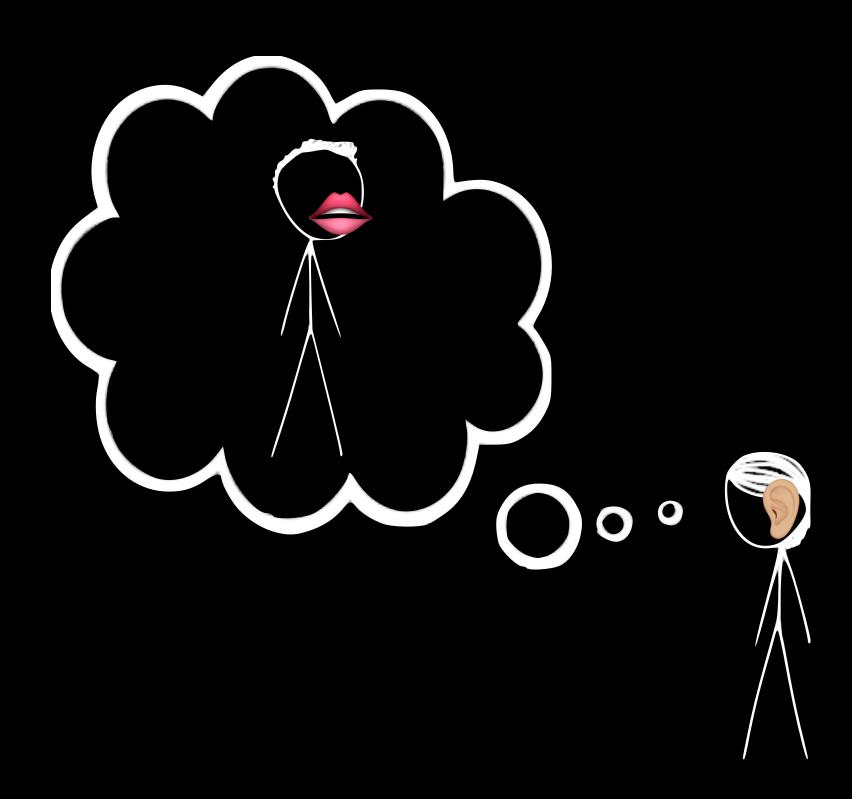






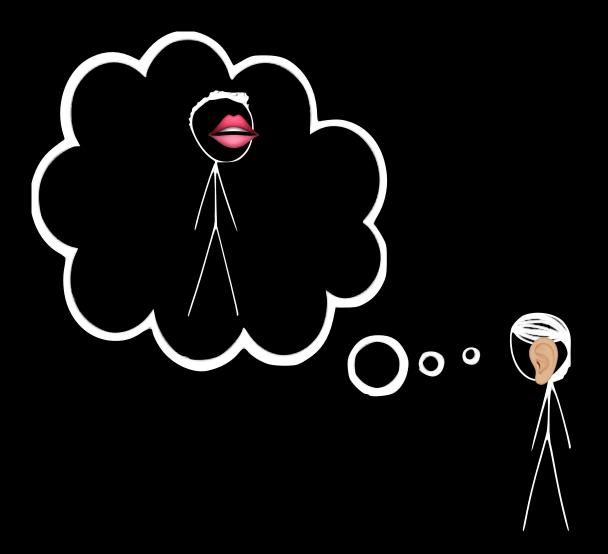
#### basic model intuition

listeners interpret utterances by **reasoning about** what would have led **a speaker** to produce the utterance in the first place



#### basic model intuition

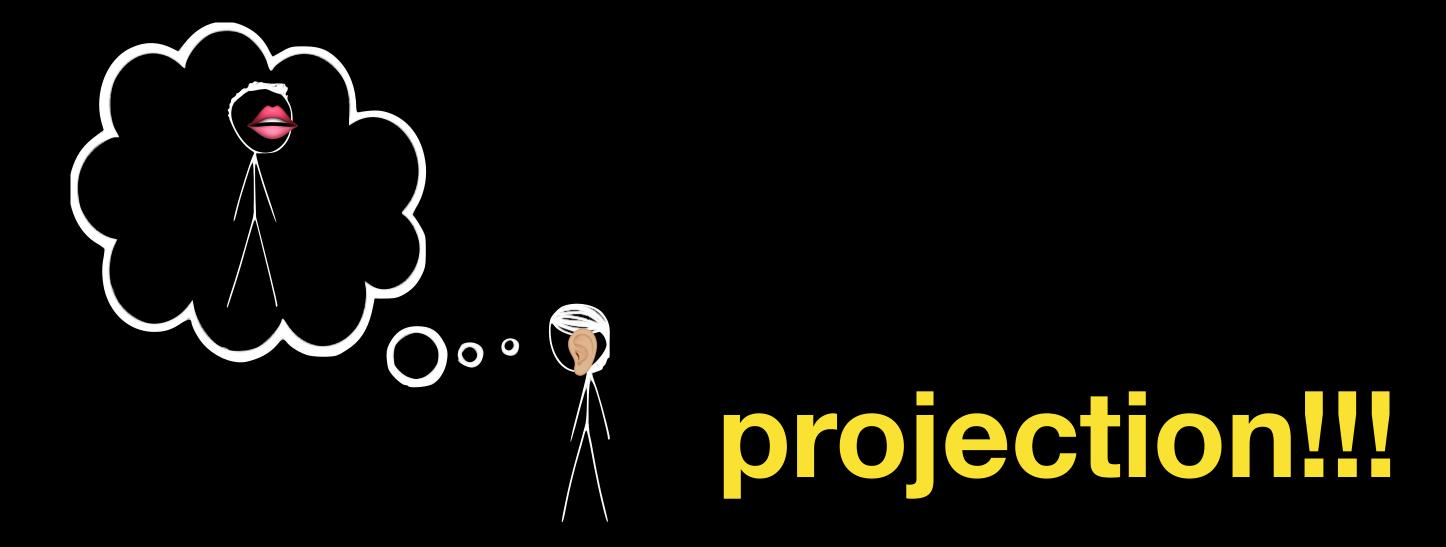
listeners interpret utterances by **reasoning about** what would have led **a speaker** to produce the utterance in the first place



when the listener hears "Cole doesn't know..." they are likely to inferthat the speaker assumes that Charley speaks Spanish

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when the listener hears "Cole doesn't know..." they are likely to infer that the speaker assumes that Charley speaks Spanish

#### Cole doesn't think/know that Charley speaks Spanish.

→ Charley speaks Spanish

# empirical targets

know projects more than think

(e.g., Kiparsky & Kiparsky 1970; Degen & Tonhauser 2022)

prior beliefs modulate projection

(e.g., Mahler 2020, 2022; Degen & Tonhauser 2021)

#### QUDs modulate projection

(e.g., Abrusán 2011, 2016; Simons et al 2017; Tonhauser et al. 2018, Degen & Tonhauser under review)

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# testing the empirical targets

know project ore than think

(e.g., Kiparsky & Kiparsh Degen & Tonhauser 2022)

prior beli s m ate projection

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QUDs Lugiection

(e.g., Abrusán 2011, 2016; Simons et al 2017

user et al. 2018, Degen & Tonhauser under review)

# experiment 1

Please read this text:		
Sue runs a company that connects language learners with remote teachers who live all over the world. She's trying to figure out how well her assistant, Cole, knows her remote teachers. Sue's business partner tells her what Cole said about Charley, who lives in Korea: "Cole knows that Charley speaks Spanish."		
Given what you have read above, how likely is it that Charley speaks Spanish?		
very unlikely	very likely	

n=833

Please read this text:	
Sue runs a company that connects language learners with remote teachers who live all over the world. She's putting together a list of the languages spoken by the remote teachers. After consulting her assistant, Cole, who knows the teachers and the languages they speak better than she does, Sue is currently working through the list of teachers to identify who speaks Spanish. When she gets to Charley, who lives in Mexico, Sue says to her business partner: "Cole doesn't think that Charley speaks Spanish."	
Given what you have read above, how	likely is it that Charley speaks Spanish?
very unlikely	very likely

read a story context, rate the probability of target content

## experiment 1

Please read this text:
Sue runs a company that connects language learners with remote teachers who live all over the world. She's trying to figure out how well her assistant, Cole, knows her remote teachers. Sue's business partner tells her what Cole said about Charley, who lives in Korea: "Cole knows"
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prior manipulation

Sue runs a language school. She's trying to figure out how well her five assistants Kate, Tom, Cole, Tatiana, and Riccardo know her remote teacher Charley. Sue keeps track on this list:

Assistants	Believes that Charley speaks Spanish?
Kate	yes
Tom	no
Cole	
Tatiana	
Riccardo	

Next up, she wants to record in her list whether

COLE believes that Charley speaks Spanish. Her

business partner tells her: "Cole thinks that

Charley speaks Spanish."

Given what you have read above, how likely is it that Charley speaks Spanish?

very unlikely

experiment 2

n=333

Sue runs a language school. She's currently working through a list of her teachers — Kate, Tom, Charley, Tatiana, and Riccardo — to identify who speaks Spanish. She occasionally consults Cole, who knows some teachers better. Sue keeps track on this list:

Teachers	Speaks Spanish?
Kate	yes
Tom	no
Charley	
Tatiana	
Riccardo	

Next up, she wants to record in the list whether

CHARLEY speaks Spanish. Sue says to her
business partner: "Cole knows that Charley

speaks Spanish."

Given what you have read above, how likely is it that Charley speaks Spanish?

very likely

very unlikely very likely

Sue runs a language school. She's trying to figure out how well her five assistants Kate, Tom, Cole, Tatiana, and Riccardo know her remote teacher Charley. Sue keeps track on this list:

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### experiment 2

n = 333

QUD manipulation

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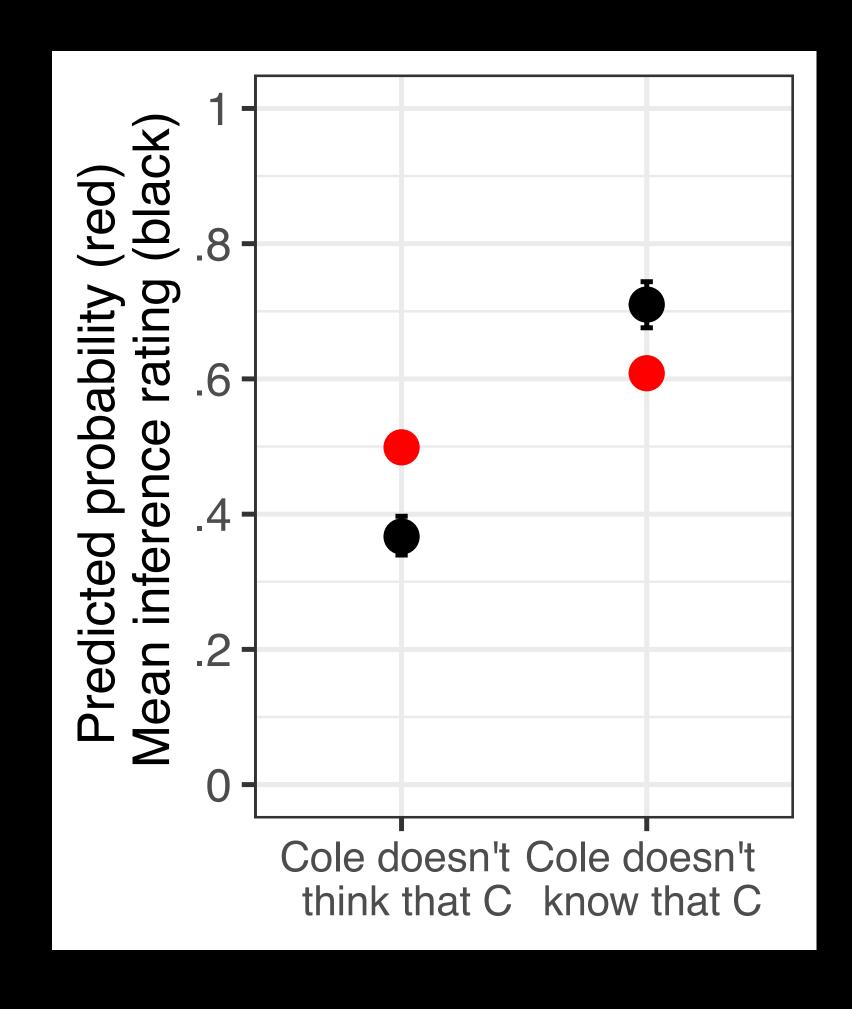
CHARLEY speaks Spanish. Sue says to her
business partner: "Cole knows that Charley

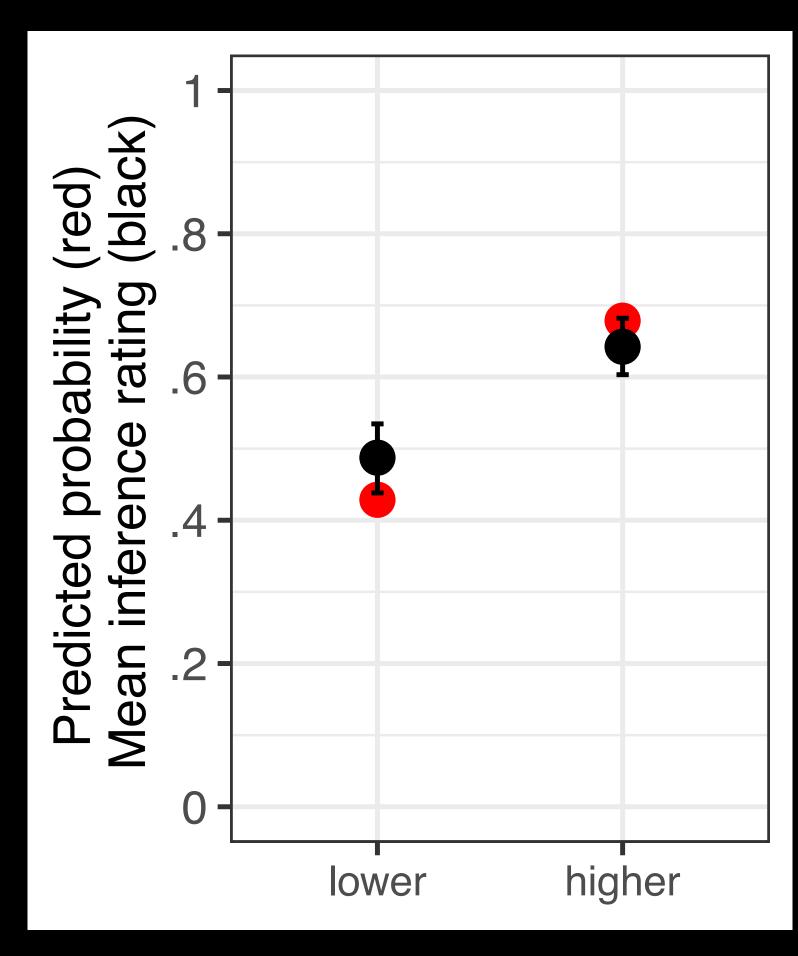
speaks Spanish."

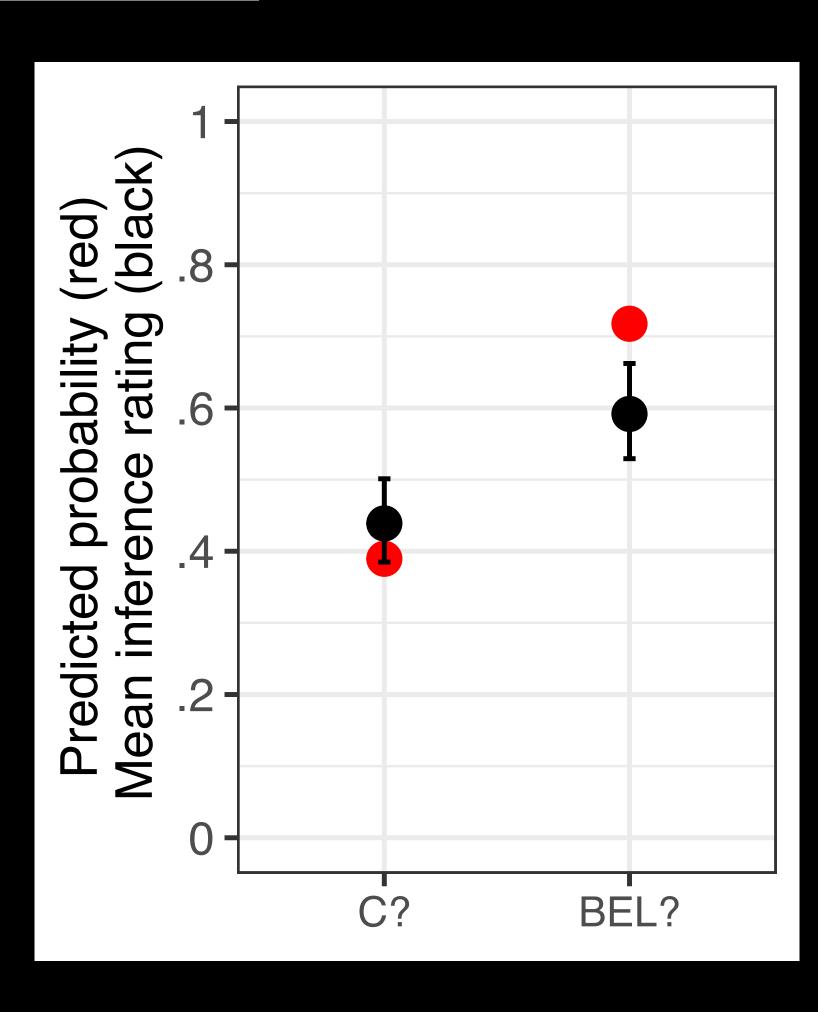
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## model predictions and human data







know projects
more than think

priors beliefs modulate projection

QUDs modulate projection

#### Cole doesn't think/know that Charley speaks Spanish.

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# no prior analysis makes all three predictions

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Cole doesn't think/know that Charley speaks Spanish.

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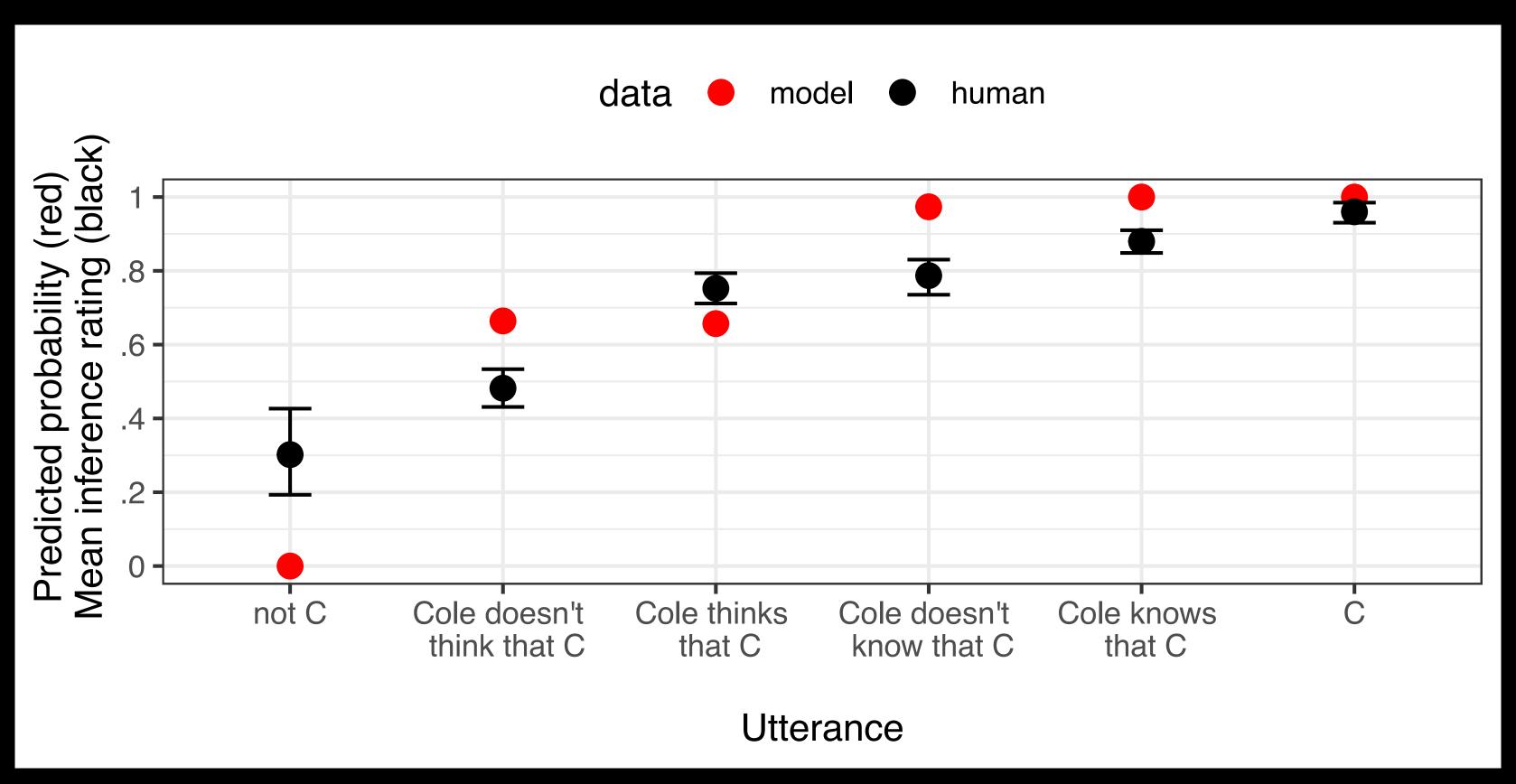




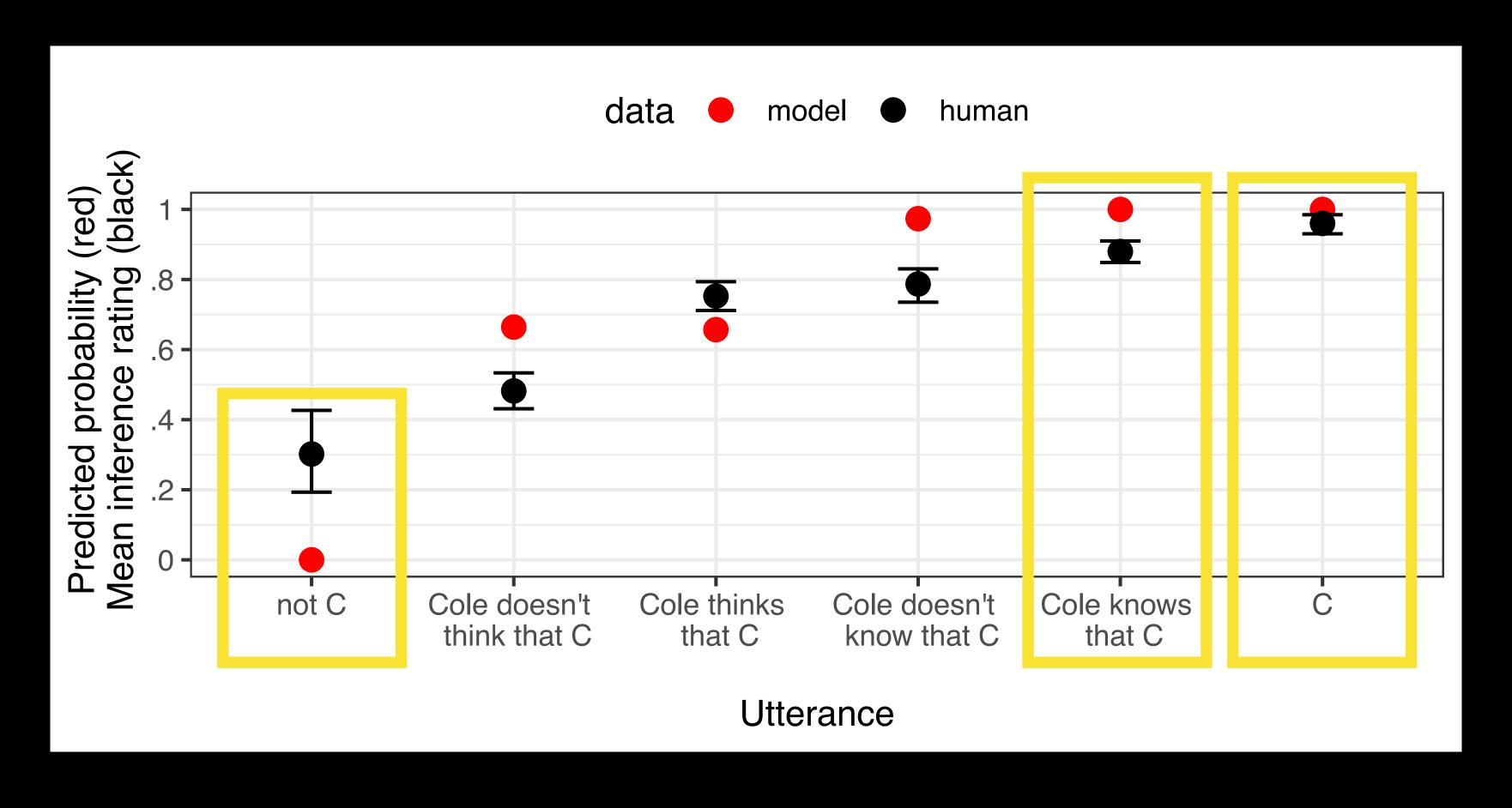
instead of developing analyses tailored to informative presuppositions, we **can** and **should** develop more general analyses that make predictions about inferences drawn from utterances

informative presuppositions are just one kind of inference

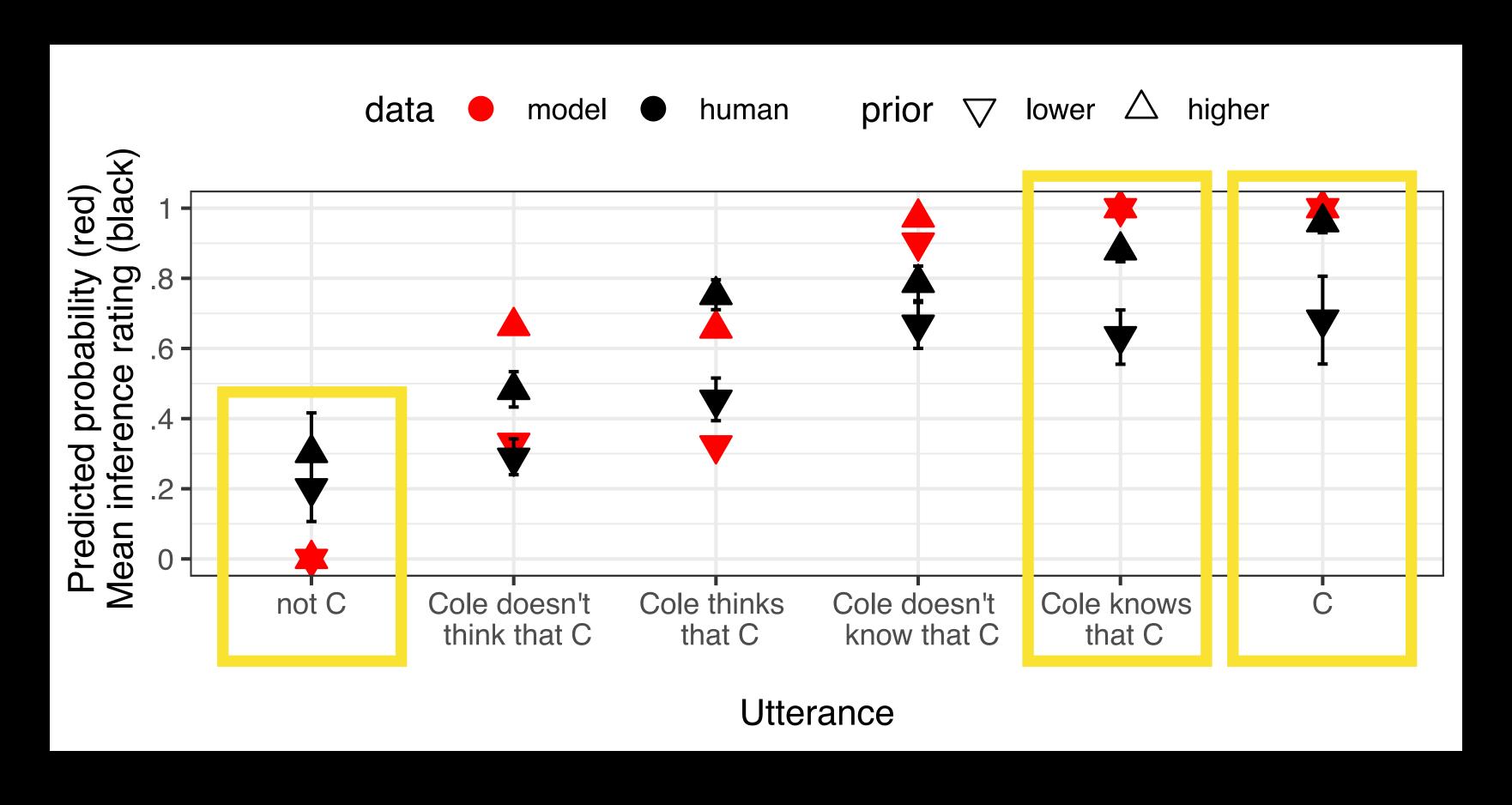




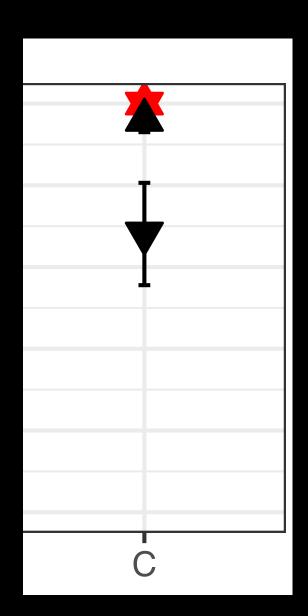
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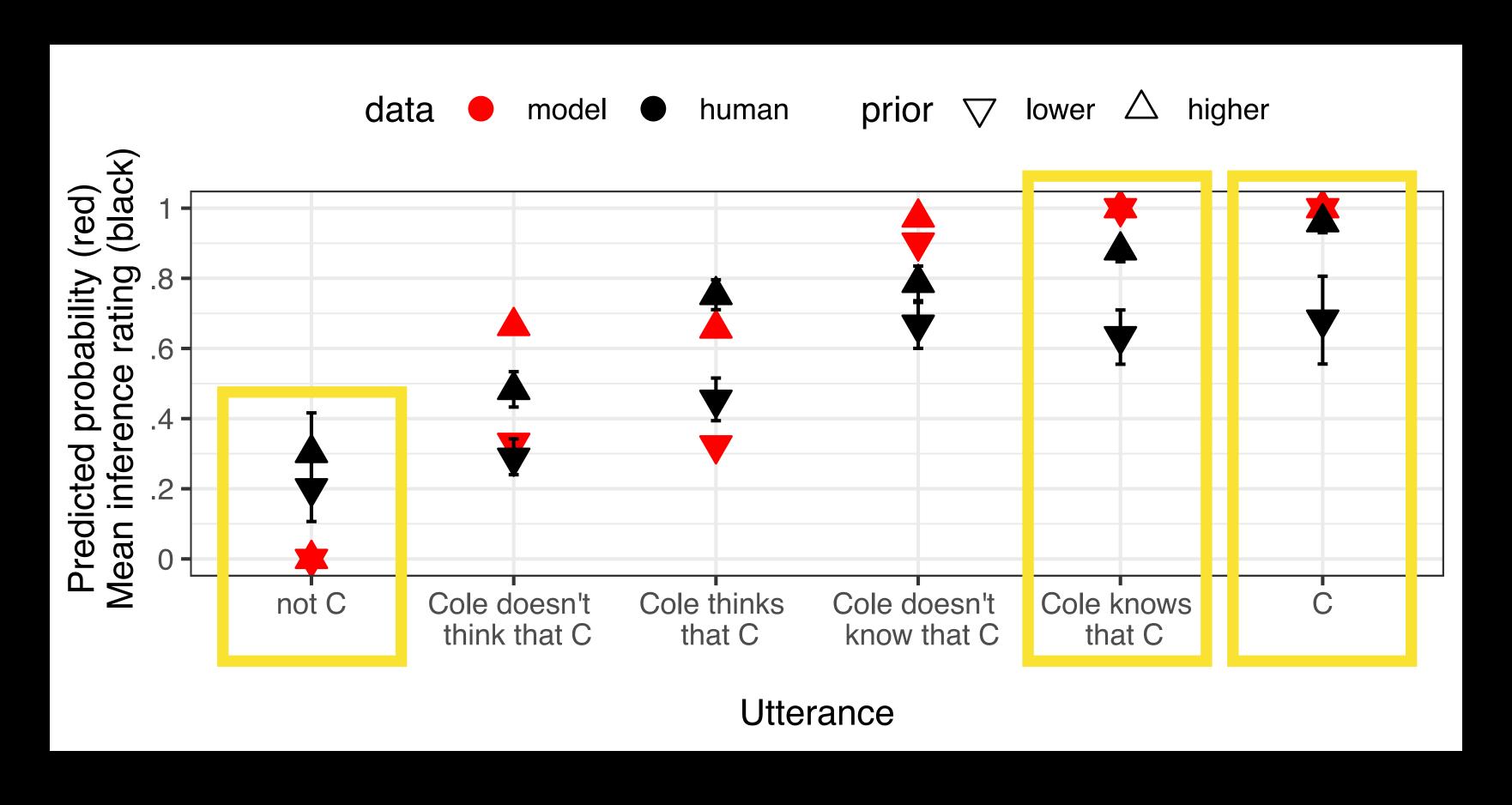
problem: too much reliance on literal semantics



problem: no sensitivity to the prior



problem: no sensitivity to the prior



problem: no sensitivity to the prior



### we need to relax the predictions of the model

option 1 relax the semantics

### we need to relax the predictions of the model

option 1 relax the semantics

option 2 relax the speaker

#### we need to relax the predictions of the model

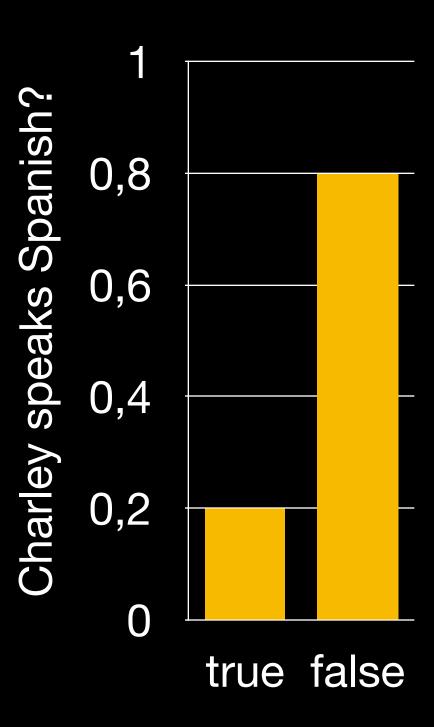
option 1 relax the semantics

option 2 relax the speaker

option 3 relax the listener

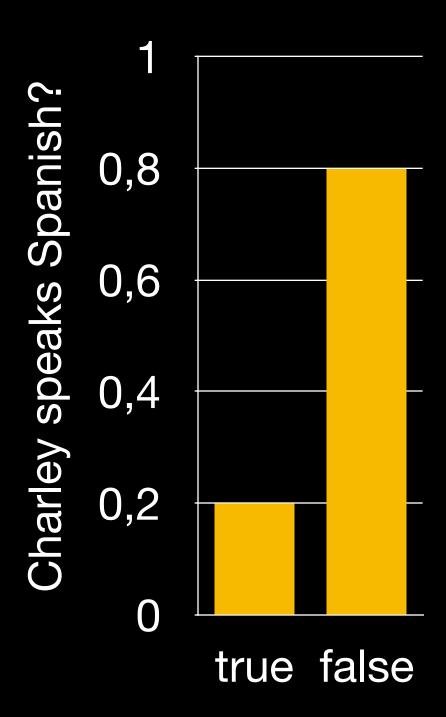
fact:
Charley lives in Korea

### prior belief



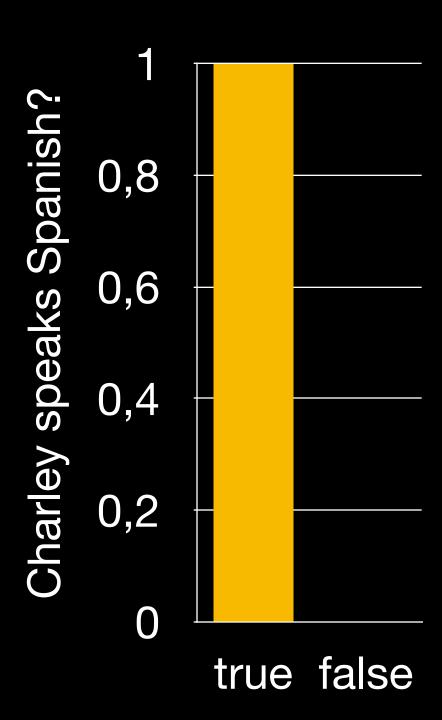
fact:
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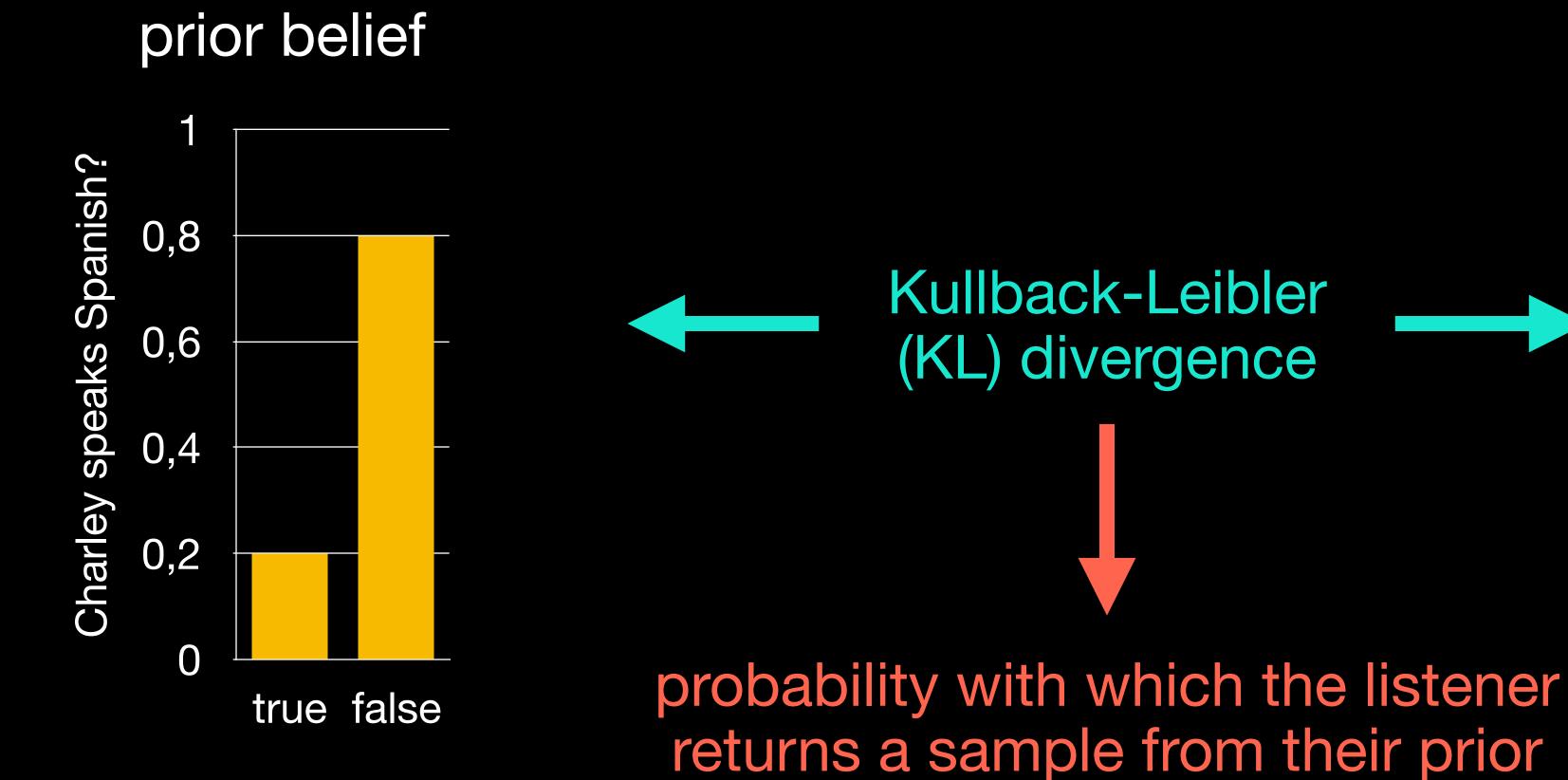


"Charley speaks Spanish."

#### posterior inference

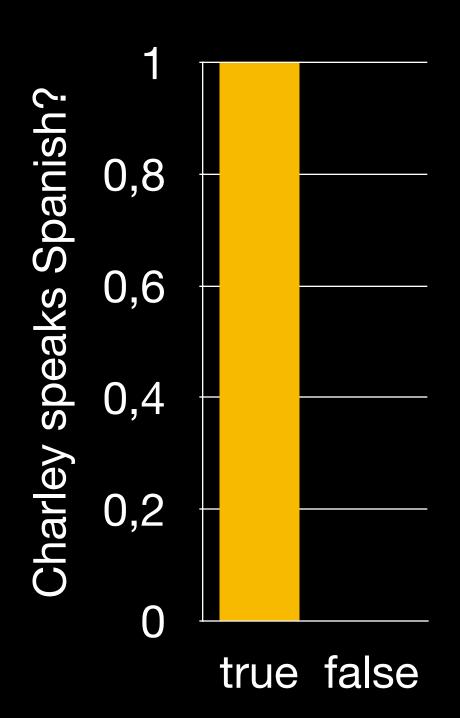


fact:
Charley lives in Korea



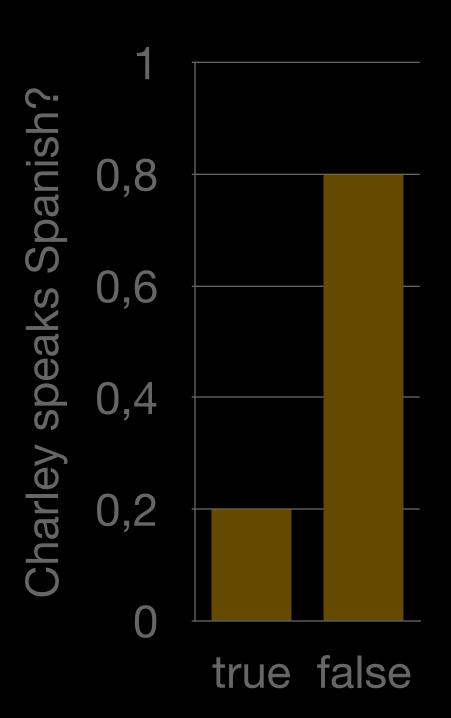
# utterance: "Charley speaks Spanish."

#### posterior inference

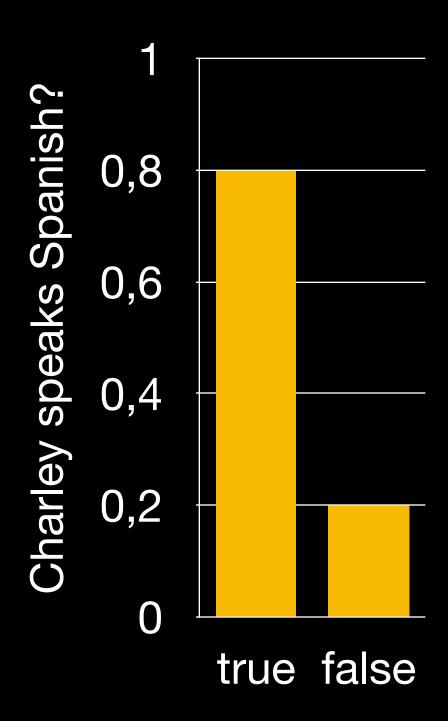


fact:
Charley lives in Korea

#### prior belief

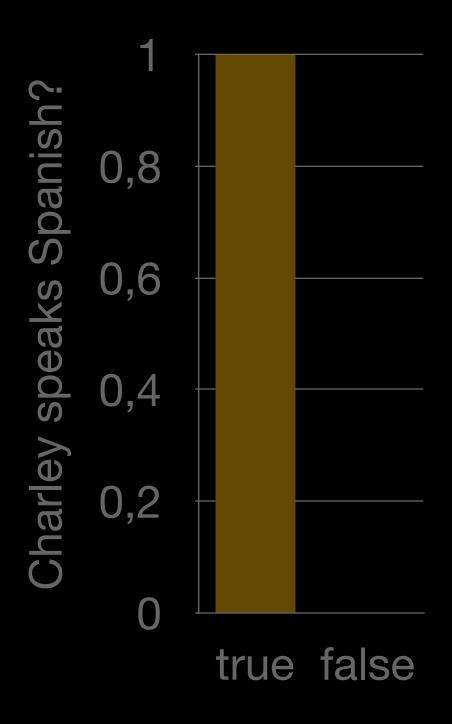


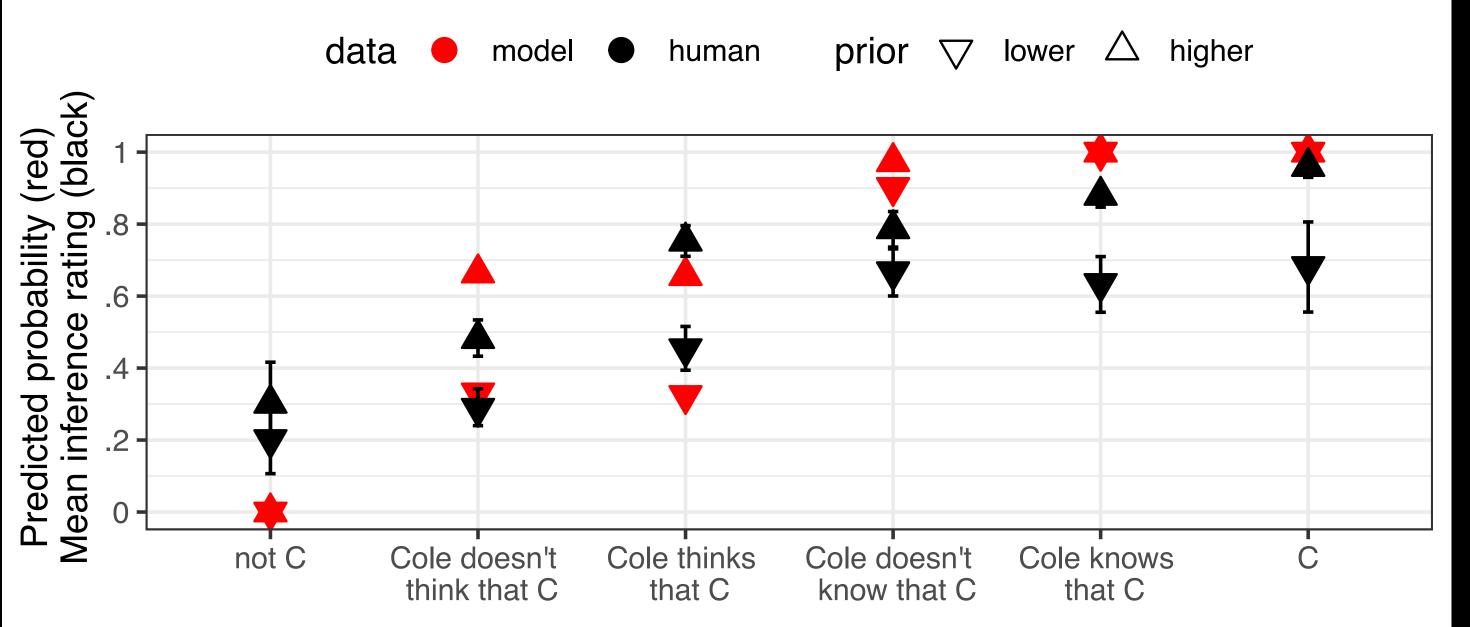
ultimate belief



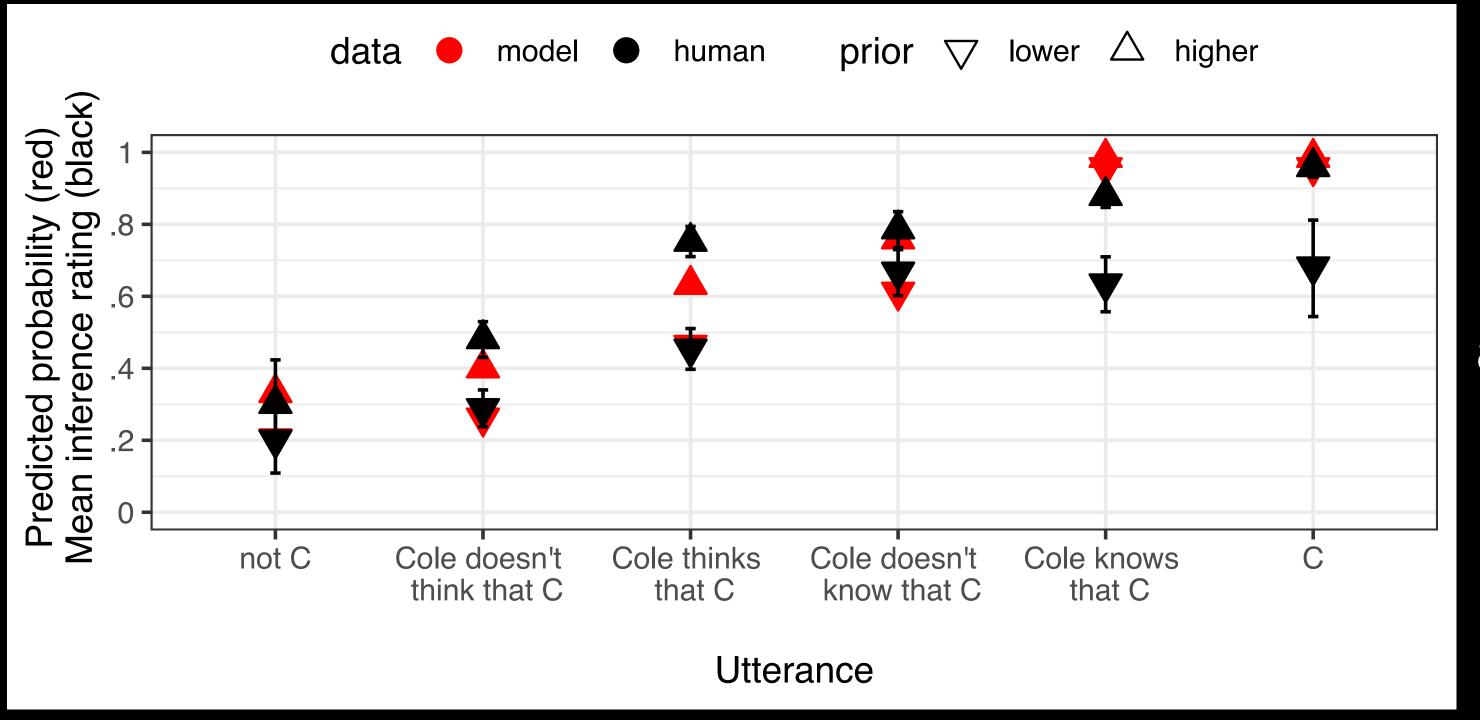
"Charley speaks Spanish."

### posterior inference





before



after



"The squirrel doesn't **know** that Estonia includes hundreds of islands, small and big."

→ Estonia includes hundreds of islands

#### Projection inferences

- without lexically coded presuppositions
- sensitive to prior beliefs and QUDs

Projection inferences are just one type of inference predicted by the analysis.

Prior beliefs modulate all kinds of inferences, as predicted by our RSA-model.



## thank you!